

# Package ‘ergm’

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**Title** Fit, Simulate and Diagnose Exponential-Family Models for Networks

**Depends** R (>= 4.2), network (>= 1.19.0)

**Imports** robustbase (>= 0.99-6), coda (>= 0.19-4.1), trust (>= 0.1-8), lpSolveAPI (>= 5.5.2.0-17.14), statnet.common (>= 4.13.0), rle (>= 0.10.0), purrr (>= 1.2.1), rlang (>= 1.1.7), memoise (>= 2.0.1), tibble (>= 3.3.1), magrittr (>= 2.0.4), Rdpack (>= 2.6.4), knitr (>= 1.51), stringr (>= 1.6.0), cli (>= 3.6.5), MASS, Matrix, parallel, methods

**Suggests** latticeExtra (>= 0.6-31), sna (>= 2.8), rmarkdown (>= 2.30), testthat (>= 3.3.2), ergm.count (>= 4.1.3), withr (>= 3.0.2), covr (>= 3.6.5), Rglpk (>= 0.6-5.1), slam (>= 0.1-55), networkLite (>= 1.1.0), lattice

**LinkingTo** cli

**RdMacros** Rdpack

**BugReports** <https://github.com/statnet/ergm/issues>

**Description** An integrated set of tools to analyze and simulate networks based on exponential-family random graph models (ERGMs). 'ergm' is a part of the Statnet suite of packages for network analysis. See Hunter, Handcock, Butts, Goodreau, and Morris (2008) <[doi:10.18637/jss.v024.i03](https://doi.org/10.18637/jss.v024.i03)> and Krivitsky, Hunter, Morris, and Klumb (2023) <[doi:10.18637/jss.v105.i06](https://doi.org/10.18637/jss.v105.i06)>.

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 'InitErgmConstraint.hints.R' 'InitErgmConstraint.operator.R'  
 'InitErgmProposal.R' 'InitErgmProposal.dyadnoise.R'  
 'InitErgmReference.R' 'InitErgmTerm.R' 'InitErgmTerm.auxnet.R'  
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 'summary.statistics.network.R' 'vcov.ergm.R' 'wtd.median.R'  
 'zzz.R'

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ergm-package	<i>ergm: Fit, Simulate and Diagnose Exponential-Family Models for Networks</i>
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## Description

An integrated set of tools to analyze and simulate networks based on exponential-family random graph models (ERGMs). 'ergm' is a part of the Statnet suite of packages for network analysis. See Hunter, Handcock, Butts, Goodreau, and Morris (2008) [doi:10.18637/jss.v024.i03](https://doi.org/10.18637/jss.v024.i03) and Krivitsky, Hunter, Morris, and Klumb (2023) [doi:10.18637/jss.v105.i06](https://doi.org/10.18637/jss.v105.i06).

## Details

For a complete list of the functions, use `library(help="ergm")` or read the rest of the manual. For a simple demonstration, use `demo(packages="ergm")`.

When publishing results obtained using this package, please cite the original authors as described in `citation(package="ergm")`.

All programs derived from this package must cite it. Please see the file LICENSE and <https://statnet.org/attribution>.

Recent advances in the statistical modeling of random networks have had an impact on the empirical study of social networks. Statistical exponential family models Strauss and Ikeda (1990) are a generalization of the Markov random network models introduced by Frank and Strauss (1986), which in turn derived from developments in spatial statistics Besag (1974). These models recognize the

complex dependencies within relational data structures. To date, the use of stochastic network models for networks has been limited by three interrelated factors: the complexity of realistic models, the lack of simulation tools for inference and validation, and a poor understanding of the inferential properties of nontrivial models.

This manual introduces software tools for the representation, visualization, and analysis of network data that address each of these previous shortcomings. The package relies on the `network` package which allows networks to be represented in `R`. The `ergm` package implements maximum likelihood estimates of ERGMs to be calculated using Markov Chain Monte Carlo (via `ergm()`). The package also provides tools for simulating networks (via `simulate.ergm()`) and assessing model goodness-of-fit (see `mcmc.diagnostics()` and `gof.ergm()`).

A number of Statnet Project packages extend and enhance `ergm`. These include `tergm` (Temporal ERGM), which provides extensions for modeling evolution of networks over time; `ergm.count`, which facilitates exponential family modeling for networks whose dyadic measurements are counts; and `ergm.userterms`, available on GitHub at <https://github.com/statnet/ergm.userterms>, which allows users to implement their own ERGM terms.

For detailed information on how to download and install the software, go to the `ergm` website: <https://statnet.org>. A tutorial, support newsgroup, references and links to further resources are provided there.

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#### See Also

[ergmTerm](#), [ergmConstraint](#), [ergmReference](#), [ergmHint](#), and [ergmProposal](#) for indices of model specification and estimation components visible to the **ergm**'s API at any given time.

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.dyads-ergmConstraint *A meta-constraint indicating handling of arbitrary dyadic constraints*

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#### Description

This is a flag in the proposal table indicating that the proposal can enforce arbitrary combinations of dyadic constraints. It cannot be invoked directly by the user.

#### See Also

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** None

---

absdiff-ergmTerm      *Absolute difference in nodal attribute*

---

### Description

This term adds one network statistic to the model equaling the sum of  $\text{abs}(\text{attr}[i]-\text{attr}[j])^{\text{pow}}$  for all edges  $(i, j)$  in the network.

### Usage

```
# binary: absdiff(attr,
#               pow=1)

# valued: absdiff(attr,
#               pow=1,
#               form="sum")
```

### Arguments

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
pow	power to which to take the absolute difference
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

### Note

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, quantitative nodal attribute, undirected, binary, valued

---

absdiffcat-ergmTerm     *Categorical absolute difference in nodal attribute*

---

## Description

This term adds one statistic for every possible nonzero distinct value of `abs(attr[i]-attr[j])` in the network. The value of each such statistic is the number of edges in the network with the corresponding absolute difference.

## Usage

```
# binary: absdiffcat(attr,
#                   base=NULL,
#                   levels=NULL)

# valued: absdiffcat(attr,
#                   base=NULL,
#                   levels=NULL,
#                   form="sum")
```

## Arguments

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>base</code>	deprecated
<code>levels</code>	specifies which nonzero difference to include in or exclude from the model. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

## Note

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

## See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, undirected, binary, valued

---

altkstar-ergmTerm      *Alternating k-star*

---

### Description

Add one network statistic to the model equal to a weighted alternating sequence of  $k$ -star statistics with weight parameter  $\lambda$ .

### Usage

```
# binary: altkstar(lambda,
#                   fixed=FALSE)
```

### Arguments

<code>lambda</code>	weight parameter to model
<code>fixed</code>	indicates whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential family model (see Hunter and Handcock 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a CEF model.

### Details

This is the version given by Snijders et al. (2006). The `gwdegree` and `altkstar` produce mathematically equivalent models, as long as they are used together with the edges (or `kstar(1)`) term, yet the interpretation of the `gwdegree` parameters is slightly more straightforward than the interpretation of the `altkstar` parameters. For this reason, we recommend the use of the `gwdegree` instead of `altkstar`. See Section 3 and especially equation (13) of Hunter (2007) for details.

### Note

This term can only be used with undirected networks.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, curved, undirected, binary

---

`anova.ergm`*ANOVA for ERGM Fits*

---

### Description

Compute an analysis of variance table for one or more ERGM fits.

### Usage

```
## S3 method for class 'ergm'  
anova(object, ..., eval.loglik = FALSE)  
  
## S3 method for class 'ergmlist'  
anova(object, ..., eval.loglik = FALSE)
```

### Arguments

`object, ...` objects of `ergm`, usually, a result of a call to `ergm()`.  
`eval.loglik` a logical specifying whether the log-likelihood will be evaluated if missing.

### Details

Specifying a single object gives a sequential analysis of variance table for that fit. That is, the reductions in the residual sum of squares as each term of the formula is added in turn are given in the rows of a table, plus the residual sum of squares.

The table will contain F statistics (and P values) comparing the mean square for the row to the residual mean square.

If more than one object is specified, the table has a row for the residual degrees of freedom and sum of squares for each model. For all but the first model, the change in degrees of freedom and sum of squares is also given. (This only make statistical sense if the models are nested.) It is conventional to list the models from smallest to largest, but this is up to the user.

If any of the objects do not have estimated log-likelihoods, produces an error, unless `eval.loglik=TRUE`.

### Value

An object of class "anova" inheriting from class "data.frame".

### Warning

The comparison between two or more models will only be valid if they are fitted to the same dataset. This may be a problem if there are missing values and 's default of `na.action = na.omit` is used, and `anova.ergmlist()` will detect this with an error.

### See Also

The model fitting function `ergm()`, `anova()`, `logLik.ergm()` for adding the log-likelihood to an existing `ergm` object.

**Examples**

```

data(molecule)
molecule %v% "atomic type" <- c(1,1,1,1,1,1,2,2,2,2,2,2,3,3,3,3,3,3)
fit0 <- ergm(molecule ~ edges)
anova(fit0)
fit1 <- ergm(molecule ~ edges + nodefactor("atomic type"))
anova(fit1)

fit2 <- ergm(molecule ~ edges + nodefactor("atomic type") + gwesp(0.5,
  fixed=TRUE), eval.loglik=TRUE) # Note the eval.loglik argument.
anova(fit0, fit1)
anova(fit0, fit1, fit2)

```

---

```
approx.hotelling.diff.test
```

*Approximate Hotelling  $T^2$ -Test for One or Two Population Means*

---

**Description**

A multivariate hypothesis test for a single population mean or a difference between them. This version attempts to adjust for multivariate autocorrelation in the samples.

**Usage**

```

approx.hotelling.diff.test(
  x,
  y = NULL,
  mu0 = 0,
  assume.indep = FALSE,
  var.equal = FALSE,
  ...
)

```

**Arguments**

<code>x</code>	a numeric matrix of data values with cases in rows and variables in columns.
<code>y</code>	an optional matrix of data values with cases in rows and variables in columns for a 2-sample test.
<code>mu0</code>	an optional numeric vector: for a 1-sample test, the population mean under the null hypothesis; and for a 2-sample test, the difference between population means under the null hypothesis; defaults to a vector of 0s.
<code>assume.indep</code>	if TRUE, performs an ordinary Hotelling's test without attempting to account for autocorrelation.
<code>var.equal</code>	for a 2-sample test, perform the pooled test: assume population variance-covariance matrices of the two variables are equal.

... additional arguments, passed on to `spectrum0.mvar()`, etc.; in particular, order `.max=` can be used to limit the order of the AR model used to estimate the effective sample size.

### Value

An object of class `htest` with the following information:

<code>statistic</code>	The $T^2$ statistic.
<code>parameter</code>	Degrees of freedom.
<code>p.value</code>	P-value.
<code>method</code>	Method specifics.
<code>null.value</code>	Null hypothesis mean or mean difference.
<code>alternative</code>	Always "two.sided".
<code>estimate</code>	Sample difference.
<code>covariance</code>	Estimated variance-covariance matrix of the estimate of the difference.
<code>covariance.x</code>	Estimated variance-covariance matrix of the estimate of the mean of x.
<code>covariance.y</code>	Estimated variance-covariance matrix of the estimate of the mean of y.

It has a print method `print.htest()`.

### Note

For `mcmc.list` input, the variance for this test is estimated with unpooled means. This is not strictly correct.

### References

Hotelling H (1947). "Multivariate Quality Control." In Eisenhart C, Hastay MW, Wallis WA (eds.), *Techniques of Statistical Analysis*. McGraw-Hill, New York.

### See Also

`t.test()`

---

as.network.numeric      *Create a Simple Random network of a Given Size*

---

### Description

`as.network.numeric()` creates a random Bernoulli network of the given size as an object of class `network`.

**Usage**

```
## S3 method for class 'numeric'
as.network(
  x,
  directed = TRUE,
  hyper = FALSE,
  loops = FALSE,
  multiple = FALSE,
  bipartite = FALSE,
  ignore.eval = TRUE,
  names.eval = NULL,
  edge.check = FALSE,
  density = NULL,
  init = NULL,
  numedges = NULL,
  ...
)
```

**Arguments**

<code>x</code>	count; the number of nodes in the network
<code>directed</code>	logical; should edges be interpreted as directed?
<code>hyper</code>	logical; are hyperedges allowed? Currently ignored.
<code>loops</code>	logical; should loops be allowed? Currently ignored.
<code>multiple</code>	logical; are multiplex edges allowed? Currently ignored.
<code>bipartite</code>	count; should the network be interpreted as bipartite? If present (i.e., non-NULL) it is the count of the number of actors in the bipartite network. In this case, the number of nodes is equal to the number of actors plus the number of events (with all actors preceding all events). The edges are then interpreted as nondirected.
<code>ignore.eval</code>	logical; ignore edge values? Currently ignored.
<code>names.eval</code>	optionally, the name of the attribute in which edge values should be stored. Currently ignored.
<code>edge.check</code>	logical; perform consistency checks on new edges?
<code>density</code>	numeric; the probability of a tie for Bernoulli networks. If neither <code>density</code> nor <code>init</code> is given, it defaults to the number of nodes divided by the number of dyads (so the expected number of ties is the same as the number of nodes.)
<code>init</code>	numeric; the log-odds of a tie for Bernoulli networks. It is only used if <code>density</code> is not specified.
<code>numedges</code>	count; if present, sample the Bernoulli network conditional on this number of edges (rather than independently with the specified probability).
<code>...</code>	additional arguments

**Details**

The network will not have vertex, edge or network attributes. These can be added with operators such as %v%, %n%, %e%.

**Value**

An object of class `network`

**References**

Butts CT (2002). “Memory Structures for Relational Data in R: Classes and Interfaces.” Working Paper.

**See Also**

`network`

**Examples**

```
# Draw a random directed network with 25 nodes
g <- network(25)

# Draw a random undirected network with density 0.1
g <- network(25, directed=FALSE, density=0.1)

# Draw a random bipartite network with 4 actors and 6 events and density 0.1
g <- network(10, bipartite=4, directed=FALSE, density=0.1)

# Draw a random directed network with 25 nodes and 50 edges
g <- network(25, numedges=50)
```

---

asymmetric-ergmTerm    *Asymmetric dyads*

---

**Description**

This term adds one network statistic to the model equal to the number of pairs of actors for which exactly one of  $(i \rightarrow j)$  or  $(j \rightarrow i)$  exists.

**Usage**

```
# binary: asymmetric(attr=NULL, diff=FALSE, keep=NULL, levels=NULL)
```

**Arguments**

attr	quantitative attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) If specified, only symmetric pairs that match on the vertex attribute are counted.
diff	Used in the same way as for the <code>nodematch</code> term. (See <code>nodematch(ergmTerm?nodematch)</code> for details.)
keep	deprecated
level	Used in the same way as for the <code>nodematch</code> term. (See <code>nodematch(ergmTerm?nodematch)</code> for details.)

**Note**

This term can only be used with directed networks.

The argument `keep` is retained for backwards compatibility and may be removed in a future version. When both `keep` and `levels` are passed, `levels` overrides `keep`. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, triad-related, binary

---

atleast-ergmTerm	<i>Number of dyads with values greater than or equal to a threshold</i>
------------------	---

---

**Description**

Adds the number of statistics equal to the length of `threshold` equaling to the number of dyads whose values equal or exceed the corresponding element of `threshold`.

**Usage**

```
# valued: atleast(threshold=0)
```

**Arguments**

threshold	vector of numerical values
-----------	----------------------------

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

atmost-ergmTerm	<i>Number of dyads with values less than or equal to a threshold</i>
-----------------	--

---

**Description**

Adds the number of statistics equal to the length of threshold equaling to the number of dyads whose values equal or are exceeded by the corresponding element of threshold .

**Usage**

```
# valued: atmost(threshold=0)
```

**Arguments**

threshold      a vector of numerical values

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

attrcov-ergmTerm	<i>Edge covariate by attribute pairing</i>
------------------	--

---

**Description**

This term adds one statistic to the model, equal to the sum of the covariate values for each edge appearing in the network, where the covariate value for a given edge is determined by its mixing type on attr. Undirected networks are regarded as having undirected mixing, and it is assumed that mat is symmetric in that case.

This term can be useful for simulating large networks with many mixing types, where nodemix would be slow due to the large number of statistics, and edgescov cannot be used because an adjacency matrix would be too big.

**Usage**

```
# binary: attrcov(attr, mat)
```

```
# valued: attrcov(attr, mat, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
mat	a matrix of covariates with the same dimensions as a mixing matrix for attr
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, binary, valued

---

B-ergmTerm

*Wrap binary terms for use in valued models*

---

**Description**

Wraps binary ergm terms for use in valued models, with formula specifying which terms are to be wrapped and form specifying how they are to be used and how the binary network they are evaluated on is to be constructed.

**Usage**

```
# valued: B(formula, form)
```

**Arguments**

formula	a one-sided <a href="#">ergm()</a> -style formula whose RHS contains the binary ergm terms to be evaluated. Which terms may be used depends on the argument form
form	One of three values: <ul style="list-style-type: none"> <li>• "sum": see section "Generalizations of binary terms" in <a href="#">ergmTerm</a> help; all terms in formula must be dyad-independent.</li> <li>• "nonzero": section "Generalizations of binary terms" in <a href="#">ergmTerm</a> help; any binary ergm terms may be used in formula .</li> <li>• a one-sided formula value-dependent network. form must contain one "valued" ergm term, with the following properties: <ul style="list-style-type: none"> <li>– dyadic independence;</li> <li>– dyadwise contribution of either 0 or 1; and</li> <li>– dyadwise contribution of 0 for a 0-valued dyad.</li> </ul> </li> </ul>

Formally, this means that it is expressible as

$$g(y) = \sum_{i,j} f_{i,j}(y_{i,j}),$$

where for all  $i, j$ , and  $y$ ,  $f_{i,j}(y_{i,j})$  is either 0 or 1 and, in particular,  $f_{i,j}(0) = 0$ .

Examples of such terms include `nonzero`, `ininterval()`, `atleast()`, `atmost()`, `greaterthan()`, `lessthen()`, and `equalto()`.

Then, the value of the statistic will be the value of the statistics in formula evaluated on a binary network that is defined to have an edge if and only if the corresponding dyad of the valued network adds 1 to the valued term in form.

### Details

For example, `B(~nodecov("a"), form="sum")` is equivalent to `nodecov("a", form="sum")` and similarly with `form="nonzero"`.

When a valued implementation is available, it should be preferred, as it is likely to be faster.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, valued

---

b1concurrent-ergmTerm *Concurrent node count for the first mode in a bipartite network*

---

### Description

This term adds one network statistic to the model, equal to the number of nodes in the first mode of the network with degree 2 or higher. The first mode of a bipartite network object is sometimes known as the "actor" mode. This term can only be used with undirected bipartite networks.

### Usage

```
# binary: b1concurrent(by=NULL, levels=NULL)
```

### Arguments

by	optional argument specifying a vertex attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details). It functions just like the <code>by</code> argument of the <code>b1degree</code> term. Without the optional argument, this statistic is equivalent to <code>b1mindegree(2)</code> .
levels	TODO (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b1cov-ergmTerm

*Main effect of a covariate for the first mode in a bipartite network*


---

**Description**

This term adds a single network statistic for each quantitative attribute or matrix column to the model equaling the total value of `attr(i)` for all edges  $(i, j)$  in the network. This term may only be used with bipartite networks. For categorical attributes, see `b1factor`.

**Usage**

```
# binary: b1cov(attr)
# valued: b1cov(attr, form="sum")
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, dyad-independent, frequently-used, quantitative nodal attribute, undirected, binary, valued

---

b1covrange-ergmTerm     *Range of covariate values for neighbors of a mode-1 node*

---

### Description

This term adds a single network statistic equalling the sum over the nodes of the range over of its neighbors' values.

### Usage

```
# binary: nodecovrange(attr)
```

### Arguments

attr                    a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal\_attributes) for details.)

### Details

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

### References

Hoffman M, Block P, Snijders TAB (2023). "Modeling Partitions of Individuals." *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:10.1177/00811750221145166.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, quantitative nodal attribute, binary

---

b1degrange-ergmTerm     *Degree range for the first mode in a bipartite network*

---

### Description

This term adds one network statistic to the model for each element of from (or to ); the  $i$ th such statistic equals the number of nodes of the first mode ("actors") in the network of degree greater than or equal to from[i] but strictly less than to[i] , i.e. with edge count in semiopen interval [from,to) .

This term can only be used with bipartite networks; for directed networks see idegrange and odegrange . For undirected networks, see degrange , and see b2degrange for degrees of the second mode ("events").

**Usage**

```
# binary: b1degrange(from, to=`+Inf`, by=NULL, homophily=FALSE, levels=NULL)
```

**Arguments**

from, to           vectors of distinct integers. If one of the vectors have length 1, it is recycled to the length of the other. Otherwise, it must have the same length.

by, levels, homophily  
 the optional argument by specifies a vertex attribute (see Specifying Vertex attributes and Levels (?nodal\_attributes) for details). If this is specified and homophily is TRUE , then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the by attribute. If by is specified and homophily is FALSE (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. levels selects which levels of by' to include.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

b1degree-ergmTerm	<i>Degree for the first mode in a bipartite network</i>
-------------------	---

---

**Description**

This term adds one network statistic to the model for each element in d ; the *i*th such statistic equals the number of nodes of degree d[*i*] in the first mode of a bipartite network, i.e. with exactly d[*i*] edges. The first mode of a bipartite network object is sometimes known as the "actor" mode.

**Usage**

```
# binary: b1degree(d, by=NULL, levels=NULL)
```

**Arguments**

d                   a vector of distinct integers.

by, levels, homophily  
 the optional argument by specifies a vertex attribute (see Specifying Vertex attributes and Levels (?nodal\_attributes) for details). If this is specified and homophily is TRUE , then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the by attribute. If by is specified and homophily is FALSE (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. levels selects which levels of by' to include.

**Note**

This term can only be used with undirected bipartite networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, frequently-used, undirected, binary

b1degrees-ergmConstraint

*Preserve the actor degree for bipartite networks*

**Description**

For bipartite networks, preserve the degree for the first mode of each vertex of the given network, while allowing the degree for the second mode to vary.

**Usage**

```
# b1degrees
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** bipartite

b1dsp-ergmTerm

*Dyadwise shared partners for dyads in the first bipartition*

**Description**

This term adds one network statistic to the model for each element in  $d$ ; the  $i$ th such statistic equals the number of dyads in the first bipartition with exactly  $d[i]$  shared partners. (Those shared partners, of course, must be members of the second bipartition.) This term can only be used with bipartite networks.

**Usage**

```
# binary: b1dsp(d)
```

**Arguments**

$d$  a vector of distinct integers.

**Note**

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

b1factor-ergmTerm	<i>Factor attribute effect for the first mode in a bipartite network</i>
-------------------	--

---

**Description**

This term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute. Each of these statistics gives the number of times a node with that attribute in the first mode of the network appears in an edge. The first mode of a bipartite network object is sometimes known as the "actor" mode.

**Usage**

```
# binary: b1factor(attr, base=1, levels=-1)

# valued: b1factor(attr, base=1, levels=-1, form="sum")
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>base</code>	deprecated
<code>levels</code>	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

To include all attribute values is usually not a good idea, because the sum of all such statistics equals the number of edges and hence a linear dependency would arise in any model also including edges. The default, `levels=-1`, is therefore to omit the first (in lexicographic order) attribute level. To include all levels, pass either `levels=TRUE` (i.e., keep all levels) or `levels=NULL` (i.e., do not filter levels).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

This term can only be used with undirected bipartite networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, dyad-independent, frequently-used, undirected, binary, valued

---

b1factordistinct-ergmTerm

*Number of distinct neighbor types for the first node*

---

**Description**

This term adds a single network statistic to the model, counting, for each node, the number of distinct values of the attribute found among its neighbors.

**Usage**

```
# binary: b1factordistinct(attr, levels=TRUE)
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>levels</code>	this optional argument controls which levels of the attribute attributes and Levels ( <a href="#">?nodal_attributes</a> ) for details.)

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). “Modeling Partitions of Individuals.” *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:[10.1177/00811750221145166](https://doi.org/10.1177/00811750221145166).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, binary

b1mindegree-ergmTerm *Minimum degree for the first mode in a bipartite network*

**Description**

This term adds one network statistic to the model for each element in `d`; the  $i$ th such statistic equals the number of nodes in the first mode of a bipartite network with at least degree `d[i]`. The first mode of a bipartite network object is sometimes known as the "actor" mode.

**Usage**

```
# binary: b1mindegree(d)
```

**Arguments**

`d` a vector of distinct integers.

**Note**

This term can only be used with undirected bipartite networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

b1nodematch-ergmTerm *Nodal attribute-based homophily effect for the first mode in a bipartite network*

**Description**

This term is introduced in Bomirya et al. (2023). With the default `alpha` and `beta` values, this term will simply be a homophily based two-star statistic. This term adds one statistic to the model unless `diff` is set to `TRUE`, in which case the term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute.

**Usage**

```
# binary: b1nodematch(attr, diff=FALSE, keep=NULL, alpha=1, beta=1, byb2attr=NULL,
#                       levels=NULL)
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
diff	by default, one statistic will be added to the model. If diff is set to TRUE, one statistic will be added for each unique value of the attr attribute
keep	deprecated
alpha, beta	optional discount parameters both of which take values from $[0, 1]$ , only one should be set at one time
byb2attr	specifies a second mode categorical attribute. Setting this argument will separate the original statistics based on the values of the set second mode attribute— i.e. for example, if diff is FALSE , then the sum of all the statistics for each level of this second-mode attribute will be equal to the original b1nodematch statistic where byb2attr set to NULL .
levels	select a subset of attr values to include. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**Details**

If an alpha discount parameter is used, each of these statistics gives the sum of the number of common second-mode nodes raised to the power alpha for each pair of first-mode nodes with that attribute. If a beta discount parameter is used, each of these statistics gives half the sum of the number of two-paths with two first-mode nodes with that attribute as the two ends of the two path raised to the power beta for each edge in the network.

**Note**

This term can only be used with undirected bipartite networks.

The argument keep is retained for backwards compatibility and may be removed in a future version. When both keep and levels are passed, levels overrides keep. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, dyad-independent, frequently-used, undirected, binary

---

b1sociality-ergmTerm *Degree*

---

**Description**

This term adds one network statistic for each node in the first bipartition, equal to the number of ties of that node. This term can only be used with bipartite networks. For directed networks, see sender and receiver. For unipartite networks, see [sociality](#).

**Usage**

```
# binary: b1sociality(nodes=-1)

# valued: b1sociality(nodes=-1, form="sum")
```

**Arguments**

nodes	By default, nodes=-1 means that the statistic for the first node (in the second bipartition) will be omitted, but this argument may be changed to control which statistics are included. The nodes argument is interpreted using the new UI for level specification (see Specifying Vertex Attributes and Levels (?nodal_attributes) for details), where both the attribute and the sorted unique values are the vector of vertex indices (nb1 + 1):n , where nb1 is the size of the first bipartition and n is the total number of nodes in the network. Thus nodes=120 will include only the statistic for the 120th node in the second bipartition, while nodes=I(120) will include only the statistic for the 120th node in the entire network.
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, dyad-independent, undirected, binary, valued

---

b1star-ergmTerm

*k-stars for the first mode in a bipartite network*


---

**Description**

This term adds one network statistic to the model for each element in  $k$ . The  $i$ th such statistic counts the number of distinct  $k[i]$ -stars whose center node is in the first mode of the network. The first mode of a bipartite network object is sometimes known as the "actor" mode. A  $k$ -star is defined to be a center node  $N$  and a set of  $k$  different nodes  $\{O_1, \dots, O_k\}$  such that the ties  $\{N, O_i\}$  exist for  $i = 1, \dots, k$ . This term can only be used for undirected bipartite networks.

**Usage**

```
# binary: b1star(k, attr=NULL, levels=NULL)
```

**Arguments**

k	a vector of distinct integers
attr, levels	a vertex attribute specification; if attr is specified, then the count is over the instances where all nodes involved have the same value of the attribute. levels specified which values of attr are included in the count. (See Specifying Vertex attributes and Levels ( <a href="#">?nodal_attributes</a> ) for details.)

**Note**

b1star(1) is equal to b2star(1) and to edges .

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b1starmix-ergmTerm	<i>Mixing matrix for k-stars centered on the first mode of a bipartite network</i>
--------------------	--

---

**Description**

This term counts all  $k$ -stars in which the b2 nodes (called events in some contexts) are homophilous in the sense that they all share the same value of attr . However, the b1 node (in some contexts, the actor) at the center of the  $k$ -star does NOT have to have the same value as the b2 nodes; indeed, the values taken by the b1 nodes may be completely distinct from those of the b2 nodes, which allows for the use of this term in cases where there are two separate nodal attributes, one for the b1 nodes and another for the b2 nodes (in this case, however, these two attributes should be combined to form a single nodal attribute, attr). A different statistic is created for each value of attr seen in a b1 node, even if no  $k$ -stars are observed with this value.

**Usage**

```
# binary: b1starmix(k, attr, base=NULL, diff=TRUE)
```

**Arguments**

k	only a single value of $k$ is allowed
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels ( <a href="#">?nodal_attributes</a> ) for details.)
base	deprecated
diff	whether a different statistic is created for each value seen in a b2 node. When diff=TRUE, the default, a different statistic is created for each value and thus the behavior of this term is reminiscent of the nodemix term, from which it takes its name; when diff=FALSE , all homophilous $k$ -stars are counted together, though these $k$ -stars are still categorized according to the value of the central b1 node.

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and levels are passed, levels overrides base. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b1twestar-ergmTerm	<i>Two-star census for central nodes centered on the first mode of a bipartite network</i>
--------------------	--

---

**Description**

This term takes two nodal attributes. Assuming that there are  $n_1$  values of b1attr among the b1 nodes and  $n_2$  values of b2attr among the b2 nodes, then the total number of distinct categories of two stars according to these two attributes is  $n_1(n_2)(n_2 + 1)/2$ . By default, this model term creates a distinct statistic counting each of these categories.

**Usage**

```
# binary: b1twestar(b1attr, b2attr, base=NULL, b1levels=NULL, b2levels=NULL, levels2=NULL)
```

**Arguments**

b1attr	b1 nodes (actors in some contexts) (see Specifying Vertex attributes and Levels (?nodal_attributes) for details)
b2attr	b2 nodes (events in some contexts). If b2attr is not passed, it is assumed to be the same as b1attr .
b1levels, b2levels, base, levels2	used to leave some of the categories out (see Specifying Vertex attributes and Levels (?nodal_attributes) for details)

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and levels are passed, levels overrides base. See [nodal\\_attributes](#).

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and levels2 are passed, levels2 overrides base. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b2concurrent-ergmTerm *Concurrent node count for the second mode in a bipartite network*

---

### Description

This term adds one network statistic to the model, equal to the number of nodes in the second mode of the network with degree 2 or higher. The second mode of a bipartite network object is sometimes known as the "event" mode. Without the optional argument, this statistic is equivalent to `b2mindegree(2)`.

### Usage

```
# binary: b2concurrent(by=NULL)
```

### Arguments

`by` This optional argument specifies a vertex attribute (see [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details); it functions just like the `by` argument of the `b2degree` term.

### Note

This term can only be used with undirected bipartite networks.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, frequently-used, undirected, binary

---

b2cov-ergmTerm *Main effect of a covariate for the second mode in a bipartite network*

---

### Description

This term adds a single network statistic for each quantitative attribute or matrix column to the model equaling the total value of `attr(j)` for all edges  $(i, j)$  in the network. This term may only be used with bipartite networks. For categorical attributes, see `b2factor`.

### Usage

```
# binary: b2cov(attr)

# valued: b2cov(attr, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, dyad-independent, frequently-used, quantitative nodal attribute, undirected, binary, valued

---

b2covrange-ergmTerm     *Range of covariate values for neighbors of a mode-2 node*

---

**Description**

This term adds a single network statistic equalling the sum over the nodes of the range over of its neighbors' values.

**Usage**

```
# binary: nodecovrange(attr)
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
------	---

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). "Modeling Partitions of Individuals." *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:[10.1177/00811750221145166](https://doi.org/10.1177/00811750221145166).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, quantitative nodal attribute, binary

---

b2degrange-ergmTerm *Degree range for the second mode in a bipartite network*

---

**Description**

This term adds one network statistic to the model for each element of `from` (or `to`); the  $i$ th such statistic equals the number of nodes of the second mode ("events") in the network of degree greater than or equal to `from[i]` but strictly less than `to[i]`, i.e. with edge count in semiopen interval `[from, to)`.

This term can only be used with bipartite networks; for directed networks see `idegrange` and `odegrange`. For undirected networks, see `degrange`, and see `b1degrange` for degrees of the first mode ("actors").

**Usage**

```
# binary: b2degrange(from, to=+Inf, by=NULL, homophily=FALSE, levels=NULL)
```

**Arguments**

`from, to` vectors of distinct integers. If one of the vectors have length 1, it is recycled to the length of the other. Otherwise, it must have the same length.

`by, levels, homophily`

the optional argument `by` specifies a vertex attribute (see `Specifying Vertex attributes` and `Levels (?nodal_attributes)` for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

b2degree-ergmTerm	<i>Degree for the second mode in a bipartite network</i>
-------------------	--

---

### Description

This term adds one network statistic to the model for each element in `d`; the  $i$ th such statistic equals the number of nodes of degree `d[i]` in the second mode of a bipartite network, i.e. with exactly `d[i]` edges. The second mode of a bipartite network object is sometimes known as the "event" mode.

### Usage

```
# binary: b2degree(d, by=NULL)
```

### Arguments

<code>d</code>	a vector of distinct integers
<code>by</code>	this optional term specifies a vertex attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details). If this is specified then each node's degree is tabulated only with other nodes having the same value of the <code>by</code> attribute.

### Note

This term can only be used with undirected bipartite networks.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, frequently-used, undirected, binary

---

b2degrees-ergmConstraint	<i>Preserve the receiver degree for bipartite networks</i>
--------------------------	--

---

### Description

For bipartite networks, preserve the degree for the second mode of each vertex of the given network, while allowing the degree for the first mode to vary.

### Usage

```
# b2degrees
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** bipartite

---

b2dsp-ergmTerm

*Dyadwise shared partners for dyads in the second bipartition*


---

**Description**

This term adds one network statistic to the model for each element in  $d$ ; the  $i$ th such statistic equals the number of dyads in the second bipartition with exactly  $d[i]$  shared partners. (Those shared partners, of course, must be members of the first bipartition.) This term can only be used with bipartite networks.

**Usage**

```
# binary: b2dsp(d)
```

**Arguments**

$d$                     a vector of distinct integers

**Note**

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

b2factor-ergmTerm      *Factor attribute effect for the second mode in a bipartite network*

---

### Description

This term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute. Each of these statistics gives the number of times a node with that attribute in the second mode of the network appears in an edge. The second mode of a bipartite network object is sometimes known as the "event" mode.

### Usage

```
# binary: b2factor(attr, base=1, levels=-1)

# valued: b2factor(attr, base=1, levels=-1, form="sum")
```

### Arguments

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>base</code>	deprecated
<code>levels</code>	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

### Note

To include all attribute values is usually not a good idea, because the sum of all such statistics equals the number of edges and hence a linear dependency would arise in any model also including edges. The default, `levels=-1`, is therefore to omit the first (in lexicographic order) attribute level. To include all levels, pass either `levels=TRUE` (i.e., keep all levels) or `levels=NULL` (i.e., do not filter levels).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

This term can only be used with undirected bipartite networks.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, dyad-independent, frequently-used, undirected, binary, valued

---

 b2factordistinct-ergmTerm

*Number of distinct neighbor types for the second mode*


---

### Description

This term adds a single network statistic to the model, counting, for each node, the number of distinct values of the attribute found among its neighbors.

### Usage

```
# binary: b2factordistinct(attr, levels=TRUE)
```

### Arguments

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
levels	this optional argument controls which levels of the attribute attributes and Levels ( <a href="#">?nodal_attributes</a> ) for details.)

### Details

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

### References

Hoffman M, Block P, Snijders TAB (2023). "Modeling Partitions of Individuals." *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:[10.1177/00811750221145166](https://doi.org/10.1177/00811750221145166).

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, binary

---

 b2mindegree-ergmTerm

*Minimum degree for the second mode in a bipartite network*


---

### Description

This term adds one network statistic to the model for each element in  $d$ ; the  $i$ th such statistic equals the number of nodes in the second mode of a bipartite network with at least degree  $d[i]$ . The second mode of a bipartite network object is sometimes known as the "event" mode.

**Usage**

```
# binary: b2mindegree(d)
```

**Arguments**

d                    a vector of distinct integers

**Note**

This term can only be used with undirected bipartite networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

b2nodematch-ergmTerm    *Nodal attribute-based homophily effect for the second mode in a bipartite network*

---

**Description**

This term is introduced by Bomiriya et al. (2023). With the default alpha and beta values, this term will simply be a homophily based two-star statistic. This term adds one statistic to the model unless `diff` is set to `TRUE`, in which case the term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute.

**Usage**

```
# binary: b2nodematch(attr, diff=FALSE, keep=NULL, alpha=1, beta=1, by1attr=NULL,
#                    levels=NULL)
```

**Arguments**

<code>diff</code>	by default, one statistic will be added to the model. If <code>diff</code> is set to <code>TRUE</code> , one statistic will be added for each unique value of the <code>attr</code> attribute
<code>keep</code>	deprecated
<code>alpha, beta</code>	optional discount parameters both of which take values from $[0, 1]$ , only one should be set at one time
<code>by2attr</code>	specifies a second mode categorical attribute. Setting this argument will separate the original statistics based on the values of the set second mode attribute— i.e. for example, if <code>diff</code> is <code>FALSE</code> , then the sum of all the statistics for each level of this second-mode attribute will be equal to the original <code>b1nodematch</code> statistic where <code>by2attr</code> set to <code>NULL</code> .

levels	select a subset of attr values to include. (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

### Details

If an alpha discount parameter is used, each of these statistics gives the sum of the number of common first-mode nodes raised to the power alpha for each pair of second-mode nodes with that attribute. If a beta discount parameter is used, each of these statistics gives half the sum of the number of two-paths with two second-mode nodes with that attribute as the two ends of the two path raised to the power beta for each edge in the network.

### Note

This term can only be used with undirected bipartite networks.

The argument keep is retained for backwards compatibility and may be removed in a future version. When both keep and levels are passed, levels overrides keep. See [nodal\\_attributes](#).

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, dyad-independent, frequently-used, undirected, binary

---

b2sociality-ergmTerm *Degree*

---

### Description

This term adds one network statistic for each node in the second bipartition, equal to the number of ties of that node. For directed networks, see [sender](#) and [receiver](#). For unipartite networks, see [sociality](#).

### Usage

```
# binary: b2sociality(nodes=-1)
# valued: b2sociality(nodes=-1, form="sum")
```

**Arguments**

nodes	By default, nodes=-1 means that the statistic for the first node (in the second bipartition) will be omitted, but this argument may be changed to control which statistics are included. The nodes argument is interpreted using the new UI for level specification (see Specifying Vertex Attributes and Levels (?nodal_attributes) for details), where both the attribute and the sorted unique values are the vector of vertex indices (nb1 + 1):n, where nb1 is the size of the first bipartition and n is the total number of nodes in the network. Thus nodes=120 will include only the statistic for the 120th node in the second bipartition, while nodes=I(120) will include only the statistic for the 120th node in the entire network.
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

This term can only be used with undirected bipartite networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, dyad-independent, undirected, binary, valued

---

b2star-ergmTerm

*k-stars for the second mode in a bipartite network*


---

**Description**

This term adds one network statistic to the model for each element in  $k$ . The  $i$ th such statistic counts the number of distinct  $k[i]$ -stars whose center node is in the second mode of the network. The second mode of a bipartite network object is sometimes known as the "event" mode. A  $k$ -star is defined to be a center node  $N$  and a set of  $k$  different nodes  $\{O_1, \dots, O_k\}$  such that the ties  $\{N, O_i\}$  exist for  $i = 1, \dots, k$ . This term can only be used for undirected bipartite networks.

**Usage**

```
# binary: b2star(k, attr=NULL, levels=NULL)
```

**Arguments**

k	a vector of distinct integers
attr, levels	a vertex attribute specification; if attr is specified, then the count is over the instances where all nodes involved have the same value of the attribute. levels specified which values of attr are included in the count. (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

**Note**

b2star(1) is equal to b1star(1) and to edges .

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b2starmix-ergmTerm	<i>Mixing matrix for <math>k</math>-stars centered on the second mode of a bipartite network</i>
--------------------	--

---

**Description**

This term is exactly the same as b1starmix except that the roles of b1 and b2 are reversed.

**Usage**

```
# binary: b2starmix(k, attr, base=NULL, diff=TRUE)
```

**Arguments**

k	only a single value of $k$ is allowed
attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
base	deprecated
diff	whether a different statistic is created for each value seen in a b1 node. When <code>diff=TRUE</code> , the default, a different statistic is created for each value and thus the behavior of this term is reminiscent of the <code>nodemix</code> term, from which it takes its name; when <code>diff=FALSE</code> , all homophilous $k$ -stars are counted together, though these $k$ -stars are still categorized according to the value of the central b1 node.

**Note**

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

b2tostar-ergmTerm	<i>Two-star census for central nodes centered on the second mode of a bipartite network</i>
-------------------	---

---

### Description

This term is exactly the same as `b1tostar` except that the roles of `b1` and `b2` are reversed.

### Usage

```
# binary: b2tostar(b1attr, b2attr, base=NULL, b1levels=NULL, b2levels=NULL, levels2=NULL)
```

### Arguments

<code>b1attr</code>	<code>b1</code> nodes (actors in some contexts) (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details)
<code>b2attr</code>	<code>b2</code> nodes (events in some contexts). If <code>b1attr</code> is not passed, it is assumed to be the same as <code>b2attr</code> .
<code>b1levels</code> , <code>b2levels</code> , <code>base</code> , <code>levels2</code>	used to leave some of the categories out (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details)

### Note

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels2` are passed, `levels2` overrides `base`. See [nodal\\_attributes](#).

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, categorical nodal attribute, undirected, binary

---

balance-ergmTerm	<i>Balanced triads</i>
------------------	------------------------

---

### Description

This term adds one network statistic to the model equal to the number of triads in the network that are balanced. The balanced triads are those of type 102 or 300 in the categorization of Davis and Leinhardt (1972). For details on the 16 possible triad types, see `?triad.classify` in the `{sna}` package. For an undirected network, the balanced triads are those with an odd number of ties (i.e., 1 and 3).

**Usage**

```
# binary: balance
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, undirected, binary

---

bd-ergmConstraint	<i>Constrain maximum and minimum vertex degree</i>
-------------------	--

---

**Description**

Condition on the number of inedges or outedges possessed by a node. See [Placing Bounds on Degrees](#) section for more information. ([?ergmConstraint](#))

**Usage**

```
# bd(attribs, maxout, maxin, minout, minin)
```

**Arguments**

attribs	a matrix of logicals with dimension (n_nodes, attrcount) for the attributes on which we are conditioning, where attrcount is the number of distinct attributes values to condition on.
maxout, maxin, minout, minin	matrices of alter attributes with the same dimension as attribs when used in conjunction with attribs. Otherwise, vectors of integers specifying the relevant limits. If the vector is of length 1, the limit is applied to all nodes. If an individual entry is NA, then there is no restriction of that kind is applied. For undirected networks (bipartite and not) use minout and maxout.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, undirected

---

 Bernoulli-ergmReference

*Bernoulli reference*


---

### Description

Specifies each dyad's baseline distribution to be Bernoulli with probability of the tie being 0.5 . This is the only reference measure used in binary mode.

### Usage

```
# Bernoulli
```

### See Also

[ergmReference](#) for index of reference distributions currently visible to the package.

**Keywords:** binary, discrete, finite, nonnegative

---

 blockdiag-ergmConstraint

*Block-diagonal structure constraint*


---

### Description

Force a block-diagonal structure (and its bipartite analogue) on the network. Only dyads  $(i, j)$  for which `attr(i)==attr(j)` can have edges.

### Usage

```
# blockdiag(attr, noncontig = "merge")
```

### Arguments

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>noncontig</code>	character: what to do if the blocks are not contiguous? "merge" A placeholder option, to treat them as the same block. It may be implemented in the future, and an explicit "stop" option added later. "split" Treat them as separate blocks.

**Details**

For bipartite graphs, blocks must be have the same ordering in both partitions. (They do not, however, require that all blocks be represented in both partitions, but those that overlap must have the same order.)

If multiple block-diagonal constraints are given, or if `attr` is a vector with multiple attribute names, blocks will be constructed on all attributes matching.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

`blocks=ergmConstraint` *Constrain blocks of dyads defined by mixing type on a vertex attribute.*

---

**Description**

Any dyad whose toggle would produce a nonzero change statistic for a `nodemix` term with the same arguments will be fixed. Note that the `levels2` argument has a different default value for `blocks` than it does for `nodemix`.

**Usage**

```
# blocks(attr=NULL, levels=NULL, levels2=FALSE, b1levels=NULL, b2levels=NULL)
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>b1levels</code> , <code>b2levels</code> , <code>levels</code> , <code>level2</code>	control what mixing types are fixed. <code>levels2</code> applies to all networks; <code>levels</code> applies to unipartite networks; <code>b1levels</code> and <code>b2levels</code> apply to bipartite networks (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details)

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

cdf-ergmTerm	<i>Empirical cumulative distribution function (unnormalized) of the network's dyad values</i>
--------------	---

---

### Description

For every value  $x$  in `seq(min, max, by)`, compute the number of dyads whose value is less than or equal than  $x$ . If not given, the range is autodetected based on the values in the LHS network, subject to adjustment via `margin` and `nmax`.

### Usage

```
# valued: cdf(min = NULL, max = NULL, by = NULL, margin = 0.1, nmax = 100)
```

### Arguments

<code>min, max, by</code>	range and step size for values at which to compute the CDF
<code>margin, nmax</code>	autodetection of the range and step size; see Details.

### Details

If `min`, `max`, and/or `by` is missing, it is automatically computed based on the LHS network's nonzero edge values, specifically their range and resolution (smallest observed difference between distinct values). Minimum and maximum are taken from the minimal and the maximal edge values, and then expanded by `margin` multiplied by their range, and rounded up to the nearest multiple of the resolution. The step is set to the smallest multiple of the resolution such that the total number of statistics is no more than `nmax`.

### Note

This term is intended to be used in a `gof()`'s GOF formula, so its coefficient names are specially formatted to be interpreted by `gof()` rather than for readability.

### See Also

[atmost\(\)](#)

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

ChangeStats-ergmConstraint

*Specified statistics must remain constant*

---

## Description

This is an constraint operator that takes a [ergmTerm](#) formula, and prevents any changes to the network that modify its value. Unlike [Dyads\(fix = ...\)](#), the terms can be dyad-dependent and are calculated at the same time as the proposal rather than used to select proposable-dyads in the first place.

## Usage

```
# ChangeStats(fix, check_dind = TRUE)
```

## Arguments

`fix` an [ergmTerm](#) formula.  
`check_dind` logical; if `fix` turns out to be dyad-independent, fall back to [Dyads\(fix\)](#).

## Dyadic dependence

If the constraint is dyad-independent, [Dyads\(fix\)](#) will usually be faster (at least for estimation) and will make MPLE far more accurate, so if `ChangeStats` detects a dyad-independent constraint, it will fall back to `Dyads`. This can be overridden by setting `check_dind = FALSE`.

## Sampleability is not guaranteed

It is perfectly possible for this constraint to make sampling impossible. For example, `ChangeStats(~edges)` will prevent any proposals that change the number of edges in the network, but **ergm** has no way of knowing that two toggles (edge and non-edge) are now required, so it will keep trying making proposals and failing.

More insidiously, it is in principle possible for the constraint to split the sample space into two parts such that it is not possible to go between them without passing through a state that breaks the constraint.

Thus, it is recommended to use this constraint to, e.g., prevent certain motifs from forming.

## See Also

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, operator, undirected

---

check.ErgmTerm	<i>Ensures an Ergm Term and its Arguments Meet Appropriate Conditions</i>
----------------	---

---

### Description

Helper functions for implementing `ergm()` terms, to check whether the term can be used with the specified network. For information on ergm terms, see `ergmTerm`. `ergm.checkargs`, `ergm.checkbipartite`, and `ergm.checkdirected` are helper functions for an old API and are deprecated. Use `check.ErgmTerm`.

### Usage

```
check.ErgmTerm(
  nw,
  arglist,
  directed = NULL,
  bipartite = NULL,
  nonnegative = FALSE,
  varnames = NULL,
  vartypes = NULL,
  defaultvalues = list(),
  required = NULL,
  dep.inform = rep(FALSE, length(required)),
  dep.warn = rep(FALSE, length(required)),
  argexpr = NULL
)
```

### Arguments

<code>nw</code>	the network that term X is being checked against
<code>arglist</code>	the list of arguments for term X
<code>directed</code>	logical, whether term X requires a directed network; default=NULL
<code>bipartite</code>	whether term X requires a bipartite network (T or F); default=NULL
<code>nonnegative</code>	whether term X requires a network with only nonnegative weights; default=FALSE
<code>varnames</code>	the vector of names of the possible arguments for term X; default=NULL
<code>vartypes</code>	the vector of types of the possible arguments for term X, separated by commas; an empty string ("") or NA disables the check for that argument, and also see Details; default=NULL
<code>defaultvalues</code>	the list of default values for the possible arguments of term X; default=list()
<code>required</code>	the logical vector of whether each possible argument is required; default=NULL
<code>dep.inform, dep.warn</code>	a list of length equal to the number of arguments the term can take; if the corresponding element of the list is not FALSE, a <code>message()</code> or a <code>warning()</code> respectively will be issued if the user tries to pass it; if the element is a character string, it will be used as a suggestion for replacement.
<code>argexpr</code>	optional call typically obtained by calling <code>substitute(arglist)</code> .

## Details

The `check.ErgmTerm` function ensures for the `InitErgmTerm.X` function that the term `X`:

- is applicable given the 'directed' and 'bipartite' attributes of the given network
- is not applied to a directed bipartite network
- has an appropriate number of arguments
- has correct argument types if arguments were provided
- has default values assigned if defaults are available

by halting execution if any of the first 3 criteria are not met.

As a convenience, if an argument is optional *and* its default is NULL, then NULL is assumed to be an acceptable argument type as well.

## Value

A list of the values for each possible argument of term `X`; user provided values are used when given, default values otherwise. The list also has an `attr(,"missing")` attribute containing a named logical vector indicating whether a particular argument had been set to its default. If `argexpr=` argument is provided, `attr(,"exprs")` attribute is also returned, containing expressions.

---

cohab	<i>Target statistics and model fit to a hypothetical 50,000-node network population with 50,000 nodes based on egocent</i>
-------	--

---

## Description

This dataset consists of three objects, each based on data from King County, Washington, USA (where Seattle is located) derived from the National Survey of Family Growth (NSFG) (<https://www.cdc.gov/nchs/nsfg/index.htm>). The full dataset cannot be released publicly, so some aspects of these objects are simulated based on the real data. These objects may be used to illustrate that network modeling may be performed using data that are collected on egos only, i.e., without directly observing information about alters in a network except for information reported from egos. The hypothetical population reepresented by this dataset consists of only a subset of individuals, as categorized by their age, race / ethnicity / immigration status, and gender and sexual identity.

## Usage

```
data(cohab)
```

## Details

The three objects are

**cohab\_MixMat** Mixing matrix on 'race'. Based on ego reports of the race / ethnicity / immigration status of their cohabiting partners, this matrix gives counts of ego-alter ties by the race of each individual for a hypothetical population. These counts are based on the NSFG mixing matrix. Only five categories of the 'race' variable are included here: Black, Black immigrant, Hispanic, Hispanic immigrant, and White.

**cohab\_PopWts** Data frame of demographic characteristics together with relative counts (weights) in a hypothetical population. Individuals are classified according to five variables: age in years, race (same five categories of race / ethnicity / immigration status as above), sex (Male or Female), sexual identity (Female, Male who has sex with Females, or Male who has sex with Males or Females), and number of model-predicted persistent partnerships with non-cohabiting partners (0 or 1, where 1 means any nonzero value; the number is capped at 3), and number of partners (0 or 1).

**cohab\_TargetStats** Vector of target (expected) statistics for a 15-term ERGM applied to a network of 50,000 nodes in which a tie represents a cohabitation relationship between two nodes. It is assumed for the purposes of these statistics that only male-female cohabitation relationships are allowed and that no individual may have such a relationship with more than one person. That is, each node must have degree zero or one. The ergm formula is: `~ edges + nodefactor("sex.ident", levels = 3) + nodecov("age") + nodecov("agesq") + nodefactor("race", levels = -5) + nodefactor("othr.net.deg", levels = -1) + nodematch("race", diff = TRUE) + absdiff("sqrt.age.adj")`

## References

Krivitsky PN, Hunter DR, Morris M, Klumb C (2023). "ergm 4: New Features for Analyzing Exponential-Family Random Graph Models." *Journal of Statistical Software*, **105**(6), 1–44. doi:10.18637/jss.v105.i06.

National Center for Health Statistics (2020). "2006-2015 National Survey of Family Growth Public-Use Data and Documentation." Hyattsville, MD: CDC National Center for Health Statistics. <https://www.cdc.gov/nchs/nsfg/index.htm>.

## See Also

ergm

---

coincidence-ergmTerm *Coincident node count for the second mode in a bipartite (aka two-mode) network*

---

## Description

By default this term adds one network statistic to the model for each pair of nodes of mode two. It is equal to the number of (first mode) mutual partners of that pair. The first mode of a bipartite network object is sometimes known as the "actor" mode and the seconds as the "event" mode. So this is the number of actors going to both events in the pair. This term can only be used with undirected bipartite networks.

## Usage

```
# binary: coincidence(levels=NULL,active=0)
```

**Arguments**

levels	specifies which pairs of nodes in mode two to include. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
active	selects pairs for which the observed count is at least active . Ignored if levels is specified. (Thus, indices passed as levels should correspond to indices when levels = NULL and active = 0.)

**Note**

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

concurrent-ergmTerm     *Concurrent node count*

---

**Description**

This term adds one network statistic to the model, equal to the number of nodes in the network with degree 2 or higher. This term can only be used with undirected networks.

**Usage**

```
# binary: concurrent(by=NULL, levels=NULL)
```

**Arguments**

by	this optional argument specifies a vertex attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) It functions just like the by argument of the degree term.
----	---

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, undirected, binary

---

 concurrentties-ergmTerm

*Concurrent tie count*


---

### Description

This term adds one network statistic to the model, equal to the number of ties incident on each actor beyond the first. This term can only be used with undirected networks.

### Usage

```
# binary: concurrentties(by=NULL, levels=NULL)
```

### Arguments

by	a vertex attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.); it functions just like the by argument of the degree term
levels	TODO (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, undirected, binary

---

 control.ergm

*Auxiliary function for fine-tuning ERGM fitting.*


---

### Description

This function is only used within a call to the [ergm\(\)](#) function. See the Usage section in [ergm\(\)](#) for details. Also see the Details section about some of the interactions between its arguments.

`control.ergm3()` is a wrapper that sets the defaults to use algorithms and settings circa **ergm** 3.11 (the last release before 4.0).

### Usage

```
control.ergm(
  drop = TRUE,
  init = NULL,
  init.method = NULL,
  main.method = c("MCMLE", "Stochastic-Approximation"),
  force.main = FALSE,
  main.hessian = TRUE,
```

```

checkpoint = NULL,
resume = NULL,
MPLE.samplesize = .Machine$integer.max,
init.MPLE.samplesize = function(d, e) max(sqrt(d), e, 40) * 8,
MPLE.type = c("glm", "penalized", "logitreg"),
MPLE.maxit = 10000,
MPLE.nonvar = c("warning", "message", "error"),
MPLE.nonident = c("warning", "message", "error"),
MPLE.nonident.tol = 1e-10,
MPLE.covariance.samplesize = 500,
MPLE.covariance.method = "invHess",
MPLE.covariance.sim.burnin = 1024,
MPLE.covariance.sim.interval = 1024,
MPLE.check = TRUE,
MPLE.constraints.ignore = FALSE,
MCMC.prop = trim_env(~sparse + .triadic),
MCMC.prop.weights = "default",
MCMC.prop.args = list(),
MCMC.interval = NULL,
MCMC.burnin = EVL(MCMC.interval * 16),
MCMC.samplesize = NULL,
MCMC.effectiveSize = NULL,
MCMC.effectiveSize.damp = 10,
MCMC.effectiveSize.maxruns = 16,
MCMC.effectiveSize.burnin.pval = 0.2,
MCMC.effectiveSize.burnin.min = 0.05,
MCMC.effectiveSize.burnin.max = 0.5,
MCMC.effectiveSize.burnin.nmin = 16,
MCMC.effectiveSize.burnin.nmax = 128,
MCMC.effectiveSize.burnin.PC = FALSE,
MCMC.effectiveSize.burnin.scl = 32,
MCMC.effectiveSize.order.max = NULL,
MCMC.return.stats = 2^12,
MCMC.runtime.traceplot = FALSE,
MCMC.maxedges = Inf,
MCMC.addto.se = TRUE,
MCMC.packagenames = c(),
SAN.maxit = 4,
SAN.nsteps.times = 8,
SAN = control.san(term.options = term.options, SAN.maxit = SAN.maxit, SAN.prop =
  MCMC.prop, SAN.prop.weights = MCMC.prop.weights, SAN.prop.args = MCMC.prop.args,
  SAN.nsteps = EVL(MCMC.burnin, 16384) * SAN.nsteps.times, SAN.samplesize =
  EVL(MCMC.samplesize, 1024), SAN.packagenames = MCMC.packagenames, parallel =
  parallel, parallel.type = parallel.type, parallel.version.check =
  parallel.version.check),
MCMLE.termination = c("confidence", "Hummel", "Hotelling", "precision", "none"),
MCMLE.maxit = 60,
MCMLE.conv.min.pval = 0.5,

```

```

MCMLE.confidence = 0.99,
MCMLE.confidence.boost = 2,
MCMLE.confidence.boost.threshold = 1,
MCMLE.confidence.boost.lag = 4,
MCMLE.NR.maxit = 100,
MCMLE.NR.reltol = sqrt(.Machine$double.eps),
obs.MCMC.mul = 1/4,
obs.MCMC.samplesize.mul = sqrt(obs.MCMC.mul),
obs.MCMC.samplesize = EVL(round(MCMC.samplesize * obs.MCMC.samplesize.mul)),
obs.MCMC.effectiveSize = NVL3(MCMC.effectiveSize, . * obs.MCMC.mul),
obs.MCMC.interval.mul = sqrt(obs.MCMC.mul),
obs.MCMC.interval = EVL(round(MCMC.interval * obs.MCMC.interval.mul)),
obs.MCMC.burnin.mul = sqrt(obs.MCMC.mul),
obs.MCMC.burnin = EVL(round(MCMC.burnin * obs.MCMC.burnin.mul)),
obs.MCMC.prop = MCMC.prop,
obs.MCMC.prop.weights = MCMC.prop.weights,
obs.MCMC.prop.args = MCMC.prop.args,
obs.MCMC.impute.min_informative = function(nw) network.size(nw)/4,
obs.MCMC.impute.default_density = function(nw) 2/network.size(nw),
MCMLE.min.depfac = 2,
MCMLE.sampszie.boost.pow = 0.5,
MCMLE.MCMC.precision = if (startsWith("confidence", MCMLE.termination[1])) 0.1 else
  0.005,
MCMLE.MCMC.max.ESS.frac = 0.1,
MCMLE.metric = c("lognormal", "logtaylor", "Median.Likelihood", "EF.Likelihood",
  "naive"),
MCMLE.method = c("BFGS", "Nelder-Mead"),
MCMLE.dampening = FALSE,
MCMLE.dampening.min.ess = 20,
MCMLE.dampening.level = 0.1,
MCMLE.steplength.margin = 0.05,
MCMLE.steplength = NVL2(MCMLE.steplength.margin, 1, 0.5),
MCMLE.steplength.parallel = c("observational", "never"),
MCMLE.sequential = TRUE,
MCMLE.density.guard.min = 10000,
MCMLE.density.guard = exp(3),
MCMLE.effectiveSize = 64,
obs.MCMLE.effectiveSize = NULL,
MCMLE.interval = 1024,
MCMLE.burnin = MCMLE.interval * 16,
MCMLE.samplesize.per_theta = 32,
MCMLE.samplesize.min = 256,
MCMLE.samplesize = NULL,
obs.MCMLE.samplesize.per_theta = round(MCMLE.samplesize.per_theta *
  obs.MCMC.samplesize.mul),
obs.MCMLE.samplesize.min = 256,
obs.MCMLE.samplesize = NULL,
obs.MCMLE.interval = round(MCMLE.interval * obs.MCMC.interval.mul),

```

```

obs.MCMLE.burnin = round(MCMLE.burnin * obs.MCMC.burnin.mul),
MCMLE.steplength.solver = c("glpk", "lpsolve"),
MCMLE.last.boost = 4,
MCMLE.steplength.esteq = TRUE,
MCMLE.steplength.miss.sample = function(x1) c(max(ncol(rbind(x1))) * 2, 30), 10),
MCMLE.steplength.min = 1e-04,
MCMLE.effectiveSize.interval_drop = 2,
MCMLE.save_intermediates = NULL,
MCMLE.nonvar = c("message", "warning", "error"),
MCMLE.nonident = c("warning", "message", "error"),
MCMLE.nonident.tol = 1e-10,
SA.phase1_n = function(q, ...) max(200, 7 + 3 * q),
SA.initial_gain = 0.1,
SA.nsubphases = 4,
SA.min_iterations = function(q, ...) (7 + q),
SA.max_iterations = function(q, ...) (207 + q),
SA.phase3_n = 1000,
SA.interval = 1024,
SA.burnin = SA.interval * 16,
SA.samplesize = 1024,
CD.samplesize.per_theta = 128,
obs.CD.samplesize.per_theta = 128,
CD.nsteps = 8,
CD.multiplicity = 1,
CD.nsteps.obs = 128,
CD.multiplicity.obs = 1,
CD.maxit = 60,
CD.conv.min.pval = 0.5,
CD.NR.maxit = 100,
CD.NR.reltol = sqrt(.Machine$double.eps),
CD.metric = c("naive", "lognormal", "logtaylor", "Median.Likelihood", "EF.Likelihood"),
CD.method = c("BFGS", "Nelder-Mead"),
CD.dampening = FALSE,
CD.dampening.min.ess = 20,
CD.dampening.level = 0.1,
CD.steplength.margin = 0.5,
CD.steplength = 1,
CD.adaptive.epsilon = 0.01,
CD.steplength.esteq = TRUE,
CD.steplength.miss.sample = function(x1) ceiling(sqrt(ncol(rbind(x1))))),
CD.steplength.min = 1e-04,
CD.steplength.parallel = c("observational", "always", "never"),
CD.steplength.solver = c("glpk", "lpsolve"),
loglik = control.logLik.ergm(),
term.options = NULL,
seed = NULL,
parallel = 0,
parallel.type = NULL,

```

```

parallel.version.check = TRUE,
parallel.inherit.MT = FALSE,
...
)

control.ergm3(
  drop = TRUE,
  init = NULL,
  init.method = NULL,
  main.method = c("MCMLE", "Stochastic-Approximation"),
  force.main = FALSE,
  main.hessian = TRUE,
  checkpoint = NULL,
  resume = NULL,
  MPLE.samplesize = .Machine$integer.max,
  init.MPLE.samplesize = function(d, e) max(sqrt(d), e, 40) * 8,
  MPLE.type = c("glm", "penalized", "logitreg"),
  MPLE.maxit = 10000,
  MPLE.nonvar = c("warning", "message", "error"),
  MPLE.nonident = c("warning", "message", "error"),
  MPLE.nonident.tol = 1e-10,
  MPLE.covariance.samplesize = 500,
  MPLE.covariance.method = "invHess",
  MPLE.covariance.sim.burnin = 1024,
  MPLE.covariance.sim.interval = 1024,
  MPLE.check = TRUE,
  MPLE.constraints.ignore = FALSE,
  MCMC.prop = trim_env(~sparse + .triadic),
  MCMC.prop.weights = "default",
  MCMC.prop.args = list(),
  MCMC.interval = NULL,
  MCMC.burnin = EVL(MCMC.interval * 16),
  MCMC.samplesize = NULL,
  MCMC.effectiveSize = NULL,
  MCMC.effectiveSize.damp = 10,
  MCMC.effectiveSize.maxruns = 16,
  MCMC.effectiveSize.burnin.pval = 0.2,
  MCMC.effectiveSize.burnin.min = 0.05,
  MCMC.effectiveSize.burnin.max = 0.5,
  MCMC.effectiveSize.burnin.nmin = 16,
  MCMC.effectiveSize.burnin.nmax = 128,
  MCMC.effectiveSize.burnin.PC = FALSE,
  MCMC.effectiveSize.burnin.scl = 32,
  MCMC.effectiveSize.order.max = NULL,
  MCMC.return.stats = 2^12,
  MCMC.runtime.traceplot = FALSE,
  MCMC.maxedges = Inf,
  MCMC.addto.se = TRUE,

```

```

MCMC.packagenames = c(),
SAN.maxit = 4,
SAN.nsteps.times = 8,
SAN = control.san(term.options = term.options, SAN.maxit = SAN.maxit, SAN.prop =
  MCMC.prop, SAN.prop.weights = MCMC.prop.weights, SAN.prop.args = MCMC.prop.args,
  SAN.nsteps = EVL(MCMC.burnin, 16384) * SAN.nsteps.times, SAN.samplesize =
  EVL(MCMC.samplesize, 1024), SAN.packagenames = MCMC.packagenames, parallel =
  parallel, parallel.type = parallel.type, parallel.version.check =
  parallel.version.check),
MCMLE.termination = c("Hummel", "confidence", "Hotelling", "precision", "none"),
MCMLE.maxit = 60,
MCMLE.conv.min.pval = 0.5,
MCMLE.confidence = 0.99,
MCMLE.confidence.boost = 2,
MCMLE.confidence.boost.threshold = 1,
MCMLE.confidence.boost.lag = 4,
MCMLE.NR.maxit = 100,
MCMLE.NR.reltol = sqrt(.Machine$double.eps),
obs.MCMC.mul = 1/4,
obs.MCMC.samplesize.mul = sqrt(obs.MCMC.mul),
obs.MCMC.samplesize = EVL(round(MCMC.samplesize * obs.MCMC.samplesize.mul)),
obs.MCMC.effectiveSize = NVL3(MCMC.effectiveSize, . * obs.MCMC.mul),
obs.MCMC.interval.mul = sqrt(obs.MCMC.mul),
obs.MCMC.interval = EVL(round(MCMC.interval * obs.MCMC.interval.mul)),
obs.MCMC.burnin.mul = sqrt(obs.MCMC.mul),
obs.MCMC.burnin = EVL(round(MCMC.burnin * obs.MCMC.burnin.mul)),
obs.MCMC.prop = MCMC.prop,
obs.MCMC.prop.weights = MCMC.prop.weights,
obs.MCMC.prop.args = MCMC.prop.args,
obs.MCMC.impute.min_informative = function(nw) network.size(nw)/4,
obs.MCMC.impute.default_density = function(nw) 2/network.size(nw),
MCMLE.min.depfac = 2,
MCMLE.sampszie.boost.pow = 0.5,
MCMLE.MCMC.precision = if (startsWith("confidence", MCMLE.termination[1])) 0.1 else
  0.005,
MCMLE.MCMC.max.ESS.frac = 0.1,
MCMLE.metric = c("lognormal", "logtaylor", "Median.Likelihood", "EF.Likelihood",
  "naive"),
MCMLE.method = c("BFGS", "Nelder-Mead"),
MCMLE.dampening = FALSE,
MCMLE.dampening.min.ess = 20,
MCMLE.dampening.level = 0.1,
MCMLE.steplength.margin = 0.05,
MCMLE.steplength = NVL2(MCMC.steplength.margin, 1, 0.5),
MCMLE.steplength.parallel = c("observational", "never"),
MCMLE.sequential = TRUE,
MCMLE.density.guard.min = 10000,
MCMLE.density.guard = exp(3),

```

```

MCMLE.effectiveSize = NULL,
obs.MCMLE.effectiveSize = NULL,
MCMLE.interval = 1024,
MCMLE.burnin = MCMLE.interval * 16,
MCMLE.samplesize.per_theta = 32,
MCMLE.samplesize.min = 256,
MCMLE.samplesize = NULL,
obs.MCMLE.samplesize.per_theta = round(MCMLE.samplesize.per_theta *
  obs.MCMC.samplesize.mul),
obs.MCMLE.samplesize.min = 256,
obs.MCMLE.samplesize = NULL,
obs.MCMLE.interval = round(MCMLE.interval * obs.MCMC.interval.mul),
obs.MCMLE.burnin = round(MCMLE.burnin * obs.MCMC.burnin.mul),
MCMLE.steplength.solver = c("glpk", "lpsolve"),
MCMLE.last.boost = 4,
MCMLE.steplength.esteq = TRUE,
MCMLE.steplength.miss.sample = function(x1) c(max(ncol(rbind(x1))) * 2, 30), 10),
MCMLE.steplength.min = 1e-04,
MCMLE.effectiveSize.interval_drop = 2,
MCMLE.save_intermediates = NULL,
MCMLE.nonvar = c("message", "warning", "error"),
MCMLE.nonident = c("warning", "message", "error"),
MCMLE.nonident.tol = 1e-10,
SA.phase1_n = function(q, ...) max(200, 7 + 3 * q),
SA.initial_gain = 0.1,
SA.nsubphases = 4,
SA.min_iterations = function(q, ...) (7 + q),
SA.max_iterations = function(q, ...) (207 + q),
SA.phase3_n = 1000,
SA.interval = 1024,
SA.burnin = SA.interval * 16,
SA.samplesize = 1024,
CD.samplesize.per_theta = 128,
obs.CD.samplesize.per_theta = 128,
CD.nsteps = 8,
CD.multiplicity = 1,
CD.nsteps.obs = 128,
CD.multiplicity.obs = 1,
CD.maxit = 60,
CD.conv.min.pval = 0.5,
CD.NR.maxit = 100,
CD.NR.reltol = sqrt(.Machine$double.eps),
CD.metric = c("naive", "lognormal", "logtaylor", "Median.Likelihood", "EF.Likelihood"),
CD.method = c("BFGS", "Nelder-Mead"),
CD.dampening = FALSE,
CD.dampening.min.ess = 20,
CD.dampening.level = 0.1,
CD.steplength.margin = 0.5,

```

```

CD.steplength = 1,
CD.adaptive.epsilon = 0.01,
CD.steplength.esteq = TRUE,
CD.steplength.miss.sample = function(x1) ceiling(sqrt(ncol(rbind(x1))))),
CD.steplength.min = 1e-04,
CD.steplength.parallel = c("observational", "always", "never"),
CD.steplength.solver = c("glpk", "lpsolve"),
loglik = control.logLik.ergm(),
term.options = NULL,
seed = NULL,
parallel = 0,
parallel.type = NULL,
parallel.version.check = TRUE,
parallel.inherit.MT = FALSE,
...
)

```

## Arguments

- |             |  |
|-------------|--|
| drop        | Logical: If TRUE, terms whose observed statistic values are at the extremes of their possible ranges are dropped from the fit and their corresponding parameter estimates are set to plus or minus infinity, as appropriate. This is done because maximum likelihood estimates cannot exist when the vector of observed statistic lies on the boundary of the convex hull of possible statistic values.  |
| init        | <p>numeric or NA vector equal in length to the number of parameters in the model or NULL (the default); the initial values for the estimation and coefficient offset terms. If NULL is passed, all of the initial values are computed using the method specified by <code>control\$init.method</code>. If a numeric vector is given, the elements of the vector are interpreted as follows:</p> <ul style="list-style-type: none"> <li>• Elements corresponding to terms enclosed in <code>offset()</code> are used as the fixed offset coefficients. Note that offset coefficients alone can be more conveniently specified using <code>ergm()</code> argument <code>offset.coef</code>. If both <code>offset.coef</code> and <code>init</code> arguments are given, values in <code>offset.coef</code> will take precedence.</li> <li>• Elements that do not correspond to offset terms and are not NA are used as starting values in the estimation.</li> <li>• Initial values for the elements that are NA are fit using the method specified by <code>control\$init.method</code>.</li> </ul> <p>If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code>. Passing <code>control.ergm(init=coef(prev.fit))</code> can be used to “resume” an uncovered <code>ergm()</code> run, though <code>checkpoint</code> and <code>‘resume’</code> would be better under most circumstances.</p> |
| init.method | A character vector or NULL. The default method depends on the reference measure used. For the binary (“Bernoulli”) ERGMs, with dyad-independent constraints, it’s maximum pseudo-likelihood estimation (MPLE). Other valid values include “zeros” for a 0 vector of appropriate length and “CD” for contrastive divergence. If passed explicitly, this setting overrides the reference’s limitations.  |

	Valid initial methods for a given reference are set by the <code>InitErgmReference.*</code> function.
<code>main.method</code>	One of "MCMLE" (default) or "Stochastic-Approximation". Chooses the estimation method used to find the MLE. MCMLE attempts to maximize an approximation to the log-likelihood function. Stochastic-Approximation are both stochastic approximation algorithms that try to solve the method of moments equation that yields the MLE in the case of an exponential family model. The direct use of the likelihood function has many theoretical advantages over stochastic approximation, but the choice will depend on the model and data being fit. See (Hunter and Handcock 2006) for details.
<code>force.main</code>	Logical: If TRUE, then force MCMC-based estimation method, even if the exact MLE can be computed via maximum pseudolikelihood estimation.
<code>main.hessian</code>	Logical: If TRUE, then an approximate Hessian matrix is used in the MCMC-based estimation method.
<code>checkpoint</code>	At the start of every iteration, save the state of the optimizer in a way that will allow it to be resumed. The name is passed through <code>sprintf()</code> with iteration number as the second argument. (For example, <code>checkpoint="step_%03d.RData"</code> will save to <code>step_001.RData</code> , <code>step_002.RData</code> , etc.)
<code>resume</code>	If given a file name of an RData file produced by checkpoint, the optimizer will attempt to resume after restoring the state. Control parameters from the saved state will be reused, except for those whose value passed via <code>control.ergm()</code> had change from the saved run. Note that if the network, the model, or some critical settings differ between runs, the results may be undefined.
<code>MPLE.samplesize</code> , <code>init.MPLE.samplesize</code>	<p>These parameters control the maximum number of dyads (potential ties) that will be used by the MPLE to construct the predictor matrix for its logistic regression. In general, the algorithm visits dyads in a systematic sample that, if it does not hit one of these limits, will visit every informative dyad. If a limit is exceeded, case-control approximation to the likelihood, comprising all edges and those non-edges that have been visited by the algorithm before the limit was exceeded will be used.</p> <p><code>MPLE.samplesize</code> limits the number of dyads visited, unless the MPLE is being computed for the purpose of being the initial value for MCMC-based estimation, in which case <code>init.MPLE.samplesize</code> is used instead, All of these can be specified either as numbers or as <code>function(d,e)</code> taking the number of informative dyads and informative edges. Specifying or returning a larger number than the number of informative dyads is safe.</p>
<code>MPLE.type</code>	One of "glm", "penalized", or "logitreg". Chooses method of calculating MPLE. "glm" is the usual formal logistic regression called via <code>glm()</code> , whereas "penalized" uses the bias-reduced method of Firth (1993) as originally implemented by Meinhard Ploner, Daniela Dunkler, Harry Southworth, and Georg Heinze in the "logistf" package. "logitreg" is an "in-house" implementation that is slower and probably less stable but supports nonlinear logistic regression. It is invoked automatically when the model has curved terms.
<code>MPLE.maxit</code>	Maximum number of iterations for "logitreg" implementation of MPLE.

MPLE.nonident, MCMLE.nonident.tol, MCMLE.nonvar	
MPLE.nonident.tol, MCMLE.nonident.tol, MCMLE.nonvar	A rudimentary nonidentifiability/multicollinearity diagnostic. If <code>MPLE.nonident.tol &gt; 0</code> , test the MPLE covariate matrix or the CD statistics matrix has linearly dependent columns via <a href="#">QR decomposition</a> with tolerance <code>MPLE.nonident.tol</code> . This is often (not always) indicative of a non-identifiable (multicollinear) model. If nonidentifiable, depending on <code>MPLE.nonident</code> issue a warning, an error, or a message specifying the potentially redundant statistics. Before the diagnostic is performed, covariates that do not vary (i.e., all-zero columns) are dropped, with their handling controlled by <code>MPLE.nonvar</code> . The corresponding <code>MCMLE.*</code> arguments provide a similar diagnostic for the unconstrained MCMC sample's estimating functions.
MPLE.covariance.method, MCMLE.covariance.method, MCMLE.covariance.samplesize, MCMLE.covariance.sim.burnin, MCMLE.covariance.sim.interval	
MPLE.covariance.method, MCMLE.covariance.method, MCMLE.covariance.samplesize, MCMLE.covariance.sim.burnin, MCMLE.covariance.sim.interval	Controls for estimating the MPLE covariance matrix. <code>MPLE.covariance.method</code> determines the method, with <code>invHess</code> (the default) returning the covariance estimate obtained from the <code>glm()</code> . <code>Godambe</code> estimates the covariance matrix using the Godambe-matrix (Schmid and Hunter 2023). This method is recommended for dyad-dependent models. Alternatively, <code>bootstrap</code> estimates standard deviations using a parametric bootstrapping approach (see Schmid and Desmarais 2017). The other parameters control, respectively, the number of networks to simulate, the MCMC burn-in, and the MCMC interval for Godambe and bootstrap methods.
MPLE.check	If TRUE (the default), perform the MPLE existence check described by Schmid and Hunter (2023).
MPLE.constraints.ignore	If TRUE, MPLE will ignore all dyad-independent constraints except for those due to attributes missingness. This can be used to avert evaluating and storing the <a href="#">rlebdms</a> for very large networks except where absolutely necessary. Note that this can be very dangerous unless you know what you are doing.
MCMC.prop	Specifies the proposal (directly) and/or a series of "hints" about the structure of the model being sampled. The specification is in the form of a one-sided formula with hints separated by + operations. If the LHS exists and is a string, the proposal to be used is selected directly.  A common and default "hint" is <code>~sparse</code> , indicating that the network is sparse and that the sample should put roughly equal weight on selecting a dyad with or without a tie as a candidate for toggling.
MCMC.prop.weights	Specifies the proposal distribution used in the MCMC Metropolis-Hastings algorithm. Possible choices depending on selected reference and constraints arguments of the <code>ergm()</code> function, but often include <code>"TNT"</code> and <code>"random"</code> , and the <code>"default"</code> is to use the one with the highest priority available.
MCMC.prop.args	An alternative, direct way of specifying additional arguments to proposal.
MCMC.interval	Number of proposals between sampled statistics. Increasing interval will reduce the autocorrelation in the sample, and may increase the precision in estimates by reducing MCMC error, at the expense of time. Set the interval higher for larger networks.

MCMC.burnin	Number of proposals before any MCMC sampling is done. It typically is set to a fairly large number.
MCMC.samplesize	Number of network statistics, randomly drawn from a given distribution on the set of all networks, returned by the Metropolis-Hastings algorithm. Increasing sample size may increase the precision in the estimates by reducing MCMC error, at the expense of time. Set it higher for larger networks, or when using parallel functionality.
MCMC.effectiveSize,	MCMC.effectiveSize.damp,
MCMC.effectiveSize.maxruns,	MCMC.effectiveSize.burnin.pval,
MCMC.effectiveSize.burnin.min,	MCMC.effectiveSize.burnin.max,
MCMC.effectiveSize.burnin.nmin,	MCMC.effectiveSize.burnin.nmax,
MCMC.effectiveSize.burnin.PC,	MCMC.effectiveSize.burnin.scl,
MCMC.effectiveSize.order.max	
	<p>Set MCMC.effectiveSize to a non-NULL value to adaptively determine the burn-in and the MCMC length needed to get the specified effective size; 50 is a reasonable value. In the adaptive MCMC mode, MCMC is run forward repeatedly (MCMC.samplesize*MCMC.interval steps, up to MCMC.effectiveSize.maxruns times) until the target effective sample size is reached or exceeded.</p> <p>After each run, the returned statistics are mapped to the estimating function scale, then an exponential decay model is fit to the scaled statistics to find that burn-in which would reduce the difference between the initial values of statistics and their equilibrium values by a factor of MCMC.effectiveSize.burnin.scl of what it initially was, bounded by MCMC.effectiveSize.min and MCMC.effectiveSize.max as proportions of sample size. If the best-fitting decay exceeds MCMC.effectiveSize.max, the exponential model is considered to be unsuitable and MCMC.effectiveSize.min is used.</p> <p>A Geweke diagnostic is then run, after thinning the sample to MCMC.effectiveSize.burnin.nmax. If this Geweke diagnostic produces a <math>p</math>-value higher than MCMC.effectiveSize.burnin.pval, it is accepted.</p> <p>If MCMC.effectiveSize.burnin.PC&gt;0, instead of using the full sample for burn-in estimation, at most this many principal components are used instead.</p> <p>The effective size of the post-burn-in sample is computed via Vats et al. (2019), and compared to the target effective size. If it is not matched, the MCMC run is resumed, with the additional draws needed linearly extrapolated but weighted in favor of the baseline MCMC.samplesize by the weighting factor MCMC.effectiveSize.damp (higher = less damping). Lastly, if after an MCMC run, the number of samples equals or exceeds 2*MCMC.samplesize, the chain will be thinned by 2 until it falls below that, while doubling MCMC.interval. MCMC.effectiveSize.order.max can be used to set the order of the AR model used to estimate the effective sample size and the variance for the Geweke diagnostic.</p> <p>Lastly, if MCMC.effectiveSize is a matrix, say, <math>W</math>, it will be treated as a target precision (inverse-variance) matrix. If <math>V</math> is the sample covariance matrix, the target effective size <math>n_{\text{eff}}</math> will be set such that <math>V/n_{\text{eff}}</math> is close to <math>W</math> in magnitude, specifically that <math>\text{tr}((V/n_{\text{eff}})W)/p \approx 1</math>.</p>
MCMC.return.stats	Numeric: If positive, include an <code>mcmc.list</code> (two, if observational process was involved) of MCMC network statistics from the last iteration of network of the

estimation. They will be thinned to have length of at most `MCMC.return.stats`. They are used for MCMC diagnostics.

`MCMC.runtime.traceplot`

Logical: If TRUE, plot trace plots of the MCMC sample after every MCMC MLE iteration. Since curved models tend to produce large numbers of mostly constant statistics, they are plotted on the estimating function scale, i.e.,  $\eta'(\theta)^\top \{g(Y^s) - g(y)\}$ .

`MCMC.maxedges`

The maximum number of edges that may occur during the MCMC sampling. If this number is exceeded at any time, sampling is stopped immediately.

`MCMC.addto.se`

Whether to add the standard errors induced by the MCMC algorithm to the estimates' standard errors.

`MCMC.packagenames`

Names of packages in which to look for change statistic functions in addition to those autodetected. This argument should not be needed outside of very strange setups.

`SAN.maxit`

When `target.stats` argument is passed to `ergm()`, the maximum number of attempts to use `san()` to obtain a network with statistics close to those specified.

`SAN.nsteps.times`

Multiplier for `SAN.nsteps` relative to `MCMC.burnin`. This lets one control the amount of SAN burn-in (arguably, the most important of SAN parameters) without overriding the other SAN defaults.

`SAN`

Control arguments to `san()`. See `control.san()` for details.

`MCMLE.termination`

The criterion used for terminating MCML estimation:

- "Hummel" Terminate when the Hummel step length is 1 for two consecutive iterations. For the last iteration, the sample size is boosted by a factor of `MCMLE.last.boost`. See Hummel et al. (2012).

Note that this criterion is incompatible with `MCMLE.steplength`  $\neq$  1 or `MCMLE.steplength.margin` = NULL.

- "Hotelling" After every MCMC sample, an autocorrelation-adjusted Hotelling's  $T^2$  test for equality of MCMC-simulated network statistics to observed is conducted, and if its P-value exceeds `MCMLE.conv.min.pval`, the estimation is considered to have converged and finishes. This was the default option in `ergm` version 3.1.
- "precision" Terminate when the estimated loss in estimating precision due to using MCMC standard errors is below the precision bound specified by `MCMLE.MCMC.precision`, and the Hummel step length is 1 for two consecutive iterations. See `MCMLE.MCMC.precision` for details. This feature is in experimental status until we verify the coverage of the standard errors.

Note that this criterion is incompatible with `MCMLE.steplength`  $\neq$  1 or `MCMLE.steplength.margin` = NULL.

- "confidence": Performs an equivalence test to prove with level of confidence `MCMLE.confidence` that the true value of the deviation of the simulated mean value parameter from the observed is within an ellipsoid defined by the inverse-variance-covariance of the sufficient statistics multiplied by

a scaling factor `control$MCMLE.MCMC.precision` (which has a different default).

- "none" Stop after `MCMLE.maxit` iterations.

`MCMLE.maxit` Maximum number of times the parameter for the MCMC should be updated by maximizing the MCMC likelihood. At each step the parameter is changed to the values that maximizes the MCMC likelihood based on the current sample.

`MCMLE.conv.min.pval`  
The P-value used in the Hotelling test for early termination.

`MCMLE.confidence`  
The confidence level for declaring convergence for "confidence" methods.

`MCMLE.confidence.boost`  
The maximum increase factor in sample size (or target effective size, if enabled) when the "confidence" termination criterion is either not approaching the tolerance region or is unable to prove convergence.

`MCMLE.confidence.boost.threshold`, `MCMLE.confidence.boost.lag`  
Sample size or target effective size will be increased if the distance from the tolerance region fails to decrease more than `MCMLE.confidence.boost.threshold` in this many successive iterations.

`MCMLE.NR.maxit`, `MCMLE.NR.reltol`  
The method, maximum number of iterations and relative tolerance to use within the optim routine in the MLE optimization. Note that by default, ergm uses trust, and falls back to optim only when trust fails.

`obs.MCMC.prop`, `obs.MCMC.prop.weights`, `obs.MCMC.prop.args`,  
`obs.MCMLE.effectiveSize`, `obs.MCMC.samplesize`, `obs.MCMC.burnin`,  
`obs.MCMC.interval`, `obs.MCMC.mul`, `obs.MCMC.samplesize.mul`,  
`obs.MCMC.burnin.mul`, `obs.MCMC.interval.mul`, `obs.MCMC.effectiveSize`,  
`obs.MCMLE.burnin`, `obs.MCMLE.interval`, `obs.MCMLE.samplesize`,  
`obs.MCMLE.samplesize.per_theta`, `obs.MCMLE.samplesize.min`

Corresponding MCMC parameters and settings used for the constrained sample when unobserved data are present in the estimation routine. By default, they are controlled by the `*.mul` parameters, as fractions of the corresponding settings for the unconstrained (standard) MCMC.

These can, in turn, be controlled by `obs.MCMC.mul`, which can be used to set the overall multiplier for the number of MCMC steps in the constrained sample; one half of its effect applies to the burn-in and interval and the other half to the total sample size. For example, for `obs.MCMC.mul=1/4` (the default), `obs.MCMC.samplesize` is set to  $\sqrt{1/4} = 1/2$  that of `obs.MCMC.samplesize`, and `obs.MCMC.burnin` and `obs.MCMC.interval` are set to  $\sqrt{1/4} = 1/2$  of their respective unconstrained sampling parameters. When `MCMC.effectiveSize` or `MCMLE.effectiveSize` are given, their corresponding obs parameters are set to them multiplied by `obs.MCMC.mul`.

Lastly, if `MCMLE.effectiveSize` is not NULL but `obs.MCMLE.effectiveSize` is, the constrained sample's target effective size is set adaptively to achieve a similar precision for the estimating functions as that achieved for the unconstrained.

- `obs.MCMC.impute.min_informative`, `obs.MCMC.impute.default_density`  
 Controls for imputation of missing dyads for initializing MCMC sampling. If numeric, `obs.MCMC.impute.min_informative` specifies the minimum number dyads that need to be non-missing before sample network density is used as the imputation density. It can also be specified as a function that returns this value. `obs.MCMC.impute.default_density` similarly controls the imputation density when number of non-missing dyads is too low.
- `MCMLE.min.depfac`, `MCMLE.sampsiz.e.boost.pow`  
 When using adaptive MCMC effective size, and methods that increase the MCMC sample size, use `MCMLE.sampsiz.e.boost.pow` as the power of the boost amount (relative to the boost of the target effective size), but ensure that sample size is no less than `MCMLE.min.depfac` times the target effective size.
- `MCMLE.MCMC.precision`, `MCMLE.MCMC.max.ESS.frac`  
`MCMLE.MCMC.precision` is a vector of upper bounds on the standard errors induced by the MCMC algorithm, expressed as a percentage of the total standard error. The MCMLE algorithm will terminate when the MCMC standard errors are below the precision bound, and the Hummel step length is 1 for two consecutive iterations. This is an experimental feature.  
 If effective sample size is used (see `MCMC.effectiveSize`), then `ergm` may increase the target ESS to reduce the MCMC standard error.
- `MCMLE.metric` Method to calculate the loglikelihood approximation. See Hummel et al. (2012) for an explanation of "lognormal" and "naive".
- `MCMLE.method` Deprecated. By default, `ergm` uses `trust`, and falls back to `optim` with Nelder-Mead method when `trust` fails.
- `MCMLE.dampening`  
 (logical) Should likelihood dampening be used?
- `MCMLE.dampening.min.ess`  
 The effective sample size below which dampening is used.
- `MCMLE.dampening.level`  
 The proportional distance from boundary of the convex hull move.
- `MCMLE.steplength.margin`  
 The extra margin required for a Hummel step to count as being inside the convex hull of the sample. Set this to 0 if the step length gets stuck at the same value over several iterations. Set it to NULL to use fixed step length. Note that this parameter is required to be non-NULL for MCMLE termination using Hummel or precision criteria.
- `MCMLE.steplength`  
 Multiplier for step length (on the mean-value parameter scale), which may (for values less than one) make fitting more stable at the cost of computational efficiency.  
 If `MCMLE.steplength.margin` is not NULL, the step length will be set using the algorithm of Hummel et al. (2012). In that case, it will serve as the maximum step length considered. However, setting it to anything other than 1 will preclude using Hummel or precision as termination criteria.
- `MCMLE.steplength.parallel`  
 Whether parallel multisection search (as opposed to a bisection search) for the Hummel step length should be used if running in multiple threads. Possible

values (partially matched) are "never", and (default) "observational" (i.e., when missing data MLE is used).

#### MCMLE.sequential

Logical: If TRUE, the next iteration of the fit uses the last network sampled as the starting network. If FALSE, always use the initially passed network. The results should be similar (stochastically), but the TRUE option may help if the `target.stats` in the `ergm()` function are far from the initial network.

#### MCMLE.density.guard.min, MCMLE.density.guard

A simple heuristic to stop optimization if it finds itself in an overly dense region, which usually indicates ERGM degeneracy: if the sampler encounters a network configuration that has more than `MCMLE.density.guard.min` edges and whose number of edges exceeds the observed network by more than `MCMLE.density.guard`, the optimization process will be stopped with an error.

#### MCMLE.effectiveSize, MCMLE.effectiveSize.interval\_drop, MCMLE.burnin, MCMLE.interval, MCMLE.samplesize, MCMLE.samplesize.per\_theta, MCMLE.samplesize.min

Sets the corresponding MCMC.\* parameters when `main.method="MCMLE"` (the default). Used because defaults may be different for different methods. `MCMLE.samplesize.per_theta` controls the MCMC sample size (not target effective size) as a function of the number of (curved) parameters in the model, and `MCMLE.samplesize.min` sets the minimum sample size regardless of their number.

#### MCMLE.steplength.solver

The linear program solver to use for MCMLE step length calculation. Can be either "glpk" to use **Rglpk** or "lpsolve" to use **lpSolveAPI**. **Rglpk** can be orders of magnitude faster, particularly for models with many parameters and with large sample sizes, so it is used where available; but it requires an external library to install under some operating systems, so fallback to **lpSolveAPI** provided.

#### MCMLE.last.boost

For the Hummel termination criterion, increase the MCMC sample size of the last iteration by this factor.

#### MCMLE.steplength.esteq

For curved ERGMs, should the estimating function values be used to compute the Hummel step length? This allows the Hummel stepping algorithm converge when some sufficient statistics are at 0.

#### MCMLE.steplength.miss.sample

In fitting the missing data MLE, the rules for step length become more complicated. In short, it is necessary for *all* points in the constrained sample to be in the convex hull of the unconstrained (though they may be on the border); and it is necessary for their centroid to be in its interior. This requires checking a large number of points against whether they are in the convex hull, so to speed up the procedure, a sample is taken of the points most likely to be outside it. This parameter specifies the sample size or a function of the unconstrained sample matrix to determine the sample size. If the parameter or the return value of the function has a length of 2, the first element is used as the sample size, and the second element is used in an early-termination heuristic, only continuing the tests until this many test points in a row did not yield a change in the step length.

- `MCMLE.steplength.min`  
Stops MCMLE estimation when the step length gets stuck below this minimum value.
- `MCMLE.save_intermediates`  
Every iteration, after MCMC sampling, save the MCMC sample and some miscellaneous information to a file with this name. This is mainly useful for diagnostics and debugging. The name is passed through `sprintf()` with iteration number as the second argument. (For example, `MCMLE.save_intermediates="step_%03d.RData"` will save to `step_001.RData`, `step_002.RData`, etc.)
- `SA.phase1_n`  
A constant or a function of number of free parameters  $q$ , number of free canonical statistic  $p$ , and network size  $n$ , giving the number of MCMC samples to draw in Phase 1 of the stochastic approximation algorithm. Defaults to  $\max(200, 7 + 3p)$ . See Snijders (2002) for details.
- `SA.initial_gain`  
Initial gain to Phase 2 of the stochastic approximation algorithm. Defaults to 0.1. See Snijders (2002) for details.
- `SA.nsubphases`  
Number of sub-phases in Phase 2 of the stochastic approximation algorithm. Defaults to `MCMLE.maxit`. See Snijders (2002) for details.
- `SA.min_iterations`, `SA.max_iterations`  
A constant or a function of number of free parameters  $q$ , number of free canonical statistic  $p$ , and network size  $n$ , giving the baseline numbers of iterations within each subphase of Phase 2 of the stochastic approximation algorithm. Default to  $7 + p$  and  $207 + p$ , respectively. See Snijders (2002) for details.
- `SA.phase3_n`  
Sample size for the MCMC sample in Phase 3 of the stochastic approximation algorithm. See Snijders (2002) for details.
- `SA.burnin`, `SA.interval`, `SA.samplesize`  
Sets the corresponding MCMC.\* parameters when `main.method="Stochastic-Approximation"`.
- `CD.samplesize.per_theta`, `obs.CD.samplesize.per_theta`, `CD.maxit`,  
`CD.conv.min.pval`, `CD.NR.maxit`, `CD.NR.reltol`, `CD.metric`, `CD.method`,  
`CD.dampening`, `CD.dampening.min.ess`, `CD.dampening.level`,  
`CD.steplength.margin`, `CD.steplength`, `CD.steplength.parallel`,  
`CD.adaptive.epsilon`, `CD.steplength.esteq`, `CD.steplength.miss.sample`,  
`CD.steplength.min`, `CD.steplength.solver`  
Miscellaneous tuning parameters of the CD sampler and optimizer. These have the same meaning as their MCMLE.\* and MCMC.\* counterparts.  
Note that only the Hotelling's stopping criterion is implemented for CD.
- `CD.nsteps`, `CD.multiplicity`  
Main settings for contrastive divergence to obtain initial values for the estimation: respectively, the number of Metropolis–Hastings steps to take before reverting to the starting value and the number of tentative proposals per step. Computational experiments indicate that increasing `CD.multiplicity` improves the estimate faster than increasing `CD.nsteps` — up to a point — but it also samples from the wrong distribution, in the sense that while as  $CD.nsteps \rightarrow \infty$ , the CD estimate approaches the MLE, this is not the case for `CD.multiplicity`.  
In practice, MPLE, when available, usually outperforms CD for even a very high `CD.nsteps` (which is, in turn, not very stable), so CD is useful primarily when MPLE is not available. This feature is to be considered experimental and in flux.

The default values have been set experimentally, providing a reasonably stable, if not great, starting values.

CD.nsteps.obs, CD.multiplicity.obs	When there are missing dyads, CD.nsteps and CD.multiplicity must be set to a relatively high value, as the network passed is not necessarily a good start for CD. Therefore, these settings are in effect if there are missing dyads in the observed network, using a higher default number of steps.
loglik	See <a href="#">control.ergm.bridge()</a>
term.options	A list of additional arguments to be passed to term initializers. See <a href="#">? term.options</a> .
seed	Seed value (integer) for the random number generator. See <a href="#">set.seed()</a> .
parallel	Number of threads in which to run the sampling. Defaults to 0 (no parallelism). See <a href="#">ergm-parallel</a> for details and troubleshooting.
parallel.type	API to use for parallel processing. Defaults to using the <b>parallel</b> package with PSOCK clusters. See <a href="#">ergm-parallel</a> .
parallel.version.check	Logical: If TRUE, check that the version of <b>ergm</b> running on the slave nodes is the same as that running on the master node.
parallel.inherit.MT	Logical: If TRUE, slave nodes and processes inherit the <a href="#">set.MT_terms()</a> setting.
...	A dummy argument to catch deprecated or mistyped control parameters.

## Details

Different estimation methods or components of estimation have different efficient tuning parameters; and we generally want to use the estimation controls to inform the simulation controls in [control.simulate.ergm\(\)](#). To accomplish this, [control.ergm\(\)](#) uses method-specific controls, with the method identified by the prefix:

CD	Contrastive Divergence estimation (Krivitsky 2017)
MPL	Maximum Pseudo-Likelihood Estimation (Strauss and Ikeda 1990)
MCML	Monte-Carlo MLE (Hunter and Handcock 2006; Hummel et al. 2012)
SA	Stochastic Approximation via Robbins–Monro Robbins and Monro (1951); Snijders (2002)
SAN	Simulated Annealing used when <code>target.stats</code> are specified for <a href="#">ergm()</a>
obs	Missing data MLE (Handcock and Gile 2010)
init	Affecting how initial parameter guesses are obtained
parallel	Affecting parallel processing
MCMC	Low-level MCMC simulation controls

Corresponding MCMC controls will usually be overwritten by the method-specific ones. After the estimation finishes, they will contain the last MCMC parameters used.

## Value

A list with arguments as components.

## References

- Firth D (1993). “Bias Reduction of Maximum Likelihood Estimates.” *Biometrika*, **80**(1), 27–38. doi:10.1093/biomet/80.1.27.
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- Snijders TAB (2002). “Markov chain Monte Carlo Estimation of Exponential Random Graph Models.” *Journal of Social Structure*, **3**(2).
- Strauss D, Ikeda M (1990). “Pseudolikelihood Estimation for Social Networks.” *Journal of the American Statistical Association*, **85**(409), 204–212. ISSN 0162-1459. doi:10.1080/01621459.1990.10475327.
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- (Firth 1993), Bias Reduction in Maximum Likelihood Estimates. *Biometrika*, 80: 27-38.
  - Kristoffer Sahlin. Estimating convergence of Markov chain Monte Carlo simulations. Master’s Thesis. Stockholm University, 2011. <https://www2.math.su.se/matstat/reports/master/2011/rep2/report.pdf>

## See Also

`ergm()`. The `control.simulate()` function performs a similar function for `simulate.ergm()`; `control.gof()` performs a similar function for `gof()`.

---

control.ergm.bridge     *Auxiliaries for Controlling `ergm.bridge.llr()` and `logLik.ergm()`*

---

## Description

Auxiliary functions as user interfaces for fine-tuning the `ergm.bridge.llr()` algorithm, which approximates log likelihood ratios using bridge sampling.

By default, the bridge sampler inherits its control parameters from the `ergm()` fit; `control.logLik.ergm()` allows the user to selectively override them.

## Usage

```
control.ergm.bridge(
  bridge.nsteps = 16,
  bridge.target.se = NULL,
  bridge.bidirectional = TRUE,
  drop = TRUE,
  MCMC.burnin = MCMC.interval * 128,
  MCMC.burnin.between = max(ceiling(MCMC.burnin/sqrt(bridge.nsteps)), MCMC.interval * 16),
  MCMC.interval = 128,
  MCMC.samplesize = 16384,
  obs.MCMC.burnin = obs.MCMC.interval * 128,
  obs.MCMC.burnin.between = max(ceiling(obs.MCMC.burnin/sqrt(bridge.nsteps)),
  obs.MCMC.interval * 16),
  obs.MCMC.interval = MCMC.interval,
  obs.MCMC.samplesize = MCMC.samplesize,
  MCMC.prop = trim_env(~sparse + .triadic),
  MCMC.prop.weights = "default",
  MCMC.prop.args = list(),
  obs.MCMC.prop = MCMC.prop,
  obs.MCMC.prop.weights = MCMC.prop.weights,
  obs.MCMC.prop.args = MCMC.prop.args,
  MCMC.maxedges = Inf,
  MCMC.packagenames = c(),
  term.options = list(),
  seed = NULL,
  parallel = 0,
  parallel.type = NULL,
  parallel.version.check = TRUE,
  parallel.inherit.MT = FALSE,
  ...
)

control.logLik.ergm(
  bridge.nsteps = 16,
  bridge.target.se = NULL,
```

```

bridge.bidirectional = TRUE,
drop = NULL,
MCMC.burnin = NULL,
MCMC.interval = NULL,
MCMC.samplesize = NULL,
obs.MCMC.samplesize = MCMC.samplesize,
obs.MCMC.interval = MCMC.interval,
obs.MCMC.burnin = MCMC.burnin,
MCMC.prop = NULL,
MCMC.prop.weights = NULL,
MCMC.prop.args = NULL,
obs.MCMC.prop = MCMC.prop,
obs.MCMC.prop.weights = MCMC.prop.weights,
obs.MCMC.prop.args = MCMC.prop.args,
MCMC.maxedges = Inf,
MCMC.packagenames = NULL,
term.options = NULL,
seed = NULL,
parallel = NULL,
parallel.type = NULL,
parallel.version.check = TRUE,
parallel.inherit.MT = FALSE,
...
)

```

## Arguments

`bridge.nsteps` Number of geometric bridges to use.

`bridge.target.se`  
If not NULL, if the estimated MCMC standard error of the likelihood estimate exceeds this, repeat the bridge sampling, accumulating samples.

`bridge.bidirectional`  
Whether the bridge sampler first bridges from from to to, then from to to from (skipping the first burn-in), etc. if multiple attempts are required.

`drop` See [control.ergm\(\)](#).

`MCMC.burnin` Number of proposals before any MCMC sampling is done. It typically is set to a fairly large number.

`MCMC.burnin.between`  
Number of proposals between the bridges; typically, less and less is needed as the number of steps decreases.

`MCMC.interval` Number of proposals between sampled statistics.

`MCMC.samplesize`  
Number of network statistics, randomly drawn from a given distribution on the set of all networks, returned by the Metropolis-Hastings algorithm.

`obs.MCMC.burnin`, `obs.MCMC.burnin.between`, `obs.MCMC.interval`,  
`obs.MCMC.samplesize`  
The obs versions of these arguments are for the unobserved data simulation algorithm.

MCMC.prop	Specifies the proposal (directly) and/or a series of "hints" about the structure of the model being sampled. The specification is in the form of a one-sided formula with hints separated by + operations. If the LHS exists and is a string, the proposal to be used is selected directly. A common and default "hint" is ~sparse, indicating that the network is sparse and that the sample should put roughly equal weight on selecting a dyad with or without a tie as a candidate for toggling.
MCMC.prop.weights	Specifies the proposal distribution used in the MCMC Metropolis-Hastings algorithm. Possible choices depending on selected reference and constraints arguments of the <code>ergm()</code> function, but often include "TNT" and "random", and the "default" is to use the one with the highest priority available.
MCMC.prop.args	An alternative, direct way of specifying additional arguments to proposal.
obs.MCMC.prop, obs.MCMC.prop.weights, obs.MCMC.prop.args	The obs versions of these arguments are for the unobserved data simulation algorithm.
MCMC.maxedges	The maximum number of edges that may occur during the MCMC sampling. If this number is exceeded at any time, sampling is stopped immediately.
MCMC.packagenames	Names of packages in which to look for change statistic functions in addition to those autodetected. This argument should not be needed outside of very strange setups.
term.options	A list of additional arguments to be passed to term initializers. See <code>?term.options</code> .
seed	Seed value (integer) for the random number generator. See <code>set.seed()</code> .
parallel	Number of threads in which to run the sampling. Defaults to 0 (no parallelism). See <code>ergm-parallel</code> for details and troubleshooting.
parallel.type	API to use for parallel processing. Defaults to using the <b>parallel</b> package with PSOCK clusters. See <code>ergm-parallel</code> .
parallel.version.check	Logical: If TRUE, check that the version of <b>ergm</b> running on the slave nodes is the same as that running on the master node.
parallel.inherit.MT	Logical: If TRUE, slave nodes and processes inherit the <code>set.MT_terms()</code> setting.
...	A dummy argument to catch deprecated or mistyped control parameters.

### Details

`control.ergm.bridge()` is only used within a call to the `ergm.bridge.llr()`, `ergm.bridge.dindstart.llk()`, or `ergm.bridge.0.llk()` functions.

`control.logLik.ergm()` is only used within a call to the `logLik.ergm()`.

### Value

A list with arguments as components.

**See Also**

[ergm.bridge.llr\(\)](#)  
[logLik.ergm\(\)](#)

---

control.gof

*Auxiliary for Controlling ERGM Goodness-of-Fit Evaluation*

---

**Description**

Auxiliary function as user interface for fine-tuning ERGM Goodness-of-Fit Evaluation.

The control.gof.ergm version is intended to be used with [gof.ergm\(\)](#) specifically and will "inherit" as many control parameters from [ergm](#) fit as possible().

**Usage**

```
control.gof.formula(  
  nsim = 100,  
  MCMC.burnin = 10000,  
  MCMC.interval = 1000,  
  MCMC.batch = 0,  
  MCMC.prop = trim_env(~sparse + .triadic),  
  MCMC.prop.weights = "default",  
  MCMC.prop.args = list(),  
  MCMC.maxedges = Inf,  
  MCMC.packagenames = c(),  
  MCMC.runtime.traceplot = FALSE,  
  network.output = "network",  
  seed = NULL,  
  parallel = 0,  
  parallel.type = NULL,  
  parallel.version.check = TRUE,  
  parallel.inherit.MT = FALSE  
)
```

```
control.gof.ergm(  
  nsim = 100,  
  MCMC.burnin = NULL,  
  MCMC.interval = NULL,  
  MCMC.batch = NULL,  
  MCMC.prop = NULL,  
  MCMC.prop.weights = NULL,  
  MCMC.prop.args = NULL,  
  MCMC.maxedges = NULL,  
  MCMC.packagenames = NULL,  
  MCMC.runtime.traceplot = FALSE,  
  network.output = "network",
```

```

    seed = NULL,
    parallel = 0,
    parallel.type = NULL,
    parallel.version.check = TRUE,
    parallel.inherit.MT = FALSE
  )

```

## Arguments

<code>nsim</code>	Number of networks to be randomly drawn using Markov chain Monte Carlo. This sample of networks provides the basis for comparing the model to the observed network.
<code>MCMC.burnin</code>	Number of proposals before any MCMC sampling is done. It typically is set to a fairly large number.
<code>MCMC.interval</code>	Number of proposals between sampled statistics.
<code>MCMC.batch</code>	if not 0 or NULL, sample about this many networks per call to the lower-level code; this can be useful if <code>output=</code> is a function, where it can be used to limit the number of networks held in memory at any given time.
<code>MCMC.prop</code>	Specifies the proposal (directly) and/or a series of "hints" about the structure of the model being sampled. The specification is in the form of a one-sided formula with hints separated by + operations. If the LHS exists and is a string, the proposal to be used is selected directly. A common and default "hint" is <code>~sparse</code> , indicating that the network is sparse and that the sample should put roughly equal weight on selecting a dyad with or without a tie as a candidate for toggling.
<code>MCMC.prop.weights</code>	Specifies the proposal distribution used in the MCMC Metropolis-Hastings algorithm. Possible choices depending on selected reference and constraints arguments of the <code>ergm()</code> function, but often include "TNT" and "random", and the "default" is to use the one with the highest priority available.
<code>MCMC.prop.args</code>	An alternative, direct way of specifying additional arguments to proposal.
<code>MCMC.maxedges</code>	The maximum number of edges that may occur during the MCMC sampling. If this number is exceeded at any time, sampling is stopped immediately.
<code>MCMC.packagenames</code>	Names of packages in which to look for change statistic functions in addition to those autodetected. This argument should not be needed outside of very strange setups.
<code>MCMC.runtime.traceplot</code>	Logical: If TRUE, plot traceplots of the MCMC sample.
<code>network.output</code>	R class with which to output networks. The options are "network" (default) and "edgelist.compressed" (which saves space but only supports networks without vertex attributes)
<code>seed</code>	Seed value (integer) for the random number generator. See <code>set.seed()</code> .
<code>parallel</code>	Number of threads in which to run the sampling. Defaults to 0 (no parallelism). See <code>ergm-parallel</code> for details and troubleshooting.

- `parallel.type` API to use for parallel processing. Defaults to using the **parallel** package with PSOCK clusters. See [ergm-parallel](#).
- `parallel.version.check`  
Logical: If TRUE, check that the version of **ergm** running on the slave nodes is the same as that running on the master node.
- `parallel.inherit.MT`  
Logical: If TRUE, slave nodes and processes inherit the `set.MT_terms()` setting.

### Details

This function is only used within a call to the `gof()` function. See the Usage section in `gof()` for details.

### Value

A list with arguments as components.

### See Also

`gof()`. The `control.simulate()` function performs a similar function for `simulate.ergm()`; `control.ergm()` performs a similar function for `ergm()`.

---

control.san

*Auxiliary for Controlling SAN*

---

### Description

Auxiliary function as user interface for fine-tuning simulated annealing algorithm.

### Usage

```
control.san(
  SAN.maxit = 4,
  SAN.tau = 1,
  SAN.invcov = NULL,
  SAN.invcov.diag = FALSE,
  SAN.nsteps.alloc = function(nsim) 2^seq_len(nsim),
  SAN.nsteps = 2^19,
  SAN.samplesize = 2^12,
  SAN.prop = trim_env(~sparse + .triadic),
  SAN.prop.weights = "default",
  SAN.prop.args = list(),
  SAN.packagenames = c(),
  SAN.ignore.finite.offsets = TRUE,
  term.options = list(),
  seed = NULL,
```

```

parallel = 0,
parallel.type = NULL,
parallel.version.check = TRUE,
parallel.inherit.MT = FALSE
)

```

## Arguments

SAN.maxit	Number of temperature levels to use.
SAN.tau	Tuning parameter, specifying the temperature of the process during the <i>penultimate</i> iteration. (During the last iteration, the temperature is set to 0, resulting in a greedy search, and during the previous iterations, the temperature is set to $SAN.tau * (\text{iterations left after this one})$ ).
SAN.invcov	Initial inverse covariance matrix used to calculate Mahalanobis distance in determining how far a proposed MCMC move is from the <code>target.stats</code> vector. If NULL, initially set to the identity matrix. In either case, during subsequent runs, it is estimated empirically.
SAN.invcov.diag	Whether to only use the diagonal of the covariance matrix. It seems to work better in practice.
SAN.nsteps.alloc	Either a numeric vector or a function of the number of runs giving a sequence of relative lengths of simulated annealing runs.
SAN.nsteps	Number of MCMC proposals for all the annealing runs combined.
SAN.samplesize	Number of realisations' statistics to obtain for tuning purposes.
SAN.prop	Specifies the proposal (directly) and/or a series of "hints" about the structure of the model being sampled. The specification is in the form of a one-sided formula with hints separated by + operations. If the LHS exists and is a string, the proposal to be used is selected directly. A common and default "hint" is <code>~sparse</code> , indicating that the network is sparse and that the sample should put roughly equal weight on selecting a dyad with or without a tie as a candidate for toggling.
SAN.prop.weights	Specifies the proposal distribution used in the SAN Metropolis-Hastings algorithm. Possible choices depending on selected reference and constraints arguments of the <code>ergm()</code> function, but often include "TNT" and "random", and the "default" is to use the one with the highest priority available.
SAN.prop.args	An alternative, direct way of specifying additional arguments to proposal.
SAN.packagenames	Names of packages in which to look for change statistic functions in addition to those autodetected. This argument should not be needed outside of very strange setups.
SAN.ignore.finite.offsets	Whether SAN should ignore (treat as 0) finite offsets.
term.options	A list of additional arguments to be passed to term initializers. See <a href="#">? term.options</a> .

seed	Seed value (integer) for the random number generator. See <a href="#">set.seed()</a> .
parallel	Number of threads in which to run the sampling. Defaults to 0 (no parallelism). See <a href="#">ergm-parallel</a> for details and troubleshooting.
parallel.type	API to use for parallel processing. Defaults to using the <b>parallel</b> package with PSOCK clusters. See <a href="#">ergm-parallel</a> .
parallel.version.check	Logical: If TRUE, check that the version of <b>ergm</b> running on the slave nodes is the same as that running on the master node.
parallel.inherit.MT	Logical: If TRUE, slave nodes and processes inherit the <a href="#">set.MT_terms()</a> setting.

### Details

This function is only used within a call to the [san\(\)](#) function. See the Usage section in [san\(\)](#) for details.

### Value

A list with arguments as components.

### See Also

[san\(\)](#)

---

control.simulate.ergm *Auxiliary for Controlling ERGM Simulation*

---

### Description

Auxiliary function as user interface for fine-tuning ERGM simulation. `control.simulate`, `control.simulate.formula`, and `control.simulate.formula.ergm` are all aliases for the same function.

While the others supply a full set of simulation settings, `control.simulate.ergm` when passed as a control parameter to [simulate.ergm\(\)](#) allows some settings to be inherited from the ERGM stimulation while overriding others.

### Usage

```
control.simulate.formula.ergm(
  MCMC.burnin = MCMC.interval * 16,
  MCMC.interval = 1024,
  MCMC.prop = trim_env(~sparse + .triadic),
  MCMC.prop.weights = "default",
  MCMC.prop.args = list(),
  MCMC.batch = NULL,
  MCMC.effectiveSize = NULL,
```

```

MCMC.effectiveSize.damp = 10,
MCMC.effectiveSize.maxruns = 1000,
MCMC.effectiveSize.burnin.pval = 0.2,
MCMC.effectiveSize.burnin.min = 0.05,
MCMC.effectiveSize.burnin.max = 0.5,
MCMC.effectiveSize.burnin.nmin = 16,
MCMC.effectiveSize.burnin.nmax = 128,
MCMC.effectiveSize.burnin.PC = FALSE,
MCMC.effectiveSize.burnin.scl = 1024,
MCMC.effectiveSize.order.max = NULL,
MCMC.maxedges = Inf,
MCMC.packagenames = c(),
MCMC.runtime.traceplot = FALSE,
network.output = "network",
term.options = NULL,
parallel = 0,
parallel.type = NULL,
parallel.version.check = TRUE,
parallel.inherit.MT = FALSE,
...
)

control.simulate(
  MCMC.burnin = MCMC.interval * 16,
  MCMC.interval = 1024,
  MCMC.prop = trim_env(~sparse + .triadic),
  MCMC.prop.weights = "default",
  MCMC.prop.args = list(),
  MCMC.batch = NULL,
  MCMC.effectiveSize = NULL,
  MCMC.effectiveSize.damp = 10,
  MCMC.effectiveSize.maxruns = 1000,
  MCMC.effectiveSize.burnin.pval = 0.2,
  MCMC.effectiveSize.burnin.min = 0.05,
  MCMC.effectiveSize.burnin.max = 0.5,
  MCMC.effectiveSize.burnin.nmin = 16,
  MCMC.effectiveSize.burnin.nmax = 128,
  MCMC.effectiveSize.burnin.PC = FALSE,
  MCMC.effectiveSize.burnin.scl = 1024,
  MCMC.effectiveSize.order.max = NULL,
  MCMC.maxedges = Inf,
  MCMC.packagenames = c(),
  MCMC.runtime.traceplot = FALSE,
  network.output = "network",
  term.options = NULL,
  parallel = 0,
  parallel.type = NULL,
  parallel.version.check = TRUE,

```

```
    parallel.inherit.MT = FALSE,
    ...
  )

control.simulate.formula(
  MCMC.burnin = MCMC.interval * 16,
  MCMC.interval = 1024,
  MCMC.prop = trim_env(~sparse + .triadic),
  MCMC.prop.weights = "default",
  MCMC.prop.args = list(),
  MCMC.batch = NULL,
  MCMC.effectiveSize = NULL,
  MCMC.effectiveSize.damp = 10,
  MCMC.effectiveSize.maxruns = 1000,
  MCMC.effectiveSize.burnin.pval = 0.2,
  MCMC.effectiveSize.burnin.min = 0.05,
  MCMC.effectiveSize.burnin.max = 0.5,
  MCMC.effectiveSize.burnin.nmin = 16,
  MCMC.effectiveSize.burnin.nmax = 128,
  MCMC.effectiveSize.burnin.PC = FALSE,
  MCMC.effectiveSize.burnin.scl = 1024,
  MCMC.effectiveSize.order.max = NULL,
  MCMC.maxedges = Inf,
  MCMC.packagenames = c(),
  MCMC.runtime.traceplot = FALSE,
  network.output = "network",
  term.options = NULL,
  parallel = 0,
  parallel.type = NULL,
  parallel.version.check = TRUE,
  parallel.inherit.MT = FALSE,
  ...
)

control.simulate.ergm(
  MCMC.burnin = NULL,
  MCMC.interval = NULL,
  MCMC.scale = 1,
  MCMC.prop = NULL,
  MCMC.prop.weights = NULL,
  MCMC.prop.args = NULL,
  MCMC.batch = NULL,
  MCMC.effectiveSize = NULL,
  MCMC.effectiveSize.damp = 10,
  MCMC.effectiveSize.maxruns = 1000,
  MCMC.effectiveSize.burnin.pval = 0.2,
  MCMC.effectiveSize.burnin.min = 0.05,
  MCMC.effectiveSize.burnin.max = 0.5,
```

```

MCMC.effectiveSize.burnin.nmin = 16,
MCMC.effectiveSize.burnin.nmax = 128,
MCMC.effectiveSize.burnin.PC = FALSE,
MCMC.effectiveSize.burnin.scl = 1024,
MCMC.effectiveSize.order.max = NULL,
MCMC.maxedges = Inf,
MCMC.packagenames = NULL,
MCMC.runtime.traceplot = FALSE,
network.output = "network",
term.options = NULL,
parallel = 0,
parallel.type = NULL,
parallel.version.check = TRUE,
parallel.inherit.MT = FALSE,
...
)

```

## Arguments

MCMC.burnin	Number of proposals before any MCMC sampling is done. It typically is set to a fairly large number.
MCMC.interval	Number of proposals between sampled statistics.
MCMC.prop	Specifies the proposal (directly) and/or a series of "hints" about the structure of the model being sampled. The specification is in the form of a one-sided formula with hints separated by + operations. If the LHS exists and is a string, the proposal to be used is selected directly.  A common and default "hint" is <code>~sparse</code> , indicating that the network is sparse and that the sample should put roughly equal weight on selecting a dyad with or without a tie as a candidate for toggling.
MCMC.prop.weights	Specifies the proposal distribution used in the MCMC Metropolis-Hastings algorithm. Possible choices depending on selected reference and constraints arguments of the <code>ergm()</code> function, but often include "TNT" and "random", and the "default" is to use the one with the highest priority available.
MCMC.prop.args	An alternative, direct way of specifying additional arguments to proposal.
MCMC.batch	if not 0 or NULL, sample about this many networks per call to the lower-level code; this can be useful if <code>output=</code> is a function, where it can be used to limit the number of networks held in memory at any given time.
MCMC.effectiveSize,	MCMC.effectiveSize.damp,
MCMC.effectiveSize.maxruns,	MCMC.effectiveSize.burnin.pval,
MCMC.effectiveSize.burnin.min,	MCMC.effectiveSize.burnin.max,
MCMC.effectiveSize.burnin.nmin,	MCMC.effectiveSize.burnin.nmax,
MCMC.effectiveSize.burnin.PC,	MCMC.effectiveSize.burnin.scl,
MCMC.effectiveSize.order.max	

Set MCMC.effectiveSize to a non-NULL value to adaptively determine the burn-in and the MCMC length needed to get the specified effective size; 50 is

a reasonable value. In the adaptive MCMC mode, MCMC is run forward repeatedly ( $\text{MCMC.samplesize} * \text{MCMC.interval}$  steps, up to  $\text{MCMC.effectiveSize.maxruns}$  times) until the target effective sample size is reached or exceeded.

After each run, the returned statistics are mapped to the estimating function scale, then an exponential decay model is fit to the scaled statistics to find that burn-in which would reduce the difference between the initial values of statistics and their equilibrium values by a factor of  $\text{MCMC.effectiveSize.burnin.scl}$  of what it initially was, bounded by  $\text{MCMC.effectiveSize.min}$  and  $\text{MCMC.effectiveSize.max}$  as proportions of sample size. If the best-fitting decay exceeds  $\text{MCMC.effectiveSize.max}$ , the exponential model is considered to be unsuitable and  $\text{MCMC.effectiveSize.min}$  is used.

A Geweke diagnostic is then run, after thinning the sample to  $\text{MCMC.effectiveSize.burnin.nmax}$ . If this Geweke diagnostic produces a  $p$ -value higher than  $\text{MCMC.effectiveSize.burnin.pval}$ , it is accepted.

If  $\text{MCMC.effectiveSize.burnin.PC} > 0$ , instead of using the full sample for burn-in estimation, at most this many principal components are used instead.

The effective size of the post-burn-in sample is computed via Vats et al. (2019), and compared to the target effective size. If it is not matched, the MCMC run is resumed, with the additional draws needed linearly extrapolated but weighted in favor of the baseline  $\text{MCMC.samplesize}$  by the weighting factor  $\text{MCMC.effectiveSize.damp}$  (higher = less damping). Lastly, if after an MCMC run, the number of samples equals or exceeds  $2 * \text{MCMC.samplesize}$ , the chain will be thinned by 2 until it falls below that, while doubling  $\text{MCMC.interval}$ .  $\text{MCMC.effectiveSize.order.max}$  can be used to set the order of the AR model used to estimate the effective sample size and the variance for the Geweke diagnostic.

Lastly, if  $\text{MCMC.effectiveSize}$  is a matrix, say,  $W$ , it will be treated as a target precision (inverse-variance) matrix. If  $V$  is the sample covariance matrix, the target effective size  $n_{\text{eff}}$  will be set such that  $V/n_{\text{eff}}$  is close to  $W$  in magnitude, specifically that  $\text{tr}((V/n_{\text{eff}})W)/p \approx 1$ .

<code>MCMC.maxedges</code>	The maximum number of edges that may occur during the MCMC sampling. If this number is exceeded at any time, sampling is stopped immediately.
<code>MCMC.packagenames</code>	Names of packages in which to look for change statistic functions in addition to those autodetected. This argument should not be needed outside of very strange setups.
<code>MCMC.runtime.traceplot</code>	Logical: If TRUE, plot traceplots of the MCMC sample.
<code>network.output</code>	R class with which to output networks. The options are "network" (default) and "edgelist.compressed" (which saves space but only supports networks without vertex attributes)
<code>term.options</code>	A list of additional arguments to be passed to term initializers. See <a href="#">? term.options</a> .
<code>parallel</code>	Number of threads in which to run the sampling. Defaults to 0 (no parallelism). See <a href="#">ergm-parallel</a> for details and troubleshooting.
<code>parallel.type</code>	API to use for parallel processing. Defaults to using the <b>parallel</b> package with PSOCK clusters. See <a href="#">ergm-parallel</a> .

<code>parallel.version.check</code>	Logical: If TRUE, check that the version of <b>ergm</b> running on the slave nodes is the same as that running on the master node.
<code>parallel.inherit.MT</code>	Logical: If TRUE, slave nodes and processes inherit the <code>set.MT_terms()</code> setting.
<code>...</code>	A dummy argument to catch deprecated or mistyped control parameters.
<code>MCMC.scale</code>	For <code>control.simulate.ergm()</code> inheriting <code>MCMC.burnin</code> and <code>MCMC.interval</code> from the <b>ergm</b> fit, the multiplier for the inherited values. This can be useful because MCMC parameters used in the fit are tuned to generate a specific effective sample size for the sufficient statistic in a large MCMC sample, so the inherited values might not generate independent realisations.

### Details

This function is only used within a call to the ERGM `simulate()` function. See the Usage section in `simulate.ergm()` for details.

### Value

A list with arguments as components.

### See Also

`simulate.ergm()`, `simulate.formula()`. `control.ergm()` performs a similar function for `ergm()`; `control.gof()` performs a similar function for `gof()`.

---

`ctriple-ergmTerm`      *Cyclic triples*

---

### Description

By default, this term adds one statistic to the model, equal to the number of cyclic triples in the network, defined as a set of edges of the form  $\{(i \rightarrow j), (j \rightarrow k), (k \rightarrow i)\}$ .

### Usage

```
# binary: ctriiple(attr=NULL, diff=FALSE, levels=NULL)

# binary: ctriad
```

**Arguments**

attr, diff	quantitative attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) If attr is specified and diff is FALSE , then the statistic is the number of cyclic triples where all three nodes have the same value of the attribute. If attr is specified and diff is TRUE , then one statistic is added to the model for each value of attr, equal to the number of cyclic triples where all three nodes have that value of the attribute.
levels	specifies the value of attr to consider if attr is passed and diff=TRUE. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**Note**

This term can only be used with directed networks.

for all directed networks, triangle is equal to ttriple+ctruple , so at most two of these three terms can be in a model.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, triad-related, binary

---

Curve-ergmTerm

*Impose a curved structure on term parameters*

---

**Description**

Arguments may have the same forms as in the API, but for convenience, alternative forms are accepted.

If the model in formula is curved, then the outputs of this operator term's map argument will be used as inputs to the curved terms of the formula model.

Curve is an obsolete alias and may be deprecated and removed in a future release.

**Usage**

```
# binary: Curve(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf, cov=NULL)

# binary: Parametrise(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf,
#                   cov=NULL)

# binary: Parametrize(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf,
#                   cov=NULL)

# valued: Curve(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf, cov=NULL)

# valued: Parametrise(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf,
```

```
#          cov=NULL)

# valued: Parametrize(formula, params, map, gradient=NULL, minpar=-Inf, maxpar=+Inf,
#          cov=NULL)
```

### Arguments

formula	a one-sided <a href="#">ergm()</a> -style formula with the terms to be evaluated
params	a named list whose names are the curved parameter names, may also be a character vector with names.
map	the mapping from curved to canonical. May have the following forms: <ul style="list-style-type: none"> <li>• a function(<math>x</math>, <math>n</math>, ...) treated as in the API: called with <math>x</math> set to the curved parameter vector, <math>n</math> to the length of output expected, and <math>cov</math>, if present, passed in ... The function must return a numeric vector of length <math>n</math>.</li> <li>• a numeric vector to fix the output coefficients, like in an offset.</li> <li>• a character string to select (partially-matched) one of predefined forms. Currently, the defined forms include: <ul style="list-style-type: none"> <li>– "rep" recycle the input vector to the length of the output vector as a rep function would.</li> </ul> </li> </ul>
gradient	its gradient function. It is optional if map is constant or one of the predefined forms; otherwise it must have one of the following forms: <ul style="list-style-type: none"> <li>• a function(<math>x</math>, <math>n</math>, ...) treated as in the API: called with <math>x</math> set to the curved parameter vector, <math>n</math> to the length of output expected, and <math>cov</math>, if present, passed in ... The function must return a numeric matrix with <math>\text{length}(\text{params})</math> rows and <math>n</math> columns.</li> <li>• a numeric matrix to fix the gradient; this is useful when map is linear.</li> <li>• a character string to select (partially-matched) one of predefined forms. Currently, the defined forms include: <ul style="list-style-type: none"> <li>– "linear" calculate the (constant) gradient matrix using finite differences. Note that this will be done only once at the initialization stage, so use only if you are certain map is, in fact, linear.</li> </ul> </li> </ul>
minpar, maxpar	the minimum and maximum allowed curved parameter values. The parameters will be recycled to the appropriate length.
cov	optional

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

cycle-ergmTerm	<i>k</i> -Cycle Census
----------------	------------------------

---

**Description**

This term adds one network statistic to the model for each value of  $k$ , corresponding to the number of  $k$ -cycles (or, alternately, semicycles) in the graph.

This term can be used with either directed or undirected networks.

**Usage**

```
# binary: cycle(k, semi=FALSE)
```

**Arguments**

<code>k</code>	a vector of integers giving the cycle lengths to count. Directed cycle lengths may range from 2 to $N$ (the network size); undirected cycle lengths and semicycle lengths may range from 3 to $N$ ; length 2 semicycles are not currently supported.
<code>semi</code>	an optional logical indicating whether semicycles (rather than directed cycles) should be counted; this is ignored in the undirected case.
<code>directed</code>	2-cycles are equivalent to mutual dyads.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, undirected, binary

---

cyclicalities-ergmTerm	<i>Cyclical ties</i>
------------------------	----------------------

---

**Description**

This term adds one statistic, equal to the number of ties  $i \rightarrow j$  such that there exists a two-path from  $j$  to  $i$ . (Related to the `ttriple` term.)

**Usage**

```
# binary: cyclicalities(attr=NULL, levels=NULL)
```

```
# valued: cyclicalities(threshold=0)
```

**Arguments**

attr	quantitative attribute (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.) If set, all three nodes involved ( $i$ , $j$ , and the node on the two-path) must match on this attribute in order for $i \rightarrow j$ to be counted.
levels	TODO (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, undirected, binary, valued

---

cyclicalweights-ergmTerm  
*Cyclical weights*

---

**Description**

This statistic implements the cyclical weights statistic, like that defined by Krivitsky (2012), Equation 13, but with the focus dyad being  $y_{j,i}$  rather than  $y_{i,j}$ . For each option, the first (and the default) is more stable but also more conservative, while the second is more sensitive but more likely to induce a multimodal distribution of networks.

**Usage**

```
# valued: cyclicalweights(twopath="min", combine="max", affect="min")
```

**Arguments**

twopath	the minimum of the constituent dyads ( "min" ) or their geometric mean ( "geomean" )
combine	the maximum of the 2-path strengths ( "max" ) or their sum ( "sum" )
affected	the minimum of the focus dyad and the combined strength of the two paths ( "min" ) or their geometric mean ( "geomean" )

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, nonnegative, undirected, valued

---

degcor-ergmTerm      *Degree Correlation*

---

**Description**

This term adds one network statistic equal to the correlation of the degrees of all pairs of nodes in the network which are tied. Only coded for undirected networks.

**Usage**

```
# binary: degcor
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** undirected, binary

---

degcrossprod-ergmTerm      *Degree Cross-Product*

---

**Description**

This term adds one network statistic equal to the mean of the cross-products of the degrees of all pairs of nodes in the network which are tied. Only coded for undirected networks.

**Usage**

```
# binary: degcrossprod
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** undirected, binary

---

degrange-ergmTerm      *Degree range*

---

### Description

This term adds one network statistic to the model for each element of `from` (or `to`); the  $i$ th such statistic equals the number of nodes in the network of degree greater than or equal to `from[i]` but strictly less than `to[i]`, i.e. with edges in semiopen interval `[from, to)`.

### Usage

```
# binary: degrange(from, to=+Inf, by=NULL, homophily=FALSE, levels=NULL)
```

### Arguments

`from, to`            vectors of distinct integers. If one of the vectors have length 1, it is recycled to the length of the other. Otherwise, it must have the same length.

`by, levels, homophily`  
the optional argument `by` specifies a vertex attribute (see [Specifying Vertex attributes](#) and [Levels \(?nodal\\_attributes\)](#) for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

### Details

This term can only be used with undirected networks; for directed networks see `idegrange` and `odegrange`. This term can be used with bipartite networks, and will count nodes of both first and second mode in the specified degree range. To count only nodes of the first mode ("actors"), use `b1degrange` and to count only those fo the second mode ("events"), use `b2degrange`.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, undirected, binary

---

degree-ergmTerm      *Degree*

---

### Description

This term adds one network statistic to the model for each element in `d`; the  $i$ th such statistic equals the number of nodes in the network of degree `d[i]`, i.e. with exactly `d[i]` edges. This term can only be used with undirected networks; for directed networks see `idegree` and `odegree`.

### Usage

```
# binary: degree(d, by=NULL, homophily=FALSE, levels=NULL)
```

### Arguments

`d`                      vector of distinct integers

`by, levels, homophily`  
the optional argument `by` specifies a vertex attribute (see `Specifying Vertex attributes` and `Levels (?nodal_attributes)` for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, frequently-used, undirected, binary

---

degree1.5-ergmTerm      *Degree to the 3/2 power*

---

### Description

This term adds one network statistic to the model equaling the sum over the actors of each actor's degree taken to the  $3/2$  power (or, equivalently, multiplied by its square root). This term is an undirected analog to the terms of Snijders et al. (2010), equations (11) and (12). This term can only be used with undirected networks.

### Usage

```
# binary: degree1.5
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** undirected, binary

---

degreedist	<i>Computes and Returns the Degree Distribution Information for a Given Network</i>
------------	---

---

**Description**

The `degreedist` generic computes and returns the degree distribution (number of vertices in the network with each degree value) for a given network. This help page documents the function. For help about [the ERGM sample space constraint with that name](#), try `help("degreedist-constraint")`.

**Usage**

```
degreedist(object, ...)

## S3 method for class 'network'
degreedist(object, print = TRUE, ...)
```

**Arguments**

<code>object</code>	a network object or some other object for which degree distribution is meaningful.
<code>...</code>	Additional arguments to functions.
<code>print</code>	logical, whether to print the degree distribution.

**Value**

If directed, a matrix of the distributions of in and out degrees; this is row bound and only contains degrees for which one of the in or out distributions has a positive count. If bipartite, a list containing the degree distributions of `b1` and `b2`. Otherwise, a vector of the positive values in the degree distribution

**Methods (by class)**

- `degreedist(network)`: Method for `network` objects.

**Examples**

```
data(faux.mesa.high)
degreedist(faux.mesa.high)
```

---

`degreedist-ergmConstraint`*Preserve the degree distribution of the given network*

---

**Description**

Only networks whose degree distributions are the same as those in the network passed in the model formula have non-zero probability.

**Usage**

```
# degreedist
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, undirected

---

`degrees-ergmConstraint`*Preserve the degree of each vertex of the given network*

---

**Description**

Only networks whose vertex degrees are the same as those in the network passed in the model formula have non-zero probability. If the network is directed, both indegree and outdegree are preserved.

**Usage**

```
# degrees
```

```
# nodedegrees
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, undirected

---

density-ergmTerm      *Density*

---

### Description

This term adds one network statistic equal to the density of the network. For undirected networks, density equals `kstar(1)` or edges divided by  $n(n-1)/2$ ; for directed networks, density equals edges or `istar(1)` or `ostar(1)` divided by  $n(n-1)$ .

### Usage

```
# binary: density
```

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, binary

---

diff-ergmTerm      *Difference*

---

### Description

For values of `pow` other than 0, this term adds one network statistic to the model, equaling the sum, over directed edges  $(i, j)$ , of `sign.action(attr[i]-attr[j])^pow` if `dir` is "t-h" and of `sign.action(attr[j]-attr[i])^pow` if "h-t". That is, the argument `dir` determines which vertex's attribute is subtracted from which, with tail being the origin of a directed edge and head being its destination, and bipartite networks' edges being treated as going from the first part (b1) to the second (b2).

If `pow==0`, the exponentiation is replaced by the signum function: +1 if the difference is positive, 0 if there is no difference, and -1 if the difference is negative. Note that this function is applied after the `sign.action`. The comparison is exact, so when using calculated values of `attr`, ensure that values that you want to be considered equal are, in fact, equal.

### Usage

```
# binary: diff(attr, pow=1, dir="t-h", sign.action="identity")
```

```
# valued: diff(attr, pow=1, dir="t-h", sign.action="identity", form="sum")
```

**Arguments**

attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
pow	exponent for the node difference
dir	determines which vertex's attribute is subtracted from which. Accepts: "t-h" (the default), "tail-head", "b1-b2", "h-t", "head-tail", and "b2-b1".
sign.action	one of "identity", "abs", "posonly", "negonly". The following sign.actions are possible: <ul style="list-style-type: none"> <li>• "identity" (the default) no transformation of the difference regardless of sign</li> <li>• "abs" absolute value of the difference: equivalent to the absdiff term</li> <li>• "posonly" positive differences are kept, negative differences are replaced by 0</li> <li>• "negonly" negative differences are kept, positive differences are replaced by 0</li> </ul>
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i,j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

this term may not be meaningful for unipartite undirected networks unless `sign.action=="abs"`. When used on such a network, it behaves as if all edges were directed, going from the lower-indexed vertex to the higher-indexed vertex.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, directed, dyad-independent, frequently-used, quantitative nodal attribute, undirected, binary, valued

DiscUnif-ergmReference

*Discrete Uniform reference*

**Description**

Specifies each dyad's baseline distribution to be discrete uniform between a and b (both inclusive):  $h(y) = 1$ , with the support being a, a+1, ..., b-1, b.

**Usage**

```
# DiscUnif(a,b)
```

**Arguments**

a, b                    minimum and maximum to the baseline discrete uniform distribution, both inclusive. Both values must be finite.

**See Also**

[ergmReference](#) for index of reference distributions currently visible to the package.

**Keywords:** discrete, finite

---

dsp-ergmTerm

*Directed dyadwise shared partners*

---

**Description**

This term adds one network statistic to the model for each element in *d* where the *i* th such statistic equals the number of dyads in the network with exactly *d*[*i*] shared partners.

**Usage**

```
# binary: ddsp(d, type="OTP")
```

```
# binary: dsp(d, type="OTP")
```

**Arguments**

*d*                    a vector of distinct integers

*type*                A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

**Shared partner types**

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the *type* argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the relevant package):

- **Outgoing Two-path ("OTP"):** vertex *k* is an OTP shared partner of ordered pair (*i*, *j*) iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- **Incoming Two-path ("ITP"):** vertex *k* is an ITP shared partner of ordered pair (*i*, *j*) iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner".
- **Reciprocated Two-path ("RTP"):** vertex *k* is an RTP shared partner of ordered pair (*i*, *j*) iff  $i \leftrightarrow k \leftrightarrow j$ .
- **Outgoing Shared Partner ("OSP"):** vertex *k* is an OSP shared partner of ordered pair (*i*, *j*) iff  $i \rightarrow k, j \rightarrow k$ .

- Incoming Shared Partner ("ISP"): vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

### Note

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

This term can only be used with directed networks.

### References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

dyadcov-ergmTerm      *Dyadic covariate*

---

### Description

This term adds three statistics to the model, each equal to the sum of the covariate values for all dyads occupying one of the three possible non-empty dyad states (mutual, upper-triangular asymmetric, and lower-triangular asymmetric dyads, respectively), with the empty or null state serving as a reference category. If the network is undirected, `x` is either a matrix of edgewise covariates, or a network; if the latter, optional argument `attrname` provides the name of the edge attribute to use for edge values. This term adds one statistic to the model, equal to the sum of the covariate values for each edge appearing in the network. The `edgescov` and `dyadcov` terms are equivalent for undirected networks.

### Usage

```
# binary: dyadcov(x, attrname=NULL)
```

**Arguments**

`x`, `attrname` a specification for the dyadic covariate: either one of the following, or the name of a network attribute containing one of the following:

- a covariate matrix** with dimensions  $n \times n$  for unipartite networks and  $b \times (n - b)$  for bipartite networks; `attrname`, if given, is used to construct the term name.
- a network object** with the same size and bipartitedness as LHS; `attrname`, if given, provides the name of the quantitative edge attribute to use for covariate values (in this case, missing edges in `x` are assigned a covariate value of zero).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, quantitative dyadic attribute, undirected, binary

dyadnoise-ergmConstraint

*A soft constraint to adjust the sampled distribution for dyad-level noise with known perturbation probabilities*

**Description**

It is assumed that the observed LHS network is a noisy observation of some unobserved true network, with `p01` giving the dyadwise probability of erroneously observing a tie where the true network had a non-tie and `p10` giving the dyadwise probability of erroneously observing a nontie where the true network had a tie.

**Usage**

```
# dyadnoise(p01, p10)
```

**Arguments**

`p01`, `p10` can both be scalars or both be adjacency matrices of the same dimension as that of the LHS network giving these probabilities.

**Note**

See Karwa et al. (2017) for an application.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, soft, undirected

---

Dyads-ergmConstraint    *Constrain fixed or varying dyad-independent terms*

---

### Description

This is an "operator" constraint that takes one or two [ergmTerm](#) dyad-independent formulas. For the terms in the vary= formula, only those that change at least one of the terms will be allowed to vary, and all others will be fixed. If both formulas are given, the dyads that vary either for one or for the other will be allowed to vary. Note that a formula passed to Dyads without an argument name will default to fix=.

### Usage

```
# Dyads(fix=NULL, vary=NULL)
```

### Arguments

fix, vary            formula with only dyad-independent terms

### See Also

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, operator, undirected

---

ecoli                            *Two versions of an E. Coli network dataset*

---

### Description

This network data set comprises two versions of a biological network in which the nodes are operons in *Escherichia Coli* and a directed edge from one node to another indicates that the first encodes the transcription factor that regulates the second.

### Usage

```
data(ecoli)
```

### Details

The network object `ecoli1` is directed, with 423 nodes and 519 arcs. The object `ecoli2` is an undirected version of the same network, in which all arcs are treated as edges and the five isolated nodes (which exhibit only self-regulation in `ecoli1`) are removed, leaving 418 nodes.

## Licenses and Citation

When publishing results obtained using this data set, the original authors (Salgado et al. 2001; Shen-Orr et al. 2002) should be cited, along with this R package.

## Source

The data set is based on the RegulonDB network of Salgado et al. (2001) and was modified by Shen-Orr et al. (2002).

## References

Salgado H, Santos-Zavaleta A, Gama-Castro S, Millan-Zarate D, Diaz-Peredo E, Sanchez-Solano F, Perez-Rueda E, Bonavides-Martinez C, Collado-Vides J (2001). "RegulonDB (version 3.2): Transcriptional Regulation and Operon Organization in Escherichia coli K-12." *Nucleic Acids Research*, **29**(1), 72–74. doi:10.1093/nar/29.1.72.

Shen-Orr SS, Milo R, Mangan S, Alon U (2002). "Network Motifs in the Transcriptional Regulation Network of Escherichia coli." *Nature Genetics*, **31**(1), 64–68. doi:10.1038/ng881.

%Saul and Filkov (2007)

%Hummel et al (2010)

---

edg cov-ergmTerm	<i>Edge covariate</i>
------------------	-----------------------

---

## Description

This term adds one statistic to the model, equal to the sum of the covariate values for each edge appearing in the network. The edg cov term applies to both directed and undirected networks. For undirected networks the covariates are also assumed to be undirected. The edg cov and dyad cov terms are equivalent for undirected networks.

## Usage

```
# binary: edg cov(x, attrname=NULL)
# valued: edg cov(x, attrname=NULL, form="sum")
```

## Arguments

`x, attrname` a specification for the dyadic covariate: either one of the following, or the name of a network attribute containing one of the following:

- a covariate matrix** with dimensions  $n \times n$  for unipartite networks and  $b \times (n - b)$  for bipartite networks; `attrname`, if given, is used to construct the term name.

**a network object** with the same size and bipartitedness as LHS; `attrname`, if given, provides the name of the quantitative edge attribute to use for covariate values (in this case, missing edges in `x` are assigned a covariate value of zero).

**form** how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form  $\sum_{i,j} x_{i,j} y_{i,j}$ , where  $y_{i,j}$  is the value of `dyad(i,j)` and  $x_{i,j}$  is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See [ergmTerm](#) for more information.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, frequently-used, quantitative dyadic attribute, undirected, binary, valued

edges-ergmConstraint *Preserve the edge count of the given network*

### Description

Only networks having the same number of edges as the network passed in the model formula have non-zero probability.

### Usage

# edges

### See Also

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** None

edges-ergmTerm *Number of edges in the network*

### Description

This term adds one network statistic equal to the number of edges (i.e. nonzero values) in the network. For undirected networks, `edges` is equal to `kstar(1)`; for directed networks, `edges` is equal to both `ostar(1)` and `istar(1)`.

**Usage**

```
# binary: edges
# valued: nonzero
# valued: edges
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, binary, valued

---

egocentric-ergmConstraint

*Preserve values of dyads incident on vertices with given attribute*

---

**Description**

Preserve values of dyads incident on vertices with attribute `attr` being TRUE or if `attrname` is NULL, the vertex attribute "na" being FALSE.

**Usage**

```
# egocentric(attr=NULL, direction="both")
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>direction</code>	one of "both", "out" and "in", only applies to directed networks. "out" only preserves the out-dyads of those actors and "in" preserves their in-dyads.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

```
enformulate.curved-deprecated
```

*Convert a curved ERGM into a form suitable as initial values for the same ergm. Deprecated in 4.0.0.*

---

## Description

The generic `enformulate.curved` converts an `ergm` object or formula of a model with curved terms to the variant in which the curved parameters embedded into the formula and are removed from the parameter vector. This is the form that used to be required by `ergm()` calls.

## Usage

```
enformulate.curved(object, ...)

## S3 method for class 'ergm'
enformulate.curved(object, ...)

## S3 method for class 'formula'
enformulate.curved(object, theta, ...)
```

## Arguments

<code>object</code>	An <code>ergm</code> object or an ERGM formula. The curved terms of the given formula (or the formula used in the fit) must have all of their arguments passed by name.
<code>...</code>	Unused at this time.
<code>theta</code>	Curved model parameter configuration.

## Details

Because of a current kludge in `ergm()`, output from one run cannot be directly passed as initial values (`control.ergm(init=)`) for the next run if any of the terms are curved. One workaround is to embed the curved parameters into the formula (while keeping `fixed=FALSE`) and remove them from `control.ergm(init=)`.

This function automates this process for curved ERGM terms included with the `ergm` package. It does not work with curved terms not included in `ergm`.

## Value

A list with the following components:

<code>formula</code>	The formula with curved parameter estimates incorporated.
<code>theta</code>	The coefficient vector with curved parameter estimates removed.

## See Also

`ergm()`, `simulate.ergm()`

---

equalto-ergmTerm	<i>Number of dyads with values equal to a specific value (within tolerance)</i>
------------------	---

---

### Description

Adds one statistic equal to the number of dyads whose values are within tolerance of value , i.e., between value-tolerance and value+tolerance , inclusive.

### Usage

```
# valued: equalto(value=0, tolerance=0)
```

### Arguments

value	numerical threshold
tolerance	numerical threshold

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

ergm

*Exponential-Family Random Graph Models*

---

### Description

`ergm()` is used to fit exponential-family random graph models (ERGMs), in which the probability of a given network,  $y$ , on a set of nodes is  $h(y) \exp\{\eta(\theta) \cdot g(y)\} / c(\theta)$ , where  $h(y)$  is the reference measure (usually  $h(y) = 1$ ),  $g(y)$  is a vector of network statistics for  $y$ ,  $\eta(\theta)$  is a natural parameter vector of the same length (with  $\eta(\theta) = \theta$  for most terms), and  $c(\theta)$  is the normalizing constant for the distribution. `ergm()` can return a maximum pseudo-likelihood estimate, an approximate maximum likelihood estimate based on a Monte Carlo scheme, or an approximate contrastive divergence estimate based on a similar scheme. (For an overview of the package **ergm**, see Hunter et al. (2008) and Krivitsky et al. (2023).)

**Usage**

```

ergm(
  formula,
  response = NULL,
  reference = ~Bernoulli,
  constraints = ~.,
  obs.constraints = ~. - observed,
  offset.coef = NULL,
  target.stats = NULL,
  eval.loglik = getOption("ergm.eval.loglik"),
  estimate = c("MLE", "MPLE", "CD"),
  control = control.ergm(),
  verbose = FALSE,
  ...,
  basis = ergm.getnetwork(formula),
  newnetwork = c("one", "all", "none")
)

is.ergm(object)

## S3 method for class 'ergm'
is.na(x)

## S3 method for class 'ergm'
anyNA(x, ...)

## S3 method for class 'ergm'
nobs(object, ...)

## S3 method for class 'ergm'
alias(object, ...)

## S3 method for class 'ergm'
print(x, digits = max(3, getOption("digits") - 3), ...)

## S3 method for class 'ergm'
vcov(object, sources = c("all", "model", "estimation"), ...)

```

**Arguments**

**formula** An R *formula*, of the form  $y \sim \langle \text{model terms} \rangle$ , where  $y$  is a [network](#) object or a matrix that can be coerced to a [network](#) object. For the details on the possible  $\langle \text{model terms} \rangle$ , see [ergmTerm](#) and (Morris et al. 2008) for binary ERGM terms and (Krivitsky 2012) for valued ERGM terms (terms for weighted edges). To create a [network](#) object in R, use the `network()` function, then add nodal attributes to it using the `%v%` operator if necessary. Enclosing a model term in `offset()` fixes its value to one specified in `offset.coef`. (A second argument—a logical or numeric index vector—can be used to select *which* of

	the parameters within the term are offsets.)
response	<p>Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows:</p> <p>NULL Model simple presence or absence, via a binary ERGM.</p> <p><b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <code>logical</code> (TRUE/FALSE) for binary or <code>numeric</code> for valued.</p> <p><b>a formula</b> must be of the form <code>NAME~EXPR TYPE</code> (with <code> </code> being literal). <code>EXPR</code> is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional <code>NAME</code> specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of <code>EXPR</code>. Normally, the type of ERGM is determined by whether the result of evaluating <code>EXPR</code> is logical or numeric, but the optional <code>TYPE</code> can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).</p>
reference	A one-sided formula specifying the reference measure ( $h(y)$ ) to be used. See help for <a href="#">ERGM reference measures</a> implemented in the <code>ergm</code> package.
constraints	<p>A formula specifying one or more constraints on the support of the distribution of the networks being modeled. Multiple constraints may be given, separated by "+" and "-" operators. See <a href="#">ergmConstraint</a> for the detailed explanation of their semantics and also for an indexed list of the constraints visible to the <code>ergm</code> package.</p> <p>The default is to have no constraints except those provided through the <a href="#">ergmlhs</a> API.</p> <p>Together with the model terms in the formula and the reference measure, the constraints define the distribution of networks being modeled.</p> <p>It is also possible to specify a proposal function directly either by passing a string with the function's name (in which case, arguments to the proposal should be specified through the <code>MCMC.prop.args</code> argument to the relevant control function, or by giving it on the LHS of the hints formula to <code>MCMC.prop</code> argument to the control function. This will override the one chosen automatically.</p> <p>Note that not all possible combinations of constraints and reference measures are supported. However, for relatively simple constraints (i.e., those that simply permit or forbid specific dyads or sets of dyads from changing), arbitrary combinations should be possible.</p>
obs.constraints	<p>A one-sided formula specifying one or more constraints or other modification <i>in addition</i> to those specified by constraints, following the same syntax as the constraints argument.</p> <p>This allows the domain of the integral in the numerator of the partially observed network face-value likelihoods of (Handcock and Gile 2010) and (Karwa et al. 2017) to be specified explicitly.</p> <p>The default is to constrain the integral to only integrate over the missing dyads (if present), after incorporating constraints provided through the <a href="#">ergmlhs</a> API.</p> <p>It is also possible to specify a proposal function directly by passing a string with the function's name of the <code>obs.MCMC.prop</code> argument to the relevant control</p>

	function. In that case, arguments to the proposal should be specified through the <code>obs.prop.args</code> argument to the relevant control function.
<code>offset.coef</code>	A vector of coefficients for the offset terms. Note that <code>NaN</code> elements are treated specially. See <code>Skipping</code> below. If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
<code>target.stats</code>	vector of "observed network statistics," if these statistics are for some reason different than the actual statistics of the network on the left-hand side of formula. Equivalently, this vector is the mean-value parameter values for the model. If this is given, the algorithm finds the natural parameter values corresponding to these mean-value parameters. If <code>NULL</code> , the mean-value parameters used are the observed statistics of the network in the formula. If the vector is named, its names will be matched to the corresponding statistic names, and if the named vector has a single coefficient without a name, it will be used for the unmatched statistics. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
<code>eval.loglik</code>	Logical: For dyad-dependent models, if <code>TRUE</code> , use bridge sampling to evaluate the log-likelihood associated with the fit. Has no effect for dyad-independent models. Since bridge sampling takes additional time, setting to <code>FALSE</code> may speed performance if likelihood values (and likelihood-based values like AIC and BIC) are not needed. Can be set globally via <code>option(ergm.eval.loglik=...)</code> , which is set to <code>TRUE</code> when the package is loaded. (See <code>options?ergm</code> .)
<code>estimate</code>	If "MPLE," then the maximum pseudolikelihood estimator is returned. If "MLE" (the default), then an approximate maximum likelihood estimator is returned. For certain models, the MPLE and MLE are equivalent, in which case this argument is ignored. (To force MCMC-based approximate likelihood calculation even when the MLE and MPLE are the same, see the <code>force.main</code> argument of <code>control.ergm()</code> . If "CD" ( <i>EXPERIMENTAL</i> ), the Monte-Carlo contrastive divergence estimate is returned. )
<code>control</code>	A list of control parameters for algorithm tuning, typically constructed with <code>control.ergm()</code> . Its documentation gives the the list of recognized control parameters and their meaning. The more generic utility <code>snctrl()</code> (StatNet CONTRoL) also provides argument completion for the available control functions and limited argument name checking.
<code>verbose</code>	A logical or an integer to control the amount of progress and diagnostic information to be printed. <code>FALSE/0</code> produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
<code>...</code>	Additional arguments, to be passed to lower-level functions.
<code>basis</code>	a value (usually a <code>network</code> ) to override the LHS of the formula.
<code>newnetwork</code>	One of "one" (the default), "all", or "none" (or, equivalently, <code>FALSE</code> ), specifying whether the network(s) from the last iteration of the MCMC sampling should be returned as a part of the fit as a elements <code>newnetwork</code> and <code>newnetworks</code> . (See their entries in section <code>Value</code> below for details.) Partial matching is supported.
<code>object</code>	an <code>ergm</code> object.

<code>x, digits</code>	See <code>print()</code> .
<code>sources</code>	For the <code>vcov</code> method, specify whether to return the covariance matrix from the ERGM model, the estimation process, or both combined.

### Value

`ergm()` returns an object of `ergm` that is a list consisting of the following elements:

<code>coef</code>	The Monte Carlo maximum likelihood estimate of $\theta$ , the vector of coefficients for the model parameters.
<code>sample</code>	The $n \times p$ matrix of network statistics, where $n$ is the sample size and $p$ is the number of network statistics specified in the model, generated by the last iteration of the MCMC-based likelihood maximization routine. These statistics are centered with respect to the observed statistics or <code>target.stats</code> , unless missing data MLE is used.
<code>sample.obs</code>	As <code>sample</code> , but for the constrained sample.
<code>iterations</code>	The number of Newton-Raphson iterations required before convergence.
<code>MCMCtheta</code>	The value of $\theta$ used to produce the Markov chain Monte Carlo sample. As long as the Markov chain mixes sufficiently well, <code>sample</code> is roughly a random sample from the distribution of network statistics specified by the model with the parameter equal to <code>MCMCtheta</code> . If <code>estimate="MPLE"</code> then <code>MCMCtheta</code> equals the MPLE.
<code>loglikelihood</code>	The approximate change in log-likelihood in the last iteration. The value is only approximate because it is estimated based on the MCMC random sample.
<code>gradient</code>	The value of the gradient vector of the approximated loglikelihood function, evaluated at the maximizer. This vector should be very close to zero.
<code>covar</code>	Approximate covariance matrix for the MLE, based on the inverse Hessian of the approximated loglikelihood evaluated at the maximizer.
<code>failure</code>	Logical: Did the MCMC estimation fail?
<code>network</code>	Network passed on the left-hand side of <code>formula</code> . If <code>target.stats</code> are passed, it is replaced by the network returned by <code>san()</code> .
<code>newnetworks</code>	If argument <code>newnetwork</code> is "all", a list of the final networks at the end of the MCMC simulation, one for each thread.
<code>newnetwork</code>	If argument <code>newnetwork</code> is "one" or "all", the first (possibly only) element of <code>newnetworks</code> .
<code>coef.init</code>	The initial value of $\theta$ .
<code>est.cov</code>	The covariance matrix of the model statistics in the final MCMC sample.
<code>coef.hist, steplen.hist, stats.hist, stats.obs.hist</code>	For the MCMLE method, the history of coefficients, Hummel step lengths, and average model statistics for each iteration..
<code>control</code>	The control list passed to the call.
<code>etamap</code>	The set of functions mapping the true parameter $\theta$ to the canonical parameter $\eta$ (irrelevant except in a curved exponential family model)
<code>formula</code>	The original <code>formula</code> passed to <code>ergm()</code> .

target.stats	The target.stats used during estimation (passed through from the Arguments)
target.esteq	Used for curved models to preserve the target mean values of the curved terms. It is identical to target.stats for non-curved models.
constraints	Constraints used during estimation (passed through from the Arguments)
reference	The reference measure used during estimation (passed through from the Arguments)
estimate	The estimation method used (passed through from the Arguments).
offset	vector of logical telling which model parameters are to be set at a fixed value (i.e., not estimated).
drop	If <code>control\$drop=TRUE</code> , a numeric vector indicating which terms were dropped due to extreme values of the corresponding statistics on the observed network, and how: $\emptyset$ The term was not dropped. -1 The term was at its minimum and the coefficient was fixed at $-\text{Inf}$ . +1 The term was at its maximum and the coefficient was fixed at $+\text{Inf}$ .
estimable	A logical vector indicating which terms could not be estimated due to a constraints constraint fixing that term at a constant value.
info	A list with miscellaneous information that would typically be accessed by the user via methods; in general, it should not be accessed directly. Current elements include: terms_dind Logical indicator of whether the model terms are all dyad-independent. space_dind Logical indicator of whether the sample space (constraints) are all dyad-independent. n_info_dyads Number of “informative” dyads: those that are observed (not missing) <i>and</i> not constrained by sample space constraints; one of the measures of sample size. obs Logical indicator of whether an observational (missing data) process was involved in estimation. valued Logical indicator of whether the model is valued.
null.lik	Log-likelihood of the null model. Valid only for unconstrained models.
mle.lik	The approximate log-likelihood for the MLE. The value is only approximate because it is estimated based on the MCMC random sample.

### Methods (by generic)

- `is.na(ergm)`: Return TRUE if the ERGM was fit to a partially observed network and/or an observational process, such as missing (NA) dyads.
- `anyNA(ergm)`: Alias to the `is.na()` method.
- `nobs(ergm)`: Return the number of informative dyads of a model fit.
- `alias(ergm)`: Extract a matrix of detected linear dependence among the model’s sufficient statistics or estimating functions (if curved). Each row, if any, contains coefficients for a linear combination of the statistics that results in a constant. These are pretty-printed as a series of equations.
- `print(ergm)`: Print the call, the estimate, and the method used to obtain it.
- `vcov(ergm)`: extracts the variance-covariance matrix of parameter estimates.

### Skipping MCMC iterations (advanced)

In some scenarios, it is helpful to forbid certain network configurations from being sampled this can be specified using `constraints`, or by creating an `offset()` term which has value 0 if the network is allowed and positive (negative) if the network is not, with offset coefficient set to `-Inf` (`+Inf`). Sometimes, however, a permitted configuration can be reached by "passing through" a forbidden one. For example, if isolates are possible but not nodes with degree exactly 1. Then, an offset term with coefficient `NaN` (not `NA`!) will cause the MCMC to not terminate as long as the value of that offset term is different from 0.

Note that this means that MCMC is not guaranteed to terminate, and there are very few safeguards at this time.

### Notes on model specification

Although each of the statistics in a given model is a summary statistic for the entire network, it is rarely necessary to calculate statistics for an entire network in a proposed Metropolis-Hastings step. Thus, for example, if the triangle term is included in the model, a census of all triangles in the observed network is never taken; instead, only the change in the number of triangles is recorded for each edge toggle.

In the implementation of `ergm()`, the model is initialized in R, then all the model information is passed to a C program that generates the sample of network statistics using MCMC. This sample is then returned to R, which then uses one of several algorithms, selected by `main.method=control.ergm()` parameter to update the estimate.

The mechanism for proposing new networks for the MCMC sampling scheme, which is a Metropolis-Hastings algorithm, depends on two things: The `constraints`, which define the set of possible networks that could be proposed in a particular Markov chain step, and the weights placed on these possible steps by the proposal distribution. The former may be controlled using the `constraints` argument described above. The latter may be controlled using the `prop.weights` argument to the `control.ergm()` function.

The package is designed so that the user could conceivably add additional proposal types.

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**See Also**

`network`, `%v%`, `%n%`, `ergmTerm`, `ergmMPLE`, `summary.ergm()`

**Examples**

```
#
# load the Florentine marriage data matrix
#
data(flo)
#
# attach the sociomatrix for the Florentine marriage data
# This is not yet a network object.
#
flo
#
# Create a network object out of the adjacency matrix
#
flomarriage <- network(flo,directed=FALSE)
flomarriage
#
# print out the sociomatrix for the Florentine marriage data
#
flomarriage[,]
#
# create a vector indicating the wealth of each family (in thousands of lira)
# and add it as a covariate to the network object
#
flomarriage %v% "wealth" <- c(10,36,27,146,55,44,20,8,42,103,48,49,10,48,32,3)
flomarriage
#
# create a plot of the social network
#
plot(flomarriage)
#
# now make the vertex size proportional to their wealth
#
plot(flomarriage, vertex.cex=flomarriage %v% "wealth" / 20, main="Marriage Ties")
#
# Use 'data(package = "ergm")' to list the data sets in a
#
data(package="ergm")
#
# Load a network object of the Florentine data
#
data(florentine)
#
# Fit a model where the propensity to form ties between
# families depends on the absolute difference in wealth
#
gest <- ergm(flomarriage ~ edges + absdiff("wealth"))
summary(gest)
#
```

```

# add terms for the propensity to form 2-stars and triangles
# of families
#
gest <- ergm(flomarriage ~ kstar(1:2) + absdiff("wealth") + triangle)
summary(gest)

# import synthetic network that looks like a molecule
data(molecule)
# Add a attribute to it to mimic the atomic type
molecule %v% "atomic type" <- c(1,1,1,1,1,1,2,2,2,2,2,2,3,3,3,3,3,3,3)
#
# create a plot of the social network
# colored by atomic type
#
plot(molecule, vertex.col="atomic type",vertex.cex=3)

# measure tendency to match within each atomic type
gest <- ergm(molecule ~ edges + kstar(2) + triangle + nodematch("atomic type"))
summary(gest)

# compare it to differential homophily by atomic type
gest <- ergm(molecule ~ edges + kstar(2) + triangle
             + nodematch("atomic type",diff=TRUE))
summary(gest)

# Extract parameter estimates as a numeric vector:
coef(gest)
# Sources of variation in parameter estimates:
vcov(gest, sources="model")
vcov(gest, sources="estimation")
vcov(gest, sources="all") # the default

```

---

ergm-options

*Global options and term options for the ergm package*


---

## Description

Options set via the built-in `options()` functions that affect ergm estimation and options that control the behavior of some terms.

## Global options and defaults

**ergm.eval.loglik = TRUE** Whether `ergm()` and similar functions will evaluate the likelihood of the fitted model. Can be overridden for a specific call by passing `eval.loglik` argument directly.

**ergm.loglik.warn\_dyads = TRUE** Whether log-likelihood evaluation should issue a warning when the effective number of dyads that can vary in the sample space is poorly defined, such as if the degree sequence is constrained.

`ergm.cluster.retries = 5` **ergm**'s parallel routines implement rudimentary fault-tolerance. This option controls the number of retries for a cluster call before giving up.

`ergm.warn_loops = TRUE` Whether to issue a warning if the network contains self-loops.

`ergm.term = list()` The default term options below.

`ergm.ABI.action = "stop"` What to do when **ergm** detects that one of its extension packages had been compiled with a different version of **ergm** from the current one that makes changes at the C level that can cause problems. Other choices include

"stop", "abort" stop with an error

"warning" warn and proceed

"message", "inform" print a message and proceed

"silent" return the value without side-effects

"disable" skip the check, always returning TRUE

Partial matching is supported.

## Term options

Term options can be set in three places, in the order of precedence from high to low:

1. As a term argument (not always). For example, `gw.cutoff` below can be set in a `gwesp` term by `gwesp(..., cutoff=X)`.
2. For functions such as `summary` that take `ergm` formulas but do not take a control list, the named arguments passed in as `...`. E.g., `summary(nw~gwesp(.5, fix=TRUE), gw.cutoff=60)` will evaluate the GWESP statistic with its cutoff set to 60.
3. As an element in a `term.options = list` passed via a control function such as `control.ergm()` or, for functions that do not, in a list with that argument name. E.g., `summary(nw~gwesp(.5, fix=TRUE), term.options=list(gw.cutoff=60))` has the same effect.
4. As an element in a global option list `ergm.term` above.

The following options are in use by terms in the `ergm` package:

`version` A string that can be interpreted as an R package version. If set, the term will attempt to emulate its behavior as it was that version of `ergm`. Not all past version behaviors are available.

`gw.cutoff` In geometrically weighted terms (`gwesp`, `gwdegree`, etc.) the highest number of shared partners, degrees, etc. for which to compute the statistic. This usually defaults to 30.

`cache.sp` Whether the `gwesp`, `dgwesp`, and similar terms need should use a cache for the dyad-wise number of shared partners. This usually improves performance significantly at a modest memory cost, and therefore defaults to TRUE, but it can be disabled.

`interact.dependent` Whether to allow and how to handle the user attempting to interact dyad-dependent terms (e.g., `absdiff("age"):triangles` or `absdiff("age")*triangles` as opposed to `absdiff("age"):nodefactor("sex")`). Possible values are "error" (the default), "message", and "warning", for their respective actions, and "silent" for simply processing the term.

**Description**

Using clusters multiple CPUs or CPU cores to speed up ERGM estimation and simulation.

The `ergm.getCluster` function is usually called internally by the `ergm` process (in `ergm_MCMC_sample()`) and will attempt to start the appropriate type of cluster indicated by the `control.ergm()` settings. It will also check that the same version of `ergm` is installed on each node.

The `ergm.stopCluster` shuts down a cluster, but only if `ergm.getCluster` was responsible for starting it.

The `ergm.restartCluster` restarts and returns a cluster, but only if `ergm.getCluster` was responsible for starting it.

`nthreads` is a simple generic to obtain the number of parallel processes represented by its argument, keeping in mind that having no cluster (e.g., `NULL`) represents one thread.

**Usage**

```
ergm.getCluster(control = NULL, verbose = FALSE, stop_on_exit = parent.frame())
```

```
ergm.stopCluster(..., verbose = FALSE)
```

```
ergm.restartCluster(control = NULL, verbose = FALSE)
```

```
set.MT_terms(n)
```

```
get.MT_terms()
```

```
nthreads(clinfo = NULL, ...)
```

```
## S3 method for class 'cluster'
```

```
nthreads(clinfo = NULL, ...)
```

```
## S3 method for class '`NULL`'
```

```
nthreads(clinfo = NULL, ...)
```

```
## S3 method for class 'control.list'
```

```
nthreads(clinfo = NULL, ...)
```

**Arguments**

`control` a `control.ergm()` (or similar) list of parameter values from which the parallel settings should be read; can also be `NULL`, in which case an existing cluster is used if started, or no cluster otherwise.

verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
stop_on_exit	An <code>environment</code> or NULL. If an environment, defaulting to that of the calling function, the cluster will be stopped when the calling the frame in question exits.
...	not currently used
n	an integer specifying the number of threads to use; 0 (the starting value) disables multithreading, and -1 or NA sets it to the number of CPUs detected.
clinfo	a <code>cluster</code> or another object.

## Details

For estimation that require MCMC, `ergm` can take advantage of multiple CPUs or CPU cores on the system on which it runs, as well as computing clusters through one of two mechanisms:

**Running MCMC chains in parallel** Packages `parallel` and `snow` are used to to facilitate this, all cluster types that they support are supported.

The number of nodes used and the `parallel` API are controlled using the `parallel` and `parallel.type` arguments passed to the control functions, such as `control.ergm()`.

The `ergm.getCluster()` function is usually called internally by the `ergm` process (in `ergm_MCMC_sample()`) and will attempt to start the appropriate type of cluster indicated by the `control.ergm()` settings. The `ergm.stopCluster()` is helpful if the user has directly created a cluster.

Further details on the various cluster types are included below.

**Multithreaded evaluation of model terms** Rather than running multiple MCMC chains, it is possible to attempt to accelerate sampling by evaluating qualified terms' change statistics in multiple threads run in parallel. This is done using the `OpenMP` API.

However, this introduces a nontrivial amount of computational overhead. See below for a list of the major factors affecting whether it is worthwhile.

Generally, the two approaches should not be used at the same time without caution. In particular, by default, cluster slave nodes will not “inherit” the multithreading setting; but `parallel.inherit.MT=` control parameter can override that. Their relative advantages and disadvantages are as follows:

- Multithreading terms cannot take advantage of clusters but only of CPUs and cores.
- Parallel MCMC chains produce several independent chains; multithreading still only produces one.
- Multithreading terms actually accelerates sampling, including the burn-in phase; parallel MCMC's multiple burn-in runs are effectively “wasted”.

## Value

`set.MT_terms()` returns the previous setting, invisibly.

`get.MT_terms()` returns the current setting.

### Different types of clusters

**PSOCK clusters** The `parallel` package is used with PSOCK clusters by default, to utilize multiple cores on a system. The number of cores on a system can be determined with the `detectCores()` function.

This method works with the base installation of R on all platforms, and does not require additional software.

For more advanced applications, such as clusters that span multiple machines on a network, the clusters can be initialized manually, and passed into `ergm()` and others using the `parallel` control argument. See the second example below.

**MPI clusters** To use MPI to accelerate ERGM sampling, pass the control parameter `parallel.type="MPI"`. `ergm` requires the `snow` and `Rmpi` packages to communicate with an MPI cluster.

Using MPI clusters requires the system to have an existing MPI installation. See the MPI documentation for your particular platform for instructions.

To use `ergm()` across multiple machines in a high performance computing environment, see the section "User initiated clusters" below.

**User initiated clusters** A cluster can be passed into `ergm()` with the `parallel` control parameter. `ergm()` will detect the number of nodes in the cluster, and use all of them for MCMC sampling. This method is flexible: it will accept any cluster type that is compatible with `snow` or `parallel` packages.

### When is multithreading terms worthwhile?

- The more terms with statistics the model has, the more benefit from parallel execution.
- The more expensive the terms in the model are, the more benefit from parallel execution. For example, models with terms like `gwdsp` will generally get more benefit than models where all terms are dyad-independent.
- Sampling more dense networks will generally get more benefit than sparse networks. Network size has little, if any, effect.
- More CPUs/cores usually give greater speed-up, but only up to a point, because the amount of overhead grows with the number of threads; it is often better to "batch" the terms into a smaller number of threads than possible.
- Any other workload on the system will have a more severe effect on multithreaded execution. In particular, do not run more threads than CPUs/cores that you want to allocate to the tasks.
- Under Windows, even compiling with OpenMP appears to introduce unacceptable amounts of overhead, so it is disabled for Windows at compile time. To enable, `delete src/Makevars.win` and recompile from scratch.

### Note

This is a setting global to the `ergm` package and all of its C functions, including when called from other packages via the Linking-To mechanism.

### Examples

```
# Uses 2 SOCK clusters for MCMLE estimation
```

```

data(faux.mesa.high)
nw <- faux.mesa.high
fauxmodel.01 <- ergm(nw ~ edges + isolates + gwesp(0.2, fixed=TRUE),
                    control=control.ergm(parallel=2, parallel.type="PSOCK"))
summary(fauxmodel.01)

```

---

<code>ergm.allstats</code>	<i>Calculate all possible vectors of statistics on a network for an ERGM</i>
----------------------------	--

---

### Description

`ergm.allstats` calculates the sufficient statistics of an ERGM over the network's sample space. `ergm.exact()` uses `ergm.allstats()` to calculate the exact loglikelihood, evaluated at `eta`.

### Usage

```

ergm.allstats(formula, constraints = ~., zeroobs = TRUE, force = FALSE, ...)
ergm.exact(eta, formula, constraints = ~., statmat = NULL, weights = NULL, ...)

```

### Arguments

<code>formula, constraints</code>	An ERGM formula and (optionally) a constraint specification formulas. See <a href="#">ergm()</a> . This function supports only dyad-independent constraints.
<code>zeroobs</code>	Logical: Should the vectors be centered so that the network passed in the formula has the zero vector as its statistics?
<code>force</code>	Logical: Should the algorithm be run even if it is determined that the problem may be very large, thus bypassing the warning message that normally terminates the function in such cases?
<code>...</code>	further arguments, passed to <a href="#">ergm_model()</a> .
<code>eta</code>	vector of canonical parameter values at which the loglikelihood should be evaluated.
<code>statmat, weights</code>	outputs from <code>ergm.allstats()</code> : if passed, used in lieu of running it.

### Details

The mechanism for doing this is a recursive algorithm, where the number of levels of recursion is equal to the number of possible dyads that can be changed from 0 to 1 and back again. The algorithm starts with the network passed in `formula`, then recursively toggles each edge twice so that every possible network is visited.

`ergm.allstats()` and `ergm.exact()` should only be used for small networks, since the number of possible networks grows extremely fast with the number of nodes. An error results if it is used on a network with more than 31 free dyads, which corresponds to a directed network of more than 6 nodes or an undirected network of more than 8 nodes; use `force=TRUE` to override this error.

In case `ergm.exact()` is to be called repeatedly, for instance by an optimization routine, it is preferable to call `ergm.allstats()` first, then pass `statmat` and `weights` explicitly to avoid repeatedly calculating these objects.

## Value

`ergm.allstats()` returns a list object with these two elements:

<code>weights</code>	integer of counts, one for each row of <code>statmat</code> telling how many networks share the corresponding vector of statistics.
<code>statmat</code>	matrix in which each row is a unique vector of statistics.

`ergm.exact()` returns the exact value of the loglikelihood, evaluated at `eta`.

## Examples

```
# Count by brute force all the edge statistics possible for a 7-node
# undirected network
mynw <- network.initialize(7, dir = FALSE)
system.time(a <- ergm.allstats(mynw~edges))

# Summarize results
rbind(t(a$statmat), .freq. = a$weights)

# Each value of a$weights is equal to 21-choose-k,
# where k is the corresponding statistic (and 21 is
# the number of dyads in an 7-node undirected network).
# Here's a check of that fact:
as.vector(a$weights - choose(21, t(a$statmat)))

# Dyad-independent constraints are also supported:
system.time(a <- ergm.allstats(mynw~edges, constraints = ~fixallbut(cbind(1:2,2:3))))
rbind(t(a$statmat), .freq. = a$weights)

# Simple ergm.exact output for this network.
# We know that the loglikelihood for my empty 7-node network
# should simply be -21*log(1+exp(eta)), so we may check that
# the following two values agree:
-21*log(1+exp(.1234))
ergm.exact(.1234, mynw~edges, statmat=a$statmat, weights=a$weights)
```

---

ergm.bridge.llr	<i>Bridge sampling to evaluate ERGM log-likelihoods and log-likelihood ratios</i>
-----------------	---

---

## Description

ergm.bridge.llr uses bridge sampling with geometric spacing to estimate the difference between the log-likelihoods of two parameter vectors for an ERGM via repeated calls to `simulate.formula.ergm()`.

ergm.bridge.0.llk is a convenience wrapper that returns the log-likelihood of configuration  $\theta$  relative to the reference measure. That is, the configuration with  $\theta = 0$  is defined as having log-likelihood of 0.

ergm.bridge.dindstart.llk is a wrapper that uses a dyad-independent ERGM as a starting point for bridge sampling to estimate the log-likelihood for a given dyad-dependent model and parameter configuration. Note that it only handles binary ERGMs (`response=NULL`) and with constraints (`constraints=`) that do not induce dyadic dependence.

## Usage

```
ergm.bridge.llr(
  object,
  response = NULL,
  reference = ~Bernoulli,
  constraints = ~.,
  from,
  to,
  obs.constraints = ~. - observed,
  target.stats = NULL,
  basis = ergm.getnetwork(object),
  verbose = FALSE,
  ...,
  llronly = FALSE,
  control = control.ergm.bridge()
)
```

```
ergm.bridge.0.llk(
  object,
  response = NULL,
  reference = ~Bernoulli,
  coef,
  ...,
  llkonly = TRUE,
  control = control.ergm.bridge(),
  basis = ergm.getnetwork(object)
)
```

```
ergm.bridge.dindstart.llk(
```

```

object,
response = NULL,
constraints = ~.,
coef,
obs.constraints = ~. - observed,
target.stats = NULL,
dind = NULL,
coef.dind = NULL,
basis = ergm.getnetwork(object),
...,
llkonly = TRUE,
control = control.ergm.bridge(),
verbose = FALSE
)

```

## Arguments

object	A model formula. See <a href="#">ergm()</a> for details.
response	<p>Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows:</p> <p>NULL Model simple presence or absence, via a binary ERGM.</p> <p><b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <a href="#">logical</a> (TRUE/FALSE) for binary or <a href="#">numeric</a> for valued.</p> <p><b>a formula</b> must be of the form NAME~EXPR TYPE (with   being literal). EXPR is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional NAME specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of EXPR. Normally, the type of ERGM is determined by whether the result of evaluating EXPR is logical or numeric, but the optional TYPE can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).</p>
reference	A one-sided formula specifying the reference measure ( $h(y)$ ) to be used. (Defaults to <code>~Bernoulli</code> .)
constraints, obs.constraints	One-sided formulas specifying one or more constraints on the support of the distribution of the networks being simulated and on the observation process respectively. See the documentation for similar arguments for <a href="#">ergm()</a> for more information.
from, to	The initial and final parameter vectors.
target.stats	A vector of sufficient statistics to be used in place of those of the network in the formula. If the vector is named, its names will be matched to the corresponding statistic names, and if the named vector has a single coefficient without a name, it will be used for the unmatched statistics. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
basis	An optional <a href="#">network</a> object to start the Markov chain. If omitted, the default is the left-hand-side of the object.

verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
...	Further arguments to <code>ergm.bridge.llr</code> and <code>simulate.formula.ergm()</code> .
llronly	Logical: If TRUE, only the estimated log-ratio will be returned by <code>ergm.bridge.llr</code> .
control	A list of control parameters for algorithm tuning, typically constructed with <code>control.ergm.bridge()</code> . Its documentation gives the the list of recognized control parameters and their meaning. The more generic utility <code>snctrl()</code> (StatNet ConTRoL) also provides argument completion for the available control functions and limited argument name checking.
coef	A vector of coefficients for the configuration of interest. If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
llkonly	Whether only the estimated log-likelihood should be returned by the <code>ergm.bridge.0.llk</code> and <code>ergm.bridge.dindstart.llk</code> . (Defaults to TRUE.)
dind	A one-sided formula with the dyad-independent model to use as a starting point. Defaults to the dyad-independent terms found in the formula object with an overall density term (edges) added if not redundant.
coef.dind	Parameter configuration for the dyad-independent starting point. Defaults to the MLE of <code>dind</code> . If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .

### Value

If `llronly=TRUE` or `llkonly=TRUE`, these functions return the scalar log-likelihood-ratio or the log-likelihood. Otherwise, they return a list with the following components:

llr	The estimated log-ratio.
llr.vcov	The estimated variance of the log-ratio due to MCMC approximation.
llrs	A list of lists (1 per attempt) of the estimated log-ratios for each of the <code>bridge.nsteps</code> bridges.
llrs.vcov	A list of lists (1 per attempt) of the estimated variances of the estimated log-ratios for each of the <code>bridge.nsteps</code> bridges.
paths	A list of lists (1 per attempt) with two elements: <code>theta</code> , a numeric matrix with <code>bridge.nsteps</code> rows, with each row being the respective bridge's parameter configuration; and <code>weight</code> , a vector of length <code>bridge.nsteps</code> containing its weight.
Dtheta.Du	The gradient vector of the parameter values with respect to position of the bridge.

ergm.bridge.0.llk result list also includes an llk element, with the log-likelihood itself (with the reference distribution assumed to have likelihood 0).

ergm.bridge.dindstart.llk result list also includes an llk element, with the log-likelihood itself and an llk.dind element, with the log-likelihood of the nearest dyad-independent model.

## References

Hunter DR, Handcock MS (2006). “Inference in Curved Exponential Family Models for Networks.” *Journal of Computational and Graphical Statistics*, **15**(3), 565–583. ISSN 1061-8600. doi:[10.1198/106186006X133069](https://doi.org/10.1198/106186006X133069).

## See Also

[simulate.formula.ergm\(\)](#)

---

ergm.design

*Obtain the set of informative dyads based on the network structure.*

---

## Description

Note that this function is not recommended for general use, since it only supports only one way of specifying observational structure—through NA edges. It is likely to be deprecated in the future.

## Usage

```
ergm.design(nw, ...)
```

## Arguments

nw            a [network](#) object.  
...           term options.

## Value

ergm.design returns a [rlebdm](#) of informative (non-missing, non fixed) dyads.

---

ergm.getnetwork	<i>Acquire and verify the network from the LHS of an ergm formula and verify that it is a valid network.</i>
-----------------	--

---

### Description

The function function ensures that the network in a given formula is valid; if so, the network is returned; if not, execution is halted with warnings.

### Usage

```
ergm.getnetwork(formula, loopswarning = getOption("ergm.warn_loops"))
```

### Arguments

formula	a two-sided formula whose LHS is a <a href="#">network</a> , an object that can be coerced to a <a href="#">network</a> , or an expression that evaluates to one.
loopswarning	whether warnings about loops should be printed (TRUE or FALSE); defaults to value of option ergm.warn_loops or TRUE.

### Value

A [network](#) object constructed by evaluating the LHS of the model formula in the formula's environment.

---

ergm.godfather	<i>A function to apply a given series of changes to a network.</i>
----------------	--

---

### Description

Gives the network a series of proposals it can't refuse. Returns the statistics of the network, and, optionally, the final network.

### Usage

```
ergm.godfather(
  object,
  changes = NULL,
  ...,
  end.network = FALSE,
  stats.start = FALSE,
  changes.only = FALSE,
  verbose = FALSE,
  basis = NULL
)
```

```

## S3 method for class 'formula'
ergm.godfather(
  object,
  changes = NULL,
  response = NULL,
  ...,
  end.network = FALSE,
  stats.start = FALSE,
  changes.only = FALSE,
  verbose = FALSE,
  basis = ergm.getnetwork(object)
)

## S3 method for class 'ergm_model'
ergm.godfather(
  object,
  changes = NULL,
  ...,
  end.network = FALSE,
  stats.start = FALSE,
  changes.only = FALSE,
  verbose = FALSE,
  basis = NULL
)

## S3 method for class 'ergm_state'
ergm.godfather(
  object,
  changes = NULL,
  ...,
  end.network = FALSE,
  stats.start = FALSE,
  verbose = FALSE
)

```

## Arguments

object	An <code>ergm()</code> -style formula, with a <code>network</code> on its LHS, an <code>ergm_model()</code> or the object appropriate to the method.
changes	Either a matrix with three columns: tail, head, and new value, describing the changes to be made; or a list of such matrices to apply these changes in a sequence. For binary network models, the third column may be omitted. In that case, the changes are treated as toggles. Note that if a list is passed, it must either be all of changes or all of toggles.
...	additional arguments to <code>ergm_model()</code> .
end.network	Whether to return a network that results. Defaults to FALSE.

stats.start	Whether to return the network statistics at start (before any changes are applied) as the first row of the statistics matrix. Defaults to FALSE, to produce output similar to that of <code>simulate</code> for ERGMs when <code>output="stats"</code> , where initial network's statistics are not returned.
changes.only	Whether to return network statistics or only their changes relative to the initial network.
verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
basis	a value (usually a <code>network</code> ) to override the LHS of the formula.
response	Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows:  NULL Model simple presence or absence, via a binary ERGM. <b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <code>logical</code> (TRUE/FALSE) for binary or <code>numeric</code> for valued. <b>a formula</b> must be of the form NAME~EXPR TYPE (with   being literal). EXPR is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional NAME specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of EXPR. Normally, the type of ERGM is determined by whether the result of evaluating EXPR is logical or numeric, but the optional TYPE can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).

### Value

If `end.network==FALSE` (the default), an `mcmc` object with the requested network statistics associated with the network series produced by applying the specified changes. Its `mcmc` attributes encode the timing information: so `start(out)` gives the time point associated with the first row returned, and `end(out)` out the last. The "thinning interval" is always 1.

If `end.network==TRUE`, return a `network` object, representing the final network, with a matrix of statistics described in the previous paragraph attached to it as an `attr`-style attribute "stats".

### Note

`ergm.godfather.ergm_model()` is a lower-level interface, providing an `ergm.godfather()` method for the `ergm_model` class. The `basis` argument is required.

`ergm.godfather.ergm_state()` is the lowest-level interface, providing an `ergm.godfather()` method for the `ergm_state` class.

### See Also

`tergm.godfather()` in `tergm`, `simulate.ergm()`, `simulate.formula()`

## Examples

```
data(florentine)
ergm.godfather(flomarriage~edges+absdiff("wealth")+triangles,
              changes=list(cbind(1:2,2:3),
                           cbind(3,5),
                           cbind(3,5),
                           cbind(1:2,2:3)),
              stats.start=TRUE)
```

---

ergmConstraint	<i>Sample Space Constraints for Exponential-Family Random Graph Models</i>
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---

## Description

This page describes how to specify the constraints on the network sample space (the set of possible networks  $Y$ , the set of networks  $y$  for which  $h(y) > 0$ ) and sometimes the baseline weights  $h(y)$  to functions in the [ergm](#) package. It also provides an indexed list of the constraints visible to the [ergm](#)'s API. Constraints can also be searched via [search.ergmConstraints](#), and help for an individual constraint can be obtained with `ergmConstraint?<constraint>` or `help("<constraint>-ergmConstraint")`.

## Specifying constraints

In an exponential-family random graph model (ERGM), the probability or density of a given network,  $y \in Y$ , on a set of nodes is

$$h(y) \exp[\eta(\theta) \cdot g(y)] / \kappa(\theta),$$

where  $h(y)$  is the reference distribution (particularly for valued network models),  $g(y)$  is a vector of network statistics for  $y$ ,  $\eta(\theta)$  is a natural parameter vector of the same length (with  $\eta(\theta) \equiv \theta$  for most terms),  $\cdot$  is the dot product, and  $\kappa(\theta)$  is the normalizing constant for the distribution. A complete ERGM specification requires a list of network statistics  $g(y)$  and (if applicable) their  $\eta(\theta)$  mappings provided by a formula of [ergmTerms](#); and, optionally, sample space  $\mathcal{Y}$  and reference distribution  $h(y)$  information provided by [ergmConstraints](#) and, for valued ERGMs, by [ergmReferences](#). Constraints typically affect  $Y$ , or, equivalently, set  $h(y) = 0$  for some  $y$ , but some ("soft" constraints) set  $h(y)$  to values other than 0 and 1.

A constraints formula is a one- or two-sided formula whose left-hand side is an optional direct selection of the `InitErgmProposal` function and whose right-hand side is a series of one or more terms separated by "+" and "-" operators, specifying the constraint.

The sample space (over and above the reference distribution) is determined by iterating over the constraints terms from left to right, each term updating it as follows:

- If the constraint introduces complex dependence structure (e.g., constrains degree or number of edges in the network), then this constraint always restricts the sample space. It may only have a "+" sign.

- If the constraint only restricts the set of dyads that may vary in the sample space (e.g., block-diagonal structure or fixing specific dyads at specific values) and has a "+" sign, the set of dyads that may vary is restricted to those that may vary according to this constraint *and* all the constraints to date.
- If the constraint only restricts the set of dyads that may vary in the sample space but has a "-" sign, the set of dyads that may vary is expanded to those that may vary according to this constraint *or* all the constraints up to date.

For example, a constraints formula  $\sim a-b+c-d$  with all constraints dyadic will allow dyads permitted by either a or b but only if they are also permitted by c; as well as all dyads permitted by d. If A, B, C, and D were logical matrices, the matrix of variable dyads would be equal to  $((A|B)\&C)|D$ .

Terms with a positive sign can be viewed as "adding" a constraint while those with a negative sign can be viewed as "relaxing" a constraint.

#### Inheriting constraints from LHS network:

By default, `%ergmlhs%` attributes constraints or `constraints.obs` (depending on which constraint) attached to the LHS of the model formula or the `basis=` argument will be added in front of the specified constraints formula. This is the desired behaviour most of the time, since those constraints are usually determined by how the network was constructed (e.g., structural zeros in a block-diagonal network).

For those situations in which this is not the desired behavior, a `.` term (with a positive sign or no sign at all) can be used to manually set the position of the inherited constraints in the formula, and a `-.` (minus-dot) term anywhere in the constraints formula will suppress the inherited formula altogether.

#### Constraints visible to the package

Term	Package	Description	Concepts
<code>ChangeStats(fix, check_dind = TRUE)</code>	ergm	Specified statistics must remain constant	directed operator undi- rected
<code>Dyads(fix=NULL, vary=NULL)</code>	ergm	Constrain fixed or varying dyad-independent terms	directed dyad- independent operator undi- rected
<code>I(formula)</code>	ergm	Substitute a formula into the constraints formula	operator
<code>b1degrees</code>	ergm	Preserve the actor degree for bipartite networks	bipartite
<code>b2degrees</code>	ergm	Preserve the receiver degree for bipartite networks	bipartite
<code>bd(attrs, maxout, maxin, minout, minin)</code>	ergm	Constrain maximum and minimum vertex degree	directed undi- rected

blockdiag(attr, noncontig = "merge")	ergm	Block-diagonal structure constraint	directed dyad-independent undirected
blocks(attr=NULL, levels=NULL, levels2=FALSE, b1levels=NULL, b2levels=NULL)	ergm	Constrain blocks of dyads defined by mixing type on a vertex attribute.	directed dyad-independent undirected
degreedist	ergm	Preserve the degree distribution of the given network	directed undirected
degrees nodedegrees	ergm	Preserve the degree of each vertex of the given network	directed undirected
dyadnoise(p01, p10)	ergm	A soft constraint to adjust the sampled distribution for dyad-level noise with known perturbation probabilities	directed dyad-independent soft undirected
edges	ergm	Preserve the edge count of the given network	
egocentric(attr=NULL, direction="both")	ergm	Preserve values of dyads incident on vertices with given attribute	directed dyad-independent undirected
fixallbut(free.dyads)	ergm	Preserve the dyad status in all but the given edges	directed dyad-independent undirected
fixedas(fixed.dyads, present, absent)	ergm	Fix specific dyads	directed dyad-independent undirected
hamming	ergm	Preserve the hamming distance to the given network (BROKEN: Do NOT Use)	directed undirected
idegreedist	ergm	Preserve the indegree distribution	directed
idegrees	ergm	Preserve indegree for directed networks	directed
observed	ergm	Preserve the observed dyads of the given network	directed dyad-independent undirected

odegreedist	ergm	Preserve the outdegree distribution	directed
odegrees	ergm	Preserve outdegree for directed networks	directed

**All constraints:**

Term	dir	op	undir	dyad- indep	bip	soft
ChangeStats	o	o	o			
Dyads	o	o	o	o		
I		o				
b1degrees					o	
b2degrees					o	
bd	o		o			
blockdiag	o		o	o		
blocks	o		o	o		
degreedist	o		o			
degrees	o		o			
dyadnoise	o		o	o		o
edges						
egocentric	o		o	o		
fixallbut	o		o	o		
fixedas	o		o	o		
hamming	o		o			
idegreedist	o					
idegrees	o					
observed	o		o	o		
odegreedist	o					
odegrees	o					

**Constraints by keywords:**

**directed** ChangeStats, Dyads, bd, blockdiag, blocks, degreedist, degrees, dyadnoise, egocentric, fixallbut, fixedas, hamming, idegreedist, idegrees, observed, odegreedist, odegrees

**operator** ChangeStats, Dyads, I

**undirected** ChangeStats, Dyads, bd, blockdiag, blocks, degreedist, degrees, dyadnoise, egocentric, fixallbut, fixedas, hamming, observed

**dyad-independent** Dyads, blockdiag, blocks, dyadnoise, egocentric, fixallbut, fixedas, observed

**bipartite** b1degrees, b2degrees

**soft** dyadnoise

**References**

Goodreau SM, Handcock MS, Hunter DR, Butts CT, Morris M (2008). “A **statnet** Tutorial.” *Journal of Statistical Software*, **24**(9), 1–26. doi:10.18637/jss.v024.i09.

Hunter DR, Handcock MS (2006). “Inference in Curved Exponential Family Models for Networks.” *Journal of Computational and Graphical Statistics*, **15**(3), 565–583. ISSN 1061-8600.

doi:[10.1198/106186006X133069](https://doi.org/10.1198/106186006X133069).

Hunter DR, Handcock MS, Butts CT, Goodreau SM, Morris M (2008). “ergm: A Package to Fit, Simulate and Diagnose Exponential-Family Models for Networks.” *Journal of Statistical Software*, **24**(3), 1–29. doi:[10.18637/jss.v024.i03](https://doi.org/10.18637/jss.v024.i03).

Karwa V, Krivitsky PN, Slavković AB (2017). “Sharing Social Network Data: Differentially Private Estimation of Exponential-Family Random Graph Models.” *Journal of the Royal Statistical Society, Series C*, **66**(3), 481–500. doi:[10.1111/rssc.12185](https://doi.org/10.1111/rssc.12185).

Krivitsky PN (2012). “Exponential-Family Random Graph Models for Valued Networks.” *Electronic Journal of Statistics*, **6**, 1100–1128. doi:[10.1214/12EJS696](https://doi.org/10.1214/12EJS696).

Morris M, Handcock MS, Hunter DR (2008). “Specification of Exponential-Family Random Graph Models: Terms and Computational Aspects.” *Journal of Statistical Software*, **24**(4), 1–24. ISSN 1548-7660. doi:[10.18637/jss.v024.i04](https://doi.org/10.18637/jss.v024.i04).

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ergmHint

*MCMC Hints for Exponential-Family Random Graph Models*

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## Description

This page describes how to provide to the **ergm**’s MCMC algorithms information about the sample space. Hints can also be searched via [search.ergmHints](#), and help for an individual hint can be obtained with `ergmHint?<hint>` or `help("<hint>-ergmHint")`.

## “Hints” for MCMC

In an exponential-family random graph model (ERGM), the probability or density of a given network,  $y \in Y$ , on a set of nodes is

$$h(y) \exp[\eta(\theta) \cdot g(y)] / \kappa(\theta),$$

where  $h(y)$  is the reference distribution (particularly for valued network models),  $g(y)$  is a vector of network statistics for  $y$ ,  $\eta(\theta)$  is a natural parameter vector of the same length (with  $\eta(\theta) \equiv \theta$  for most terms),  $\cdot$  is the dot product, and  $\kappa(\theta)$  is the normalizing constant for the distribution. A complete ERGM specification requires a list of network statistics  $g(y)$  and (if applicable) their  $\eta(\theta)$  mappings provided by a formula of [ergmTerms](#); and, optionally, sample space  $\mathcal{Y}$  and reference distribution  $h(y)$  information provided by [ergmConstraints](#) and, for valued ERGMs, by [ergmReferences](#).

It is often the case that there is additional information available about the distribution of networks being modelled. For example, you may be aware that the network is sparse or that there are strata among the dyads. “Hints”, typically passed on the right-hand side of `MCMC.prop` and `obs.MCMC.prop` arguments to `control.ergm()`, `control.simulate.ergm()`, and others, allow this information to be provided. By default, hint `sparse` is in effect.

Unlike constraints, model terms, and reference distributions, “hints” do not affect the specification of the model. That is, regardless of what “hints” may or may not be in effect, the sample space

and the probabilities within it are the same. However, “hints” may affect the MCMC proposal distribution used by the samplers.

Note that not all proposals support all “hints”: and if the most suitable proposal available cannot incorporate a particular “hint”, a warning message will be printed.

“Hints” use the same underlying API as constraints, and, if present, `%ergmlhs%` attributes constraints and `constraints.obs` will be substituted in its place.

### Hints available to the package

The following hints are known to **ergm** at this time:

Term	Package	Description	Concepts
<code>sparse</code>	ergm	Sparse network	dyad-independent
<code>strat(attr=NULL, pmat=NULL, empirical=FALSE)</code>	ergm	Stratify Proposed Toggles by Mixing Type on a Vertex Attribute	dyad-independent
<code>triadic(triFocus = 0.25, type="OTP")</code> <code>.triadic(triFocus = 0.25, type = "OTP")</code>	ergm	Network with strong clustering (triad-closure) effects	

### References

Goodreau SM, Handcock MS, Hunter DR, Butts CT, Morris M (2008). “A **statnet** Tutorial.” *Journal of Statistical Software*, **24**(9), 1–26. doi:10.18637/jss.v024.i09.

Hunter DR, Handcock MS (2006). “Inference in Curved Exponential Family Models for Networks.” *Journal of Computational and Graphical Statistics*, **15**(3), 565–583. ISSN 1061-8600. doi:10.1198/106186006X133069.

Hunter DR, Handcock MS, Butts CT, Goodreau SM, Morris M (2008). “ergm: A Package to Fit, Simulate and Diagnose Exponential-Family Models for Networks.” *Journal of Statistical Software*, **24**(3), 1–29. doi:10.18637/jss.v024.i03.

Karwa V, Krivitsky PN, Slavković AB (2017). “Sharing Social Network Data: Differentially Private Estimation of Exponential-Family Random Graph Models.” *Journal of the Royal Statistical Society, Series C*, **66**(3), 481–500. doi:10.1111/rssc.12185.

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ergmKeyword	<i>Keywords defined for Exponential-Family Random Graph Models</i>
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**Description**

This collects all defined keywords defined for the ERGM and derived packages

**Possible keywords defined by the ERGM and derived packages**

name	short	description	popular	package
binary	bin	suitable for binary ERGMs	TRUE	ergm
bipartite	bip	suitable for bipartite networks	TRUE	ergm
categorical nodal attribute	cat nodal attr	involves a categorical nodal attribute	FALSE	ergm
categorical dyadic attribute	cat dyad attr	involves a categorical dyadic attribute	FALSE	ergm
categorical triadic attribute	cat triad attr	involves a categorical triadic attribute	FALSE	ergm
continuous	cont	a continuous distribution for edge values	FALSE	ergm
curved	curved	is a curved term	FALSE	ergm
directed	dir	suitable for directed networks	TRUE	ergm
discrete	discrete	a discrete distribution for edge values	FALSE	ergm
dyad-independent	dyad-indep	does not induce dyadic dependence	TRUE	ergm
finite	fin	finite edge values only	FALSE	ergm
frequently-used	freq	is frequently used	FALSE	ergm
nonnegative	nneg	only meaningful for nonnegative edge values	FALSE	ergm
operator	op	a term operator	TRUE	ergm
positive	pos	only meaningful for positive edge values	FALSE	ergm
quantitative nodal attribute	quant nodal attr	involves a quantitative nodal attribute	FALSE	ergm
quantitative dyadic attribute	quant dyad attr	involves a quantitative dyadic attribute	FALSE	ergm
quantitative triadic attribute	quant triad attr	involves a quantitative triadic attribute	FALSE	ergm
soft	soft	a constraint that does not necessarily forbid specific networks outright but reweights their probabilities	FALSE	ergm

triad-related	triad rel	involves triangles, two-paths, and other triadic structures	FALSE	ergm
valued	val	suitable for valued ERGMs	TRUE	ergm
undirected	undir	suitable for undirected networks	TRUE	ergm

---

ergmMPLE                    *ERGM Predictors and response for logistic regression calculation of MPLE*

---

### Description

Return the predictor matrix, response vector, and vector of weights that can be used to calculate the MPLE for an ERGM.

### Usage

```
ergmMPLE(
  formula,
  constraints = ~.,
  obs.constraints = ~-observed,
  output = c("matrix", "array", "dyadlist", "fit"),
  expand.bipartite = FALSE,
  control = control.ergm(),
  verbose = FALSE,
  ...,
  basis = ergm.getnetwork(formula)
)
```

### Arguments

`formula`, `constraints`, `obs.constraints`  
 An ERGM formula and (optionally) a constraint specification formulas. See [ergm\(\)](#). This function supports only dyad-independent constraints.

`output`  
 Character, partially matched. See Value.

`expand.bipartite`  
 Logical. Specifies whether the output matrices (or array slices) representing dyads for bipartite networks are represented as rectangular matrices with first mode vertices in rows and second mode in columns, or as square matrices with dimension equalling the total number of vertices, containing with structural NAs or 0s within each mode.

`control`  
 A list of control parameters for algorithm tuning, typically constructed with [control.ergm\(\)](#). Its documentation gives the the list of recognized control parameters and their meaning. The more generic utility [snctrl\(\)](#) (StatNet CONTROL) also provides argument completion for the available control functions and limited argument name checking.

verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
...	Additional arguments, to be passed to lower-level functions.
basis	a value (usually a <a href="#">network</a> ) to override the LHS of the formula.

## Details

The MPLE for an ERGM is calculated by first finding the matrix of change statistics. Each row of this matrix is associated with a particular pair (ordered or unordered, depending on whether the network is directed or undirected) of nodes, and the row equals the change in the vector of network statistics (as defined in formula) when that pair is toggled from a 0 (no edge) to a 1 (edge), holding all the rest of the network fixed. The MPLE results if we perform a logistic regression in which the predictor matrix is the matrix of change statistics and the response vector is the observed network (i.e., each entry is either 0 or 1, depending on whether the corresponding edge exists or not).

Using `output="matrix"`, note that the result of the fit may be obtained from the `glm()` function, as shown in the examples below.

## Value

If `output=="matrix"` (the default), then only the response, predictor, and weights are returned; thus, the MPLE may be found by hand or the vector of change statistics may be used in some other way. To save space, the algorithm will automatically search for any duplicated rows in the predictor matrix (and corresponding response values). `ergmMPLE` function will return a list with three elements, `response`, `predictor`, and `weights`, respectively the response vector, the predictor matrix, and a vector of weights, which are really counts that tell how many times each corresponding response, predictor pair is repeated.

If `output=="dyadlist"`, as "matrix", but rather than coalescing the duplicated rows, every relation in the network that is not fixed and is observed will have its own row in predictor and element in response and weights, and predictor matrix will have two additional columns at the start, `tail` and `head`, indicating to which dyad the row and the corresponding elements pertain.

If `output=="array"`, a list with similarly named three elements is returned, but response is formatted into a sociomatrix; predictor is a 3-dimensional array of with cell `predictor[t,h,k]` containing the change score of term `k` for dyad `(t,h)`; and weights is also formatted into a sociomatrix, with an element being 1 if it is to be added into the pseudolikelihood and 0 if it is not.

In particular, for a unipartite network, cells corresponding to self-loops, i.e., `predictor[i,i,k]` will be NA and `weights[i,i]` will be 0; and for a unipartite undirected network, lower triangle of each `predictor[, ,k]` matrix will be set to NA, with the lower triangle of weights being set to 0.

To all of the above output types, `attr(,"etamap")` is attached containing the [mapping and offset information](#).

If `output=="fit"`, then `ergmMPLE` simply calls the `ergm()` function with the `estimate="MPLE"` option set, returning an object of class `ergm` that gives the fitted pseudolikelihood model.

## See Also

[ergm\(\)](#), [glm\(\)](#)

## Examples

```

data(faux.mesa.high)
formula <- faux.mesa.high ~ edges + nodematch("Sex") + nodefactor("Grade")
mplesetup <- ergmMPLE(formula)

# Obtain MPLE coefficients "by hand":
coef(glm(mplesetup$response ~ . - 1, data = data.frame(mplesetup$predictor),
  weights = mplesetup$weights, family="binomial"))

# Check that the coefficients agree with the output of the ergm function:
coef(ergmMPLE(formula, output="fit"))

# We can also format the predictor matrix into an array:
mplearray <- ergmMPLE(formula, output="array")

# The resulting matrices are big, so only print the first 8 actors:
mplearray$response[1:8,1:8]
mplearray$predictor[1:8,1:8,]
mplearray$weights[1:8,1:8]

# Constraints are handled:
faux.mesa.high%v%"block" <- seq_len(network.size(faux.mesa.high)) %% 4
mplearray <- ergmMPLE(faux.mesa.high~edges, constraints=~blockdiag("block"), output="array")
mplearray$response[1:8,1:8]
mplearray$predictor[1:8,1:8,]
mplearray$weights[1:8,1:8]

# Or, a dyad list:
faux.mesa.high%v%"block" <- seq_len(network.size(faux.mesa.high)) %% 4
mplearray <- ergmMPLE(faux.mesa.high~edges, constraints=~blockdiag("block"), output="dyadlist")
mplearray$response[1:8]
mplearray$predictor[1:8,]
mplearray$weights[1:8]

# Curved terms produce predictors on the canonical scale:
formula2 <- faux.mesa.high ~ gwesp
mplearray <- ergmMPLE(formula2, output="array")
# The resulting matrices are big, so only print the first 5 actors:
mplearray$response[1:5,1:5]
mplearray$predictor[1:5,1:5,1:3]
mplearray$weights[1:5,1:5]

```

---

ergmProposal

*Metropolis-Hastings Proposal Methods for ERGM MCMC*

---

## Description

This page describes the low-level Metropolis–Hastings (MH) proposal algorithms. They are rarely invoked directly by the user but are rather selected based on the provided [sample space constraints](#) and [hints about the network process](#). They can also be searched via [search.ergmProposals](#), and help for an individual proposal can be obtained with `ergmProposal?<proposal>` or `help("<proposal>-ergmProposal")`.

## Details

`ergm` uses a Metropolis-Hastings (MH) algorithm to control the behavior of the Markov Chain Monte Carlo (MCMC) for sampling networks. The MCMC chain is intended to step around the sample space of possible networks, generating a network at regular intervals to evaluate the statistics in the model. For each MCMC step, one or more toggles are proposed to change the dyads to the opposite value. The probability of accepting the proposed change is determined by the MH acceptance ratio. The role of the different MH methods implemented in `ergm()` is to vary how the sets of dyads are selected for toggle proposals. This is used in some cases to improve the performance (speed and mixing) of the algorithm, and in other cases to constrain the sample space.

## Proposals available to the package

Proposal	Reference	Enforces	May Enforce	Priority	Weight	Class
BDStratTNT	Bernoulli	sparse	bdmax blocks strat	-3	BDStratTNT	c
BDStratTNT	Bernoulli	bdmax sparse	blocks strat	5	BDStratTNT	c
BDStratTNT	Bernoulli	blocks sparse	bdmax strat	5	BDStratTNT	c
BDStratTNT	Bernoulli	strat sparse	bdmax blocks	5	BDStratTNT	c
CondB1Degree	Bernoulli	b1degrees		0	random	c
CondB2Degree	Bernoulli	b2degrees		0	random	c
CondDegree	Bernoulli	degrees		0	random	c
CondDegree	Bernoulli	idegrees odegrees		0	random	c
CondDegree	Bernoulli	b1degrees b2degrees		0	random	c
CondDegreeDist	Bernoulli	degreedist		0	random	c
CondDegreeMix	Bernoulli	degreesmix		0	random	c
CondInDegree	Bernoulli	idegrees		0	random	c
CondInDegreeDist	Bernoulli	idegreedist		0	random	c
CondOutDegree	Bernoulli	odegrees		0	random	c
CondOutDegreeDist	Bernoulli	odegreedist		0	random	c
ConstantEdges	Bernoulli	edges	.dyads bd	0	random	c
DiscUnif	DiscUnif			0	random	c
DiscUnif2	DiscUnif			-1	random2	c
DiscUnifNonObserved	DiscUnif	observed		0	random	c
DistRLE	StdNormal		.dyads	0	random	c
DistRLE	Unif		.dyads	0	random	c
DistRLE	Unif		.dyads	-3	random	c
DistRLE	DiscUnif		.dyads	-3	random	c
DistRLE	StdNormal		.dyads	-3	random	c
DistRLE	Poisson		.dyads	-3	random	c
DistRLE	Binomial		.dyads	-3	random	c
HammingConstantEdges	Bernoulli	edges hamming		0	random	c
HammingTNT	Bernoulli	hamming sparse		0	random	c
SPDyad	Bernoulli	sparse triadic	.dyads bd changestats	0	TNT	c
StdNormal	StdNormal			0	random	c
TNT	Bernoulli	sparse	.dyads bd changestats	0	TNT	c
Unif	Unif			0	random	c
UnifNonObserved	Unif	observed		0	random	c

dyadnoise	Bernoulli	dyadnoise	0	random	c
dyadnoiseTNT	Bernoulli	dyadnoise sparse	1	TNT	c
randomtoggle	Bernoulli	.dyads bd changestats	-2	random	c

Note that `.dyads` is a meta-constraint, indicating that the proposal supports an arbitrary dyad-level constraint combination.

## References

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## See Also

[ergm](#) package, [ergm](#), [ergmConstraint](#), [ergmHint](#), [ergm\\_proposal](#)

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ergmReference

*Reference Measures for Exponential-Family Random Graph Models*

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## Description

This page describes how to specify the reference measures (baseline distributions) (the set of possible networks  $Y$  and the baseline weights  $h(y)$ ) to functions in the `ergm` package. It also provides an indexed list of the references visible to the `ergm`'s API. References can also be searched via `search.ergmReferences()`, and help for an individual reference can be obtained with `ergmReference?<reference>` or `help("<reference>-ergmReference")`.

**Specifying reference measures**

In an exponential-family random graph model (ERGM), the probability or density of a given network,  $y \in Y$ , on a set of nodes is

$$h(y) \exp[\eta(\theta) \cdot g(y)] / \kappa(\theta),$$

where  $h(y)$  is the reference distribution (particularly for valued network models),  $g(y)$  is a vector of network statistics for  $y$ ,  $\eta(\theta)$  is a natural parameter vector of the same length (with  $\eta(\theta) \equiv \theta$  for most terms),  $\cdot$  is the dot product, and  $\kappa(\theta)$  is the normalizing constant for the distribution. A complete ERGM specification requires a list of network statistics  $g(y)$  and (if applicable) their  $\eta(\theta)$  mappings provided by a formula of [ergmTerms](#); and, optionally, sample space  $\mathcal{Y}$  and reference distribution  $h(y)$  information provided by [ergmConstraints](#) and, for valued ERGMs, by [ergmReferences](#).

The reference measure ( $Y, h(y)$ ) is specified on the right-hand side of a one-sided formula passed typically as the reference argument.

**Reference measures visible to the package**

Term	Package	Description	Concepts
Bernoulli	ergm	Bernoulli reference	discrete finite non-negative
DiscUnif(a,b)	ergm	Discrete Uniform reference	discrete finite
StdNormal	ergm	Standard Normal reference	continuous
Unif(a,b)	ergm	Continuous Uniform reference	continuous

**All references:**

Term	bin	discrete	fin	nneg	cont
Bernoulli	o	o	o	o	
DiscUnif		o	o		
StdNormal					o
Unif					o

**References by keywords:**

**binary** Bernoulli

**discrete** Bernoulli, DiscUnif

**finite** Bernoulli, DiscUnif

**nonnegative** Bernoulli

**continuous** StdNormal, Unif

**References**

Hunter DR, Handcock MS, Butts CT, Goodreau SM, Morris M (2008). “ergm: A Package to Fit, Simulate and Diagnose Exponential-Family Models for Networks.” *Journal of Statistical Software*,

24(3), 1–29. doi:10.18637/jss.v024.i03.

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### See Also

[ergm](#), [network](#), [sna](#), [summary.ergm](#), [print.ergm](#), `\%v\%`, `\%n\%`

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ergmTerm

*Terms used in Exponential Family Random Graph Models*

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### Description

This page explains how to specify the network statistics  $g(y)$  to functions in the [ergm](#) package and packages that extend it. It also provides an indexed list of the possible terms (and hence network statistics) visible to the [ergm](#) API. Terms can also be searched via [search.ergmTerms](#), and help for an individual term can be obtained with `ergmTerm?<term>` or `help("<term>-ergmTerm")`.

### Specifying models

In an exponential-family random graph model (ERGM), the probability or density of a given network,  $y \in Y$ , on a set of nodes is

$$h(y) \exp[\eta(\theta) \cdot g(y)] / \kappa(\theta),$$

where  $h(y)$  is the reference distribution (particularly for valued network models),  $g(y)$  is a vector of network statistics for  $y$ ,  $\eta(\theta)$  is a natural parameter vector of the same length (with  $\eta(\theta) \equiv \theta$  for most terms),  $\cdot$  is the dot product, and  $\kappa(\theta)$  is the normalizing constant for the distribution. A complete ERGM specification requires a list of network statistics  $g(y)$  and (if applicable) their  $\eta(\theta)$  mappings provided by a formula of [ergmTerms](#); and, optionally, sample space  $\mathcal{Y}$  and reference distribution  $h(y)$  information provided by [ergmConstraints](#) and, for valued ERGMs, by [ergmReferences](#).

Network statistics  $g(y)$  and mappings  $\eta(\theta)$  are specified by a formula object, of the form `y ~ <term 1> + <term 2> ...`, where `y` is a network object or a matrix that can be coerced to a network object, and `<term 1>`, `<term 2>`, etc. are each terms chosen from the list given below. To create a network object in `R`, use the [network](#) function, then add nodal attributes to it using the `%v%` operator if necessary.

#### Term operators:

Operator terms like `B()` and `F()` take formulas with other [ergm](#) terms as their arguments and transform them by modifying their inputs (e.g., the network they evaluate) and/or their outputs.

By convention, their names are capitalized and CamelCased.

#### Interactions:

For binary ERGMs, interactions between [ergm](#) terms can be specified in a manner similar to `lm` and others, as using the `:` and `*` operators. However, they must be interpreted carefully, especially for dyad-dependent terms. (Interactions involving curved terms are not supported at this time.)

Generally, if term a has  $p_a$  statistics and b has  $p_b$ , a:b will add  $p_a \times p_b$  statistics to the model, corresponding to each element of  $g_a(y)$  interacted with each element of  $g_b(y)$ .

The interaction is defined as follows. Dyad-independent terms can be expressed in the general form  $g(y; x) = \sum_{i,j} x_{i,j} y_{i,j}$  for some edge covariate matrix  $x$ ,

$$g_{a:b}(y) = \sum_{i,j} x_{a,i,j} x_{b,i,j} y_{i,j}.$$

In other words, rather than being a product of their sufficient statistics ( $g_a(y)g_b(y)$ ), it is a dyad-wise product of their dyad-level effects.

This means that an interaction between two dyad-independent terms can be interpreted the same way as it would be in the corresponding logistic regression for each potential edge. However, for undirected networks in particular, this may lead to somewhat counterintuitive results. For example, given two nodal covariates "a" and "b" (whose values for node  $i$  are denoted  $a_i$  and  $b_i$ , respectively), `nodecov("a")` adds one statistic of the form  $\sum_{i,j} (a_i + a_j) y_{i,j}$  and analogously for `nodecov("b")`, so `nodecov("a"):nodecov("b")` produces

$$\sum_{i,j} (a_i + a_j)(b_i + b_j) y_{i,j}.$$

**Binary and valued ERGM terms:**

`ergm` functions such as `ergm` and `simulate` (for ERGMs) may operate in two modes: binary and weighted/valued, with the latter activated by passing a non-NULL value as the response argument, giving the edge attribute name to be modeled/simulated.

*Generalizations of binary terms:*

Binary ERGM statistics cannot be used directly in valued mode and vice versa. However, a substantial number of binary ERGM statistics — particularly the ones with dyadic independence — have simple generalizations to valued ERGMs, and have been adapted in `ergm`. They have the same form as their binary ERGM counterparts, with an additional argument: `form`, which, at this time, has two possible values: "sum" (the default) and "nonzero". The former creates a statistic of the form  $\sum_{i,j} x_{i,j} y_{i,j}$ , where  $y_{i,j}$  is the value of dyad  $(i, j)$  and  $x_{i,j}$  is the term's covariate associated with it. The latter computes the binary version, with the edge considered to be present if its value is not 0. Valued version of some binary ERGM terms have an argument `threshold`, which sets the value above which a dyad is considered to have a tie. (Value less than or equal to `threshold` is considered a nontie.)

The `B()` operator term documented below can be used to pass other binary terms to valued models, and is more flexible, at the cost of being somewhat slower.

*Transformations of dyad values:*

An expression of the form `... + (EXPR ~ TERMS) + ...` will evaluate `TERMS` on a network constructed by applying the transformation specified by `EXPR` to edge values. At this time, "sqrt" is the only transformation supported (e.g., `("sqrt" ~ sum)` is equivalent to `sum(pow = 1/2)`).

**Nodal attribute levels and indices:**

Terms taking a categorical nodal covariate also take the `levels` argument. (There are analogous `b1levels` and `b2levels` arguments for some terms that apply to bipartite networks, and the `levels2` argument for mixing terms.) The `levels` argument can be used to control the set and the ordering of attribute levels.

Terms that allow the selection of nodes do so with the `nodes` argument, which is interpreted in the same way as the `levels` argument, where the categories are the relevant nodal indices themselves.

Both levels and nodes use the new level selection UI. (See [Specifying Vertex attributes and Levels](#) (? nodal\_attributes) for details.)

*Legacy arguments:*

The legacy base and keep arguments are deprecated as of version 3.10, and replaced by the levels UI. The levels argument provides consistent and flexible mechanisms for specifying which attribute levels to exclude (previously handled by base) and include (previously handled by keep). If levels or nodes argument is given, then base and keep arguments are ignored. The legacy arguments will most likely be removed in a future version.

Note that this exact behavior is new in version 3.10, and it differs slightly from older versions: previously if both levels and base/keep were given, levels argument was applied first and then applied the base/keep argument. Since version 3.10, base/keep would be ignored, even if old term behavior is invoked (as described in the next section).

**Term versioning:**

When a term's behavior has changed from prior version, it is often possible to invoke the old behavior by setting and/or passing a version term option, giving the version (constructed by `as.package_version`) desired.

**Custom ergm terms:**

Users and other packages may build custom terms, and package **ergm.userterms** (<https://github.com/statnet/ergm.userterms>) provides tools for implementing them, and the [Terms-API vignette](#).

There is also a number of *auxiliaries* available—terms that do not have statistics of their own but provide data structures useful to other terms. For auxiliaries currently visible to **ergm**, see [ergmAuxiliary](#).

The current recommendation for any package implementing additional terms is to document the term with Roxygen comments and a name in the form `termName-ergmTerm`. This ensures that `help("ergmTerm")` will list ERGM terms available from all loaded packages.

**Terms included in the ergm package**

As noted above, a cross-referenced HTML version of the term documentation is also available via `vignette('ergm-term-crossRef')` and terms can also be searched via `search.ergmTerms`.

**Term index (plain):**

Term	Package	Description	Concepts
<code>absdiff(attr, pow)</code> (bin)	ergm	Absolute difference in nodal attribute	directed
<code>absdiff(attr, pow, form)</code> (val)			dyad-independent quantitative nodal attribute undirected

absdiffcat(attr, base, levels) (bin) absdiffcat(attr, base, levels, form) (val)	ergm	Categorical absolute difference in nodal attribute	categorical nodal attribute directed dyad-independent undirected
altkstar(lambda, fixed) (bin)	ergm	Alternating k-star	categorical nodal attribute curved undirected
asymmetric(attr, diff, keep, levels) (bin)	ergm	Asymmetric dyads	directed dyad-independent triad-related
atleast(threshold) (val)	ergm	Number of dyads with values greater than or equal to a threshold	directed dyad-independent undirected
atmost(threshold) (val)	ergm	Number of dyads with values less than or equal to a threshold	directed dyad-independent undirected
attrcov(attr, mat) (bin) attrcov(attr, mat, form) (val)	ergm	Edge covariate by attribute pairing	directed dyad-independent undirected
b1concurrent(by, levels) (bin)	ergm	Concurrent node count for the first mode in a bipartite network	bipartite categorical nodal attribute undirected

b1cov(attr) (bin) b1cov(attr, form) (val)	ergm	Main effect of a covariate for the first mode in a bipartite network	bipartite dyad- independent frequently- used quantita- tive nodal attribute undi- rected
nodecovrange(attr) (bin)	ergm	Range of covariate values for neighbors of a mode-1 node	bipartite quantita- tive nodal attribute
b1degrange(from, to, by, homophily, levels) (bin)	ergm	Degree range for the first mode in a bipartite network	bipartite undi- rected
b1degree(d, by, levels) (bin)	ergm	Degree for the first mode in a bipartite network	bipartite categori- cal nodal attribute frequently- used undi- rected
b1dsp(d) (bin)	ergm	Dyadwise shared partners for dyads in the first bipartition	bipartite undi- rected
b1factor(attr, base, levels) (bin) b1factor(attr, base, levels, form) (val)	ergm	Factor attribute effect for the first mode in a bipartite network	bipartite categori- cal nodal attribute dyad- independent frequently- used undi- rected
b1factordistinct(attr, levels) (bin)	ergm	Number of distinct neighbor types for the first node	bipartite categori- cal nodal attribute
b1mindegree(d) (bin)	ergm	Minimum degree for the first mode in a bipartite network	bipartite undi- rected

b1nodematch(attr, diff, keep, alpha, beta, byb2attr, levels) (bin)	ergm	Nodal attribute-based homophily effect for the first mode in a bipartite network	bipartite categorical nodal attribute dyad- independent frequently- used undi- rected
b1sociality(nodes) (bin) b1sociality(nodes, form) (val)	ergm	Degree	bipartite dyad- independent undi- rected
b1star(k, attr, levels) (bin)	ergm	k-stars for the first mode in a bipartite network	bipartite categorical nodal attribute undi- rected
b1starmix(k, attr, base, diff) (bin)	ergm	Mixing matrix for k-stars centered on the first mode of a bipartite network	bipartite categorical nodal attribute undi- rected
b1twostar(b1attr, b2attr, base, b1levels, b2levels, levels2) (bin)	ergm	Two-star census for central nodes centered on the first mode of a bipartite network	bipartite categorical nodal attribute undi- rected
b2concurrent(by) (bin)	ergm	Concurrent node count for the second mode in a bipartite network	bipartite frequently- used undi- rected

b2cov(attr) (bin) b2cov(attr, form) (val)	ergm	Main effect of a covariate for the second mode in a bipartite network	bipartite dyad- independent frequently- used quantita- tive nodal attribute undi- rected
nodecovrange(attr) (bin)	ergm	Range of covariate values for neighbors of a mode-2 node	bipartite quantita- tive nodal attribute
b2degrange(from, to, by, homophily, levels) (bin)	ergm	Degree range for the second mode in a bipartite network	bipartite undi- rected
b2degree(d, by) (bin)	ergm	Degree for the second mode in a bipartite network	bipartite categori- cal nodal attribute frequently- used undi- rected
b2dsp(d) (bin)	ergm	Dyadwise shared partners for dyads in the second bipartition	bipartite undi- rected
b2factor(attr, base, levels) (bin) b2factor(attr, base, levels, form) (val)	ergm	Factor attribute effect for the second mode in a bipartite network	bipartite categori- cal nodal attribute dyad- independent frequently- used undi- rected
b2factordistinct(attr, levels) (bin)	ergm	Number of distinct neighbor types for the second mode	bipartite categori- cal nodal attribute
b2mindegree(d) (bin)	ergm	Minimum degree for the second mode in a bipartite network	bipartite undi- rected

b2nodematch(attr, diff, keep, alpha, beta, byb1attr, levels) (bin)	ergm	Nodal attribute-based homophily effect for the second mode in a bipartite network	bipartite categorical nodal attribute dyad- independent frequently- used undi- rected
b2sociality(nodes) (bin) b2sociality(nodes, form) (val)	ergm	Degree	bipartite dyad- independent undi- rected
b2star(k, attr, levels) (bin)	ergm	k-stars for the second mode in a bipartite network	bipartite categorical nodal attribute undi- rected
b2starmix(k, attr, base, diff) (bin)	ergm	Mixing matrix for k-stars centered on the second mode of a bipartite network	bipartite categorical nodal attribute undi- rected
b2twostar(b1attr, b2attr, base, b1levels, b2levels, levels2) (bin)	ergm	Two-star census for central nodes centered on the second mode of a bipartite network	bipartite categorical nodal attribute undi- rected
balance (bin)	ergm	Balanced triads	directed triad- related undi- rected
cdf(min, max, by, margin, nmax) (val)	ergm	Empirical cumulative distribution function (unnormalized) of the network's dyad values	directed dyad- independent undi- rected
coincidence(levels, active) (bin)	ergm	Coincident node count for the second mode in a bipartite (aka two-mode) network	bipartite undi- rected

concurrent(by, levels) (bin)	ergm	Concurrent node count	categorical nodal at- tribute undi- rected
concurrentties(by, levels) (bin)	ergm	Concurrent tie count	categorical nodal at- tribute undi- rected
ctriple(attr, diff, levels) (bin) ctriad (bin)	ergm	Cyclic triples	categorical nodal at- tribute directed triad- related
cycle(k, semi) (bin)	ergm	k-Cycle Census	directed undi- rected
cyclicalities(attr, levels) (bin) cyclicalities(threshold) (val)	ergm	Cyclical ties	directed undi- rected
cyclicalweights(twopath, combine, affect) (val)	ergm	Cyclical weights	directed nonneg- ative undi- rected
degcor (bin)	ergm	Degree Correlation	undirected
degcrossprod (bin)	ergm	Degree Cross-Product	undirected
degrange(from, to, by, homophily, levels) (bin)	ergm	Degree range	categorical nodal at- tribute undi- rected
degree(d, by, homophily, levels) (bin)	ergm	Degree	categorical nodal attribute frequently- used undi- rected
degree1.5 (bin)	ergm	Degree to the 3/2 power	undirected

density (bin)	ergm	Density	directed dyad- independent undi- rected
diff(attr, pow, dir, sign.action) (bin) diff(attr, pow, dir, sign.action, form) (val)	ergm	Difference	bipartite directed dyad- independent frequently- used quantita- tive nodal attribute undi- rected
ddsp(d, type) (bin) dsp(d, type) (bin)	ergm	Directed dyadwise shared partners	directed
dyadcov(x, attrname) (bin)	ergm	Dyadic covariate	directed dyad- independent quanti- tative dyadic attribute undi- rected
edgecov(x, attrname) (bin) edgecov(x, attrname, form) (val)	ergm	Edge covariate	directed dyad- independent frequently- used quan- titative dyadic attribute undi- rected
edges (bin) nonzero (val) edges (val)	ergm	Number of edges in the network	directed dyad- independent undi- rected

<code>equalto(value, tolerance)</code> (val)	ergm	Number of dyads with values equal to a specific value (within tolerance)	directed dyad- independent undi- rected
<code>desp(d, type)</code> (bin) <code>esp(d, type)</code> (bin)	ergm	Directed edgewise shared partners	directed
<code>greaterthan(threshold)</code> (val)	ergm	Number of dyads with values strictly greater than a threshold	directed dyad- independent undi- rected
<code>gwb1degree(decay, fixed, attr, cutoff, levels)</code> (bin)	ergm	Geometrically weighted degree distribution for the first mode in a bipartite network	bipartite curved undi- rected
<code>gwb1dsp(decay, fixed, cutoff)</code> (bin)	ergm	Geometrically weighted dyadwise shared partner distribution for dyads in the first bipartition	bipartite curved undi- rected
<code>gwb2degree(decay, fixed, attr, cutoff, levels)</code> (bin)	ergm	Geometrically weighted degree distribution for the second mode in a bipartite network	bipartite curved undi- rected
<code>gwb2dsp(decay, fixed, cutoff)</code> (bin)	ergm	Geometrically weighted dyadwise shared partner distribution for dyads in the second bipartition	bipartite curved undi- rected
<code>gwdegree(decay, fixed, attr, cutoff, levels)</code> (bin)	ergm	Geometrically weighted degree distribution	curved frequently- used undi- rected
<code>dgwdsp(decay, fixed, cutoff, type)</code> (bin) <code>gwdsp(decay, fixed, cutoff, type)</code> (bin)	ergm	Geometrically weighted dyadwise shared partner distribution	directed
<code>dgwesp(decay, fixed, cutoff, type)</code> (bin) <code>gwesp(decay, fixed, cutoff, type)</code> (bin)	ergm	Geometrically weighted edgewise shared partner distribution	directed
<code>gwidegree(decay, fixed, attr, cutoff, levels)</code> (bin)	ergm	Geometrically weighted in-degree distribution	curved di- rected
<code>dgwnsp(decay, fixed, cutoff, type)</code> (bin) <code>gwnsp(decay, fixed, cutoff, type)</code> (bin)	ergm	Geometrically weighted non-edgewise shared partner distribution	directed

gwodegree(decay, fixed, attr, cutoff, levels) (bin)	ergm	Geometrically weighted out-degree distribution	curved directed
hamming(x, cov, attrname) (bin)	ergm	Hamming distance	directed dyad-independent undirected
idegrange(from, to, by, homophily, levels) (bin)	ergm	In-degree range	categorical nodal attribute directed
idegree(d, by, homophily, levels) (bin)	ergm	In-degree	categorical nodal attribute directed frequently-used
idegree1.5 (bin)	ergm	In-degree to the 3/2 power	directed
ininterval(lower, upper, open) (val)	ergm	Number of dyads whose values are in an interval	directed dyad-independent undirected
intransitive (bin)	ergm	Intransitive triads	directed triad-related
isolatededges (bin)	ergm	Isolated edges	bipartite undirected
isolates (bin)	ergm	Isolates	directed frequently-used undirected
istar(k, attr, levels) (bin)	ergm	In-stars	categorical nodal attribute directed
kstar(k, attr, levels) (bin)	ergm	k-stars	categorical nodal attribute undirected

localtriangle(x) (bin)	ergm	Triangles within neighborhoods	categoryal dyadic attribute directed triad- related undi- rected
m2star (bin)	ergm	Mixed 2-stars, a.k.a 2-paths	directed
meandeg (bin)	ergm	Mean vertex degree	directed dyad- independent undi- rected
mm(attrs, levels, levels2) (bin) mm(attrs, levels, levels2, form) (val)	ergm	Mixing matrix cells and margins	categoryal nodal at- tribute directed dyad- independent frequently- used undi- rected
mutual(same, by, diff, keep, levels) (bin) mutual(form, threshold) (val)	ergm	Mutuality	directed frequently- used
nearsimmelian (bin)	ergm	Near simmelian triads	directed triad- related
nodecov(attr) (bin) nodemain (bin) nodecov(attr, form) (val) nodemain(attr, form) (val)	ergm	Main effect of a covariate	directed dyad- independent frequently- used quantita- tive nodal attribute undi- rected
nodecovar(center, transform) (val)	ergm	Covariance of undirected dyad values incident on each actor	undirected

nodecovrange(attr) (bin)	ergm	Range of covariate values for neighbors of a node	directed quantitative nodal attribute undirected
nodefactor(attr, base, levels) (bin) nodefactor(attr, base, levels, form) (val)	ergm	Factor attribute effect	categoryal nodal attribute directed dyad-independent frequently-used undirected
nodefactordistinct(attr, levels) (bin)	ergm	Number of distinct neighbor types	categoryal nodal attribute directed undirected
nodeicov(attr) (bin) nodeicov(attr, form) (val)	ergm	Main effect of a covariate for in-edges	directed frequently-used quantitative nodal attribute
nodeicovar(center, transform) (val)	ergm	Covariance of in-dyad values incident on each actor	directed
nodeicovrange(attr) (bin)	ergm	Range of covariate values for in-neighbors of a node	directed quantitative nodal attribute
nodeifactor(attr, base, levels) (bin) nodeifactor(attr, base, levels, form) (val)	ergm	Factor attribute effect for in-edges	categoryal nodal attribute directed dyad-independent frequently-used
nodeifactordistinct(attr, levels) (bin)	ergm	Number of distinct in-neighbor types	categoryal nodal attribute directed

nodematch(attr, diff, keep, levels) (bin) nodematch(attr, diff, keep, levels, form) (val) match(attr, diff, keep, levels, form) (val)	ergm	Uniform homophily and differential homophily	categorical nodal attribute directed dyad-independent frequently-used undirected
nodemix(attr, base, b1levels, b2levels, levels, levels2) (bin) nodemix(attr, base, b1levels, b2levels, levels, levels2, form) (val)	ergm	Nodal attribute mixing	categorical nodal attribute directed dyad-independent frequently-used undirected
nodeocov(attr) (bin) nodeocov(attr, form) (val)	ergm	Main effect of a covariate for out-edges	directed dyad-independent quantitative nodal attribute
nodeocovar(center, transform) (val)	ergm	Covariance of out-dyad values incident on each actor	directed
nodeocovrange(attr) (bin)	ergm	Range of covariate values for out-neighbors of a node	directed quantitative nodal attribute
nodeofactor(attr, base, levels) (bin) nodeofactor(attr, base, levels, form) (val)	ergm	Factor attribute effect for out-edges	categorical nodal attribute directed dyad-independent
nodeofactordistinct(attr, levels) (bin)	ergm	Number of distinct out-neighbor types	categorical nodal attribute directed
dnsp(d, type) (bin) nsp(d, type) (bin)	ergm	Directed non-edgewise shared partners	directed

odegrange(from, to, by, homophily, levels) (bin)	ergm	Out-degree range	categorical nodal attribute directed
odegree(d, by, homophily, levels) (bin)	ergm	Out-degree	categorical nodal attribute directed frequently-used
odegree1.5 (bin)	ergm	Out-degree to the 3/2 power	directed
opentriad (bin)	ergm	Open triads	triad-related undirected
ostar(k, attr, levels) (bin)	ergm	k-Outstars	categorical nodal attribute directed
receiver(base, nodes) (bin) receiver(base, nodes, form) (val)	ergm	Receiver effect	directed dyad-independent
sender(base, nodes) (bin) sender(base, nodes, form) (val)	ergm	Sender effect	directed dyad-independent
simmelian (bin)	ergm	Simmelian triads	directed triad-related
simmelian_ties (bin)	ergm	Ties in simmelian triads	directed triad-related
smalldiff(attr, cutoff) (bin)	ergm	Number of ties between actors with similar attribute values	directed dyad-independent quantitative nodal attribute undirected
smallerthan(threshold) (val)	ergm	Number of dyads with values strictly smaller than a threshold	directed dyad-independent undirected

sociality(attr, base, levels, nodes) (bin) sociality(attr, base, levels, nodes, form) (val)	ergm	Undirected degree	categorical nodal attribute dyad-independent undirected
sum(pow) (val)	ergm	Sum of dyad values (optionally taken to a power)	directed undirected
threetrail(keep, levels) (bin) threepath(keep, levels) (bin)	ergm	Three-trails	directed triad-related undirected
transitive (bin)	ergm	Transitive triads	directed triad-related
transitivities(attr, levels) (bin)	ergm	Transitive ties	categorical nodal attribute directed triad-related undirected
transitiveweights(twopath, combine, affect) (val)	ergm	Transitive weights	directed nonnegative triad-related undirected
triadcensus(levels) (bin)	ergm	Triad census	directed triad-related undirected

triangle(attr, diff, levels) (bin) triangles(attr, diff, levels) (bin)	ergm	Triangles	categoryal nodal at-tribute directed frequently-used triad-related undi-rected
tripercnt(attr, diff, levels) (bin)	ergm	Triangle percentage	categoryal nodal at-tribute triad-related undi-rected
ttriple(attr, diff, levels) (bin) ttriad (bin)	ergm	Transitive triples	categoryal nodal at-tribute directed triad-related
twopath (bin)	ergm	2-Paths	directed undi-rected

**Term index (operator):**

Term	Package	Description	Concepts
B(formula, form) (val)	ergm	Wrap binary terms for use in valued models	operator

Curve(formula, params, map, gradient, minpar, maxpar, cov) (bin) Parametrise(formula, params, map, gradient, minpar, maxpar, cov) (bin) Parametrize(formula, params, map, gradient, minpar, maxpar, cov) (bin) Curve(formula, params, map, gradient, minpar, maxpar, cov) (val) Parametrise(formula, params, map, gradient, minpar, maxpar, cov) (val) Parametrize(formula, params, map, gradient, minpar, maxpar, cov) (val)	ergm	Impose a curved structure on term parameters	operator
Exp(formula) (bin) Exp(formula) (val)	ergm	Exponentiate a network's statistic	operator
F(formula, filter) (bin)	ergm	Filtering on arbitrary one-term model	operator
For(...) (bin) For(...) (val)	ergm	A for operator for terms	operator
I(formula) (bin) I(formula) (val)	ergm	Substitute a formula into the model formula	operator
Label(formula, label, pos) (bin) Label(formula, label, pos) (val)	ergm	Modify terms' coefficient names	operator
Log(formula, log $\theta$ ) (bin) Log(formula, log $\theta$ ) (val)	ergm	Take a natural logarithm of a network's statistic	operator
NodematchFilter(formula, attrname) (bin)	ergm	Filtering on nodematch	operator
Offset(formula, coef, which) (bin)	ergm	Terms with fixed coefficients	operator
Prod(formulas, label) (bin) Prod(formulas, label) (val)	ergm	A product (or an arbitrary power combination) of one or more formulas	operator
Project(formula, mode) (bin) Proj1(formula) (bin) Proj2(formula) (bin)	ergm	Evaluation on a projection of a bipartite network	bipartite operator
S(formula, attrs) (bin) S(formula, attrs) (val)	ergm	Evaluation on an induced subgraph	operator
Sum(formulas, label) (bin) Sum(formulas, label) (val)	ergm	A sum (or an arbitrary linear combination) of one or more formulas	operator

Symmetrize(formula, rule) (bin)	ergm	Evaluation on symmetrized (undirected) network	directed operator
Symmetrize(formula, rule) (val)			

**Frequently-used terms:**

Term	bin	bip	dir	dyad- indep	op	val	undir
b1cov	o	o		o		o	o
b1degree	o	o					o
b1factor	o	o		o		o	o
b1nodematch	o	o		o			o
b2concurrent	o	o					o
b2cov	o	o		o		o	o
b2degree	o	o					o
b2factor	o	o		o		o	o
b2nodematch	o	o		o			o
degree	o						o
diff	o	o	o	o		o	o
edgecov	o		o	o		o	o
gwdegree	o						o
idegree	o		o				
isolates	o		o				o
mm	o		o	o		o	o
mutual	o		o			o	
nodecov	o		o	o		o	o
nodefactor	o		o	o		o	o
nodeicov	o		o			o	
nodeifactor	o		o	o		o	
nodematch	o		o	o		o	o
nodemix	o		o	o		o	o
odegree	o		o				
triangle	o		o				o

**Operator terms:**

Term	bin	bip	dir	dyad- indep	val	undir
B					o	
Curve	o				o	
Exp	o				o	
F	o					
For	o				o	
I	o				o	
Label	o				o	

Log	o		o
NodematchFilter	o		
Offset	o		
Prod	o		o
Project	o	o	
S	o		o
Sum	o		o
Symmetrize	o	o	o

**All terms:**

Term	op	val	bin	bip	dir	dyad- indep	quant nodal attr	undir	cat nodal attr	curved	triad rel	freq	nneg	qua dya attr
B	o	o												
Curve	o	o	o											
Exp	o	o	o											
F	o		o											
For	o	o	o											
I	o	o	o											
Label	o	o	o											
Log	o	o	o											
NodematchFilter	o		o											
Offset	o		o											
Prod	o	o	o											
Project	o		o	o										
S	o	o	o											
Sum	o	o	o											
Symmetrize	o	o	o		o									
absdiff		o	o		o	o	o	o						
absdiffcat		o	o		o	o		o	o					
altkstar			o					o	o	o				
asymmetric			o		o	o					o			
atleast		o			o	o		o						
atmost		o			o	o		o						
attreov		o	o		o	o		o						
b1concurrent			o	o				o	o					
b1cov		o	o	o		o	o	o				o		
b1covrange			o	o			o							
b1degrange			o	o				o						
b1degree			o	o				o	o			o		
b1dsp			o	o				o						
b1factor		o	o	o		o		o	o			o		
b1factordistinct			o	o					o					
b1mindegree			o	o				o						
b1nodematch			o	o		o		o	o			o		

b1sociality	0	0	0	0	0	0	0	0
b1star		0	0			0	0	
b1starmix		0	0			0	0	
b1twostar		0	0			0	0	
b2concurrent		0	0			0		0
b2cov	0	0	0	0	0	0		0
b2covrange		0	0		0			
b2degrange		0	0			0		
b2degree		0	0			0	0	0
b2dsp		0	0			0		
b2factor	0	0	0	0	0	0	0	0
b2factordistinct		0	0				0	
b2mindegree		0	0			0		
b2nodematch		0	0	0	0	0		0
b2sociality	0	0	0	0	0			
b2star		0	0			0	0	
b2starmix		0	0			0	0	
b2twostar		0	0			0	0	
balance		0		0		0		0
cdf	0			0	0	0		
coincidence		0	0			0		
concurrent		0				0	0	
concurrentties		0				0	0	
ctriple		0		0			0	0
cycle		0		0		0		
cyclicalities	0	0		0		0		
cyclicalweights	0			0		0		0
degcor		0				0		
degcrossprod		0				0		
degrange		0				0	0	
degree		0				0	0	0
degree1.5		0				0		
density		0		0	0	0		
diff	0	0	0	0	0	0	0	0
dsp		0		0				
dyadcov		0		0	0	0		0
edgecov	0	0		0	0	0		0
edges	0	0		0	0	0		
equalto	0			0	0	0		
esp		0		0				
greaterthan	0			0	0	0		
gwb1degree		0	0			0		0
gwb1dsp		0	0			0		0
gwb2degree		0	0			0		0
gwb2dsp		0	0			0		0
gwdegree		0				0	0	0

gwdsp	0	0						
gwesp	0	0						
gwidegree	0	0				0		
gwensp	0	0						
gwodegree	0	0				0		
hamming	0	0	0	0				
idegrange	0	0				0		
idegree	0	0				0		0
idegree1.5	0	0						
ininterval	0		0	0	0			
intransitive	0		0					0
isolatededges	0	0				0		
isolates	0	0	0	0				0
istar	0	0				0		
kstar	0					0	0	
localtriangle	0	0				0		0
m2star	0	0						
meandeg	0	0	0	0	0			
mm	0	0	0	0	0	0		0
mutual	0	0	0					0
nearsimmelian	0	0						0
nodecov	0	0	0	0	0	0		0
nodecovar	0					0		
nodecovrange	0	0		0	0			
nodefactor	0	0	0	0		0	0	0
nodefactordistinct	0	0				0	0	
nodeicov	0	0	0		0			0
nodeicovar	0		0					
nodeicovrange	0	0			0			
nodeifactor	0	0	0	0			0	0
nodeifactordistinct	0	0					0	
nodematch	0	0	0	0		0	0	0
nodemix	0	0	0	0		0	0	0
nodeocov	0	0	0	0	0			
nodeocovar	0		0					
nodeocovrange	0	0			0			
nodeofactor	0	0	0	0			0	
nodeofactordistinct	0	0					0	
nsp	0	0						
odegrange	0	0					0	
odegree	0	0					0	0
odegree1.5	0	0						
opentriad	0					0		0
ostar	0	0					0	
receiver	0	0	0	0				
sender	0	0	0	0				

simmelian	o	o			o
simmeliانتies	o	o			o
smalldiff	o	o	o	o	o
smallerthan	o	o	o	o	
sociality	o	o	o	o	o
sum	o	o		o	
threetrail	o	o		o	o
transitive	o	o			o
transitivityes	o	o		o	o
transitivityweights	o	o		o	o
triadcensus	o	o		o	o
triangle	o	o		o	o
tripercents	o			o	o
ttriple	o	o		o	o
twopath	o	o		o	

**Terms by keywords:**

**operator** B, Curve, Exp, F, For, I, Label, Log, NodematchFilter, Offset, Prod, Project, S, Sum, Symmetrize

**valued** B, Curve, Exp, For, I, Label, Log, Prod, S, Sum, Symmetrize, absdiff, absdiffcat, atleast, atmost, attrcov, b1cov, b1factor, b1sociality, b2cov, b2factor, b2sociality, cdf, cyclicalities, cyclicalweights, diff, edgescov, edges, equalto, greaterthan, ininterval, mm, mutual, nodecov, nodecovar, nodefactor, nodeicov, nodeicovar, nodeifactor, nodematch, nodemix, nodecov, nodecovar, nodeofactor, receiver, sender, smallerthan, sociality, sum, transitivityweights

**binary** Curve, Exp, F, For, I, Label, Log, NodematchFilter, Offset, Prod, Project, S, Sum, Symmetrize, absdiff, absdiffcat, altkstar, asymmetric, attrcov, b1concurrent, b1cov, b1covrange, b1degrange, b1degree, b1dsp, b1factor, b1factordistinct, b1mindegree, b1nodematch, b1sociality, b1star, b1starmix, b1twostar, b2concurrent, b2cov, b2covrange, b2degrange, b2degree, b2dsp, b2factor, b2factordistinct, b2mindegree, b2nodematch, b2sociality, b2star, b2starmix, b2twostar, balance, coincidence, concurrent, concurrentties, ctriples, cycle, cyclicalities, degcor, degcrossprod, degrange, degree, degree1.5, density, diff, dsp, dyadcov, edgescov, edges, esp, gwbldegree, gwbldsp, gwbl2degree, gwbl2dsp, gwdegree, gwdsp, gwespc, gwdegree, gwncsp, gwodegree, hamming, idegrange, idegree, idegree1.5, intransitive, isolatededges, isolates, istar, kstar, localtriangle, m2star, meandeg, mm, mutual, nearsimmelian, nodecov, nodecovrange, nodefactor, nodefactordistinct, nodeicov, nodeicovrange, nodeifactor, nodeifactordistinct, nodematch, nodemix, nodecov, nodecovrange, nodeofactor, nodeofactordistinct, nsp, odegrange, odegree, odegree1.5, opentriad, ostar, receiver, sender, simmelian, simmeliانتies, smalldiff, sociality, threetrail, transitive, transitivityes, triadcensus, triangle, tripercents, ttriple, twopath

**bipartite** Project, b1concurrent, b1cov, b1covrange, b1degrange, b1degree, b1dsp, b1factor, b1factordistinct, b1mindegree, b1nodematch, b1sociality, b1star, b1starmix, b1twostar, b2concurrent, b2cov, b2covrange, b2degrange, b2degree, b2dsp, b2factor, b2factordistinct, b2mindegree, b2nodematch, b2sociality, b2star, b2starmix, b2twostar, coincidence, diff, gwbldegree, gwbldsp, gwbl2degree, gwbl2dsp, isolatededges

**directed** Symmetrize, absdiff, absdiffcat, asymmetric, atleast, atmost, attrcov, balance, cdf, ctriples, cycle, cyclicalities, cyclicalweights, density, diff, dsp, dyadcov, edgescov, edges, equalto, esp, greaterthan, gwdsp, gwespc, gwdegree, gwncsp, gwodegree, hamming, idegrange, idegree, idegree1.5, ininterval, intransitive, isolates, istar, localtriangle, m2star, meandeg, mm,

mutual, nearsimmelian, nodecov, nodecovrange, nodefactor, nodefactordistinct, nodeicov, nodeicovar, nodeicovrange, nodeifactor, nodeifactordistinct, nodematch, nodemix, nodeocov, nodeocovar, nodeocovrange, nodeofactor, nodeofactordistinct, nsp, odegrange, odegree, odegree1.5, ostar, receiver, sender, simmelian, simmelianties, smalldiff, smallerthan, sum, thretrail, transitive, transitivities, transitivityweights, triadcensus, triangle, ttriple, twopath

**dyad-independent** absdiff, absdiffcat, asymmetric, atleast, atmost, attrcov, b1cov, b1factor, b1nodematch, b1sociality, b2cov, b2factor, b2nodematch, b2sociality, cdf, density, diff, dyadcov, edgescov, edges, equalto, greaterthan, hamming, ininterval, meandeg, mm, nodecov, nodefactor, nodeifactor, nodematch, nodemix, nodeocov, nodeofactor, receiver, sender, smalldiff, smallerthan, sociality

**quantitative nodal attribute** absdiff, b1cov, b1covrange, b2cov, b2covrange, diff, nodecov, nodecovrange, nodeicov, nodeicovrange, nodeocov, nodeocovrange, smalldiff

**undirected** absdiff, absdiffcat, altkstar, atleast, atmost, attrcov, b1concurrent, b1cov, b1degrange, b1degree, b1dsp, b1factor, b1mindegree, b1nodematch, b1sociality, b1star, b1starmix, b1twostar, b2concurrent, b2cov, b2degrange, b2degree, b2dsp, b2factor, b2mindegree, b2nodematch, b2sociality, b2star, b2starmix, b2twostar, balance, cdf, coincidence, concurrent, concurrentties, cycle, cyclicalities, cyclicalweights, degcor, degcrossprod, degrange, degree, degree1.5, density, diff, dyadcov, edgescov, edges, equalto, greaterthan, gwbldegree, gwbldsp, gwbd2degree, gwbd2dsp, gwdegree, hamming, ininterval, isolatededges, isolates, kstar, localtriangle, meandeg, mm, nodecov, nodecovar, nodecovrange, nodefactor, nodefactordistinct, nodematch, nodemix, opentriad, smalldiff, smallerthan, sociality, sum, thretrail, transitivities, transitivityweights, triadcensus, triangle, tripercent, twopath

**categorical nodal attribute** absdiffcat, altkstar, b1concurrent, b1degree, b1factor, b1factordistinct, b1nodematch, b1star, b1starmix, b1twostar, b2degree, b2factor, b2factordistinct, b2nodematch, b2star, b2starmix, b2twostar, concurrent, concurrentties, ctriple, degrange, degree, idegrange, idegree, istar, kstar, mm, nodefactor, nodefactordistinct, nodeifactor, nodeifactordistinct, nodematch, nodemix, nodeofactor, nodeofactordistinct, odegrange, odegree, ostar, sociality, transitivities, triangle, tripercent, ttriple

**curved** altkstar, gwbldegree, gwbldsp, gwbd2degree, gwbd2dsp, gwdegree, gwdegree, gwdegree

**triad-related** asymmetric, balance, ctriple, intransitive, localtriangle, nearsimmelian, opentriad, simmelian, simmelianties, thretrail, transitive, transitivities, transitivityweights, triadcensus, triangle, tripercent, ttriple

**frequently-used** b1cov, b1degree, b1factor, b1nodematch, b2concurrent, b2cov, b2degree, b2factor, b2nodematch, degree, diff, edgescov, gwdegree, idegree, isolates, mm, mutual, nodecov, nodefactor, nodeicov, nodeifactor, nodematch, nodemix, odegree, triangle

**nonnegative** cyclicalweights, transitivityweights

**quantitative dyadic attribute** dyadcov, edgescov

**categorical dyadic attribute** localtriangle

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### See Also

[ergm](#) package, [search.ergmTerms](#), [ergm](#), [network](#), [%v%](#), [%n%](#)

### Examples

```
## Not run:
```

```

ergm(flomarriage ~ kstar(1:2) + absdiff("wealth") + triangle)

ergm(molecule ~ edges + kstar(2:3) + triangle
      + nodematch("atomic type",diff=TRUE)
      + triangle + absdiff("atomic type"))

## End(Not run)

```

---

ergm\_MCMC\_sample

*Internal Function to Sample Networks and Network Statistics*


---

## Description

This is an internal function, not normally called directly by the user. The `ergm_MCMC_sample` function samples networks and network statistics using an MCMC algorithm via `MCMC_wrapper` and is capable of running in multiple threads using `ergm_MCMC_slave`.

The `ergm_MCMC_slave` function calls the actual C routine and does minimal preprocessing.

## Usage

```

ergm_MCMC_sample(
  state,
  control,
  theta = NULL,
  verbose = FALSE,
  ...,
  eta = ergm.eta(theta, (if (is.ergm_state(state)) as.ergm_model(state) else
    as.ergm_model(state[[1]]))$etamap)
)

ergm_MCMC_slave(
  state,
  eta,
  control,
  verbose,
  ...,
  burnin = NULL,
  samplesize = NULL,
  interval = NULL
)

```

## Arguments

`state` an `ergm_state` representing the sampler state, containing information about the network, the model, the proposal, and (optionally) initial statistics, or a list thereof.

control	A list of control parameters for algorithm tuning, typically constructed with <code>control.ergm()</code> , <code>control.simulate.ergm()</code> , etc., which have different defaults. Their documentation gives the the list of recognized control parameters and their meaning. The more generic utility <code>snctrl()</code> (StatNet ConTRoL) also provides argument completion for the available control functions and limited argument name checking.
theta	the (possibly curved) parameters of the model.
verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
...	additional arugments.
eta	the natural parameters of the model; by default constructed from theta.
burnin, samplesize, interval	MCMC paramters that can be used to temporarily override those in the control list.

### Value

`ergm_MCMC_sample` returns a list containing:

stats	an <code>mcmc.list</code> with sampled statistics.
networks	a list of final sampled networks, one for each thread.
status	status code, propagated from <code>ergm_MCMC_slave()</code> .
final.interval	adaptively determined MCMC interval.
final.effectiveSize	adaptively determined target ESS (non-trivial if <code>control\$MCMC.effectiveSize</code> is specified via a matrix).
sampnetworks	If <code>control\$MCMC.save_networks</code> is set and is TRUE, a list of lists of <code>ergm_states</code> corresponding to the sampled networks.

`ergm_MCMC_slave` returns the MCMC sample as a list of the following:

s	the matrix of statistics.
state	an <code>ergm_state</code> object for the new network.
status	success or failure code: 0 is success, 1 for too many edges, and 2 for a Metropolis-Hastings proposal failing, -1 for <code>ergm_model</code> or <code>ergm_proposal</code> not passed and missing from the cache.

### Note

`ergm_MCMC_sample` and `ergm_MCMC_slave` replace `ergm.getMCMCsample` and `ergm.mcmcslave` respectively. They differ slightly in their argument names and in their return formats. For example, `ergm_MCMC_sample` expects `ergm_state` rather than `network/model/proposal`, and `theta` or `eta` rather than `eta0`; and it does not return `statsmatrix` or `newnetwork` elements. Rather, if parallel processing is not in effect, `stats` is an `mcmc.list` with one chain and `networks` is a list with one element.

Note that unless `stats` is a part of the `ergm_state`, the returned stats will be relative to the original network, i.e., the calling function must shift the statistics if required.

At this time, repeated calls to `ergm_MCMC_sample` will not produce the same sequence of networks as a single long call, even with the same starting seeds. This is because the network sampling algorithms rely on the internal state of the network representation in C, which may not be reconstructed exactly the same way when "resuming". This behaviour may change in the future.

## Examples

```
# This example illustrates constructing "ingredients" for calling
# ergm_MCMC_sample() from calls to simulate.ergm(). One can also
# construct an ergm_state object directly from ergm_model(),
# ergm_proposal(), etc., but the approach shown here is likely to
# be the least error-prone and the most robust to future API
# changes.
#
# The regular simulate() call hierarchy is
#
# simulate_formula.network(formula) ->
#   simulate.ergm_model(ergm_model) ->
#     simulate.ergm_state_full(ergm_state)
#
# They take an argument, return.args=, that will interrupt the call
# and have it return its arguments. We can use it to obtain
# low-level inputs robustly.

data(florentine)
control <- control.simulate(MCMC.burnin = 2, MCMC.interval = 1)

# FYI: Obtain input for simulate.ergm_model():
sim.mod <- simulate(flomarriage~absdiff("wealth"), constraints=~edges,
                  coef = NULL, nsim=3, control=control,
                  return.args="ergm_model")
names(sim.mod)
str(sim.mod$object,1) # ergm_model

# Obtain input for simulate.ergm_state_full():
sim.state <- simulate(flomarriage~absdiff("wealth"), constraints=~edges,
                    coef = NULL, nsim=3, control=control,
                    return.args="ergm_state")
names(sim.state)
str(sim.state$object, 1) # ergm_state

# This control parameter would be set by nsim in the regular
# simulate() call:
control$MCMC.samplesize <- 3

# Capture intermediate networks; can also be left NULL for just the
# statistics:
control$MCMC.save_networks <- TRUE
```

```

# Simulate starting from this state:
out <- ergm_MCMC_sample(sim.state$object, control, theta = -1, verbose=6)
names(out)
out$stats # Sampled statistics
str(out$networks, 1) # Updated ergm_state (one per thread)
# List (an element per thread) of lists of captured ergm_states,
# one for each sampled network:
str(out$sampnetworks, 2)
lapply(out$sampnetworks[[1]], as.network) # Converted to networks.

# One more, picking up where the previous sampler left off, but see Note:
control$MCMC.samplesize <- 1
str(ergm_MCMC_sample(out$networks, control, theta = -1, verbose=6), 2)

```

---

ergm\_plot.mcmc.list    *Plot MCMC list using lattice package graphics*

---

## Description

Plot MCMC list using lattice package graphics

## Usage

```
ergm_plot.mcmc.list(x, main = NULL, vars.per.page = 3, ...)
```

## Arguments

x	an <code>mcmc.list</code> object containing the mcmc diagnostic samples.
main	character, main plot heading title.
vars.per.page	Number of rows (one variable per row) per plotting page. Ignored if <code>latticeExtra</code> package is not installed.
...	additional arguments, currently unused.

## Note

This is not a method at this time.

---

ergm\_state\_cache      *A rudimentary cache for large objects*

---

### Description

This cache is intended to store large, infrequently changing data structures such as [ergm\\_models](#) and [ergm\\_proposals](#) on worker nodes.

### Usage

```
ergm_state_cache(
  comm = c("pass", "all", "clear", "insert", "get", "check", "list"),
  key,
  object
)
```

### Arguments

comm	a character string giving the desired function; see the default argument above for permitted values and Details for meanings; partial matching is supported.
key	a character string, typically a <code>digest::digest()</code> of the object or a random string.
object	the object to be stored.

Supported tasks are, respectively, to do nothing (the default), return all entries (mainly useful for testing), clear the cache, insert into cache, retrieve an object by key, check if a key is present, or list keys defined.

Deleting an entry can be accomplished by inserting a NULL for that key.

Cache is limited to a hard-coded size (currently 4). This should accommodate an [ergm\\_model](#) and an [ergm\\_proposal](#) for unconstrained and constrained MCMC. When additional objects are stored, the oldest object is purged and garbage-collected.

### Note

If called via, say, `clusterMap(cl, ergm_state_cache, ...)` the function will not accomplish anything. This is because `parallel` package will serialise the `ergm_state_cache()` function object, send it to the remote node, evaluate it there, and fetch the return value. This will leave the environment of the worker's `ergm_state_cache()` unchanged. To actually evaluate it on the worker nodes, it is recommended to wrap it in an empty function whose environment is set to `globalenv()`. See Examples below.

### Examples

```
## Not run:
# Wrap ergm_state_cache() and call it explicitly from ergm:
call_ergm_state_cache <- function(...) ergm::ergm_state_cache(...)
```

```

# Reset the function's environment so that it does not get sent to
# worker nodes (who have their own instance of ergm namespace
# loaded).
environment(call_ergm_state_cache) <- globalenv()

# Now, call the the wrapper function, with ... below replaced by
# lists of desired arguments.
clusterMap(cl, call_ergm_state_cache, ...)

## End(Not run)

```

---

ergm\_symmetrize      *Return a symmetrized version of a binary network*

---

## Description

Return a symmetrized version of a binary network

## Usage

```

ergm_symmetrize(x, rule = c("weak", "strong", "upper", "lower"), ...)

## Default S3 method:
ergm_symmetrize(x, rule = c("weak", "strong", "upper", "lower"), ...)

## S3 method for class 'network'
ergm_symmetrize(x, rule = c("weak", "strong", "upper", "lower"), ...)

```

## Arguments

x	an object representing a network.
rule	a string specifying how the network is to be symmetrized; see <a href="#">sna::symmetrize()</a> for details; for the <a href="#">network</a> method, it can also be a function or a list; see Details.
...	additional arguments to <a href="#">sna::symmetrize()</a> .

## Details

The [network](#) method requires more flexibility, in order to specify how the edge attributes are handled. Therefore, rule can be one of the following types:

- a character vector** The string is interpreted as in [sna::symmetrize\(\)](#). For edge attributes, "weak" takes the maximum value and "strong" takes the minimum value" for ordered attributes, and drops the unordered.
- a function** The function is evaluated on a [data.frame](#) constructed by joining (via [merge\(\)](#)) the edge [tibble](#) with all attributes and NA indicators with itself reversing tail and head columns, and appending original columns with ".th" and the reversed columns with ".ht". It is then evaluated for each attribute in turn, given two arguments: the data frame and the name of the attribute.

**a list** The list must have exactly one unnamed element, and the remaining elements must be named with the names of edge attributes. The elements of the list are interpreted as above, allowing each edge attribute to be handled differently. Unnamed arguments are dropped.

### Methods (by class)

- `ergm_symmetrize(default)`: The default method, passing the input on to `sna::symmetrize()`.
- `ergm_symmetrize(network)`: A method for `network` objects, which preserves network and vertex attributes, and handles edge attributes.

### Note

This was originally exported as a generic to overwrite `sna::symmetrize()`. By developer's request, it has been renamed; eventually, `sna` or `network` packages will export the generic instead.

### Examples

```
data(sampson)
samplike[1,2] <- NA
samplike[4.1] <- NA
sm <- as.matrix(samplike)

tst <- function(x,y){
  mapply(identical, x, y)
}

stopifnot(all(tst(as.logical(as.matrix(ergm_symmetrize(samplike, "weak"))), sm | t(sm))),
  all(tst(as.logical(as.matrix(ergm_symmetrize(samplike, "strong"))), sm & t(sm))),
  all(tst(c(as.matrix(ergm_symmetrize(samplike, "upper")),
    sm[cbind(c(pmin(row(sm), col(sm))), c(pmax(row(sm), col(sm)))]))),
  all(tst(c(as.matrix(ergm_symmetrize(samplike, "lower")),
    sm[cbind(c(pmax(row(sm), col(sm))), c(pmin(row(sm), col(sm)))])])))))
```

---

esp-ergmTerm

*Directed edgewise shared partners*

---

### Description

This term adds one network statistic to the model for each element in `d` where the  $i$ th such statistic equals the number of edges in the network with exactly `d[i]` shared partners.

### Usage

```
# binary: desp(d, type="OTP")

# binary: esp(d, type="OTP")
```

## Arguments

d	a vector of distinct integers
type	A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

## Shared partner types

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the `type` argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the `relevent` package):

- **Outgoing Two-path ("OTP"):** vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- **Incoming Two-path ("ITP"):** vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- **Reciprocated Two-path ("RTP"):** vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .
- **Outgoing Shared Partner ("OSP"):** vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- **Incoming Shared Partner ("ISP"):** vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

## Note

This term takes an additional term option (see `options?ergm`), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

This term can only be used with directed networks.

## References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

## See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

Exp-ergmTerm	<i>Exponentiate a network's statistic</i>
--------------	---

---

**Description**

Evaluate the terms specified in `formula` and exponentiates them with base  $e$ .

**Usage**

```
# binary: Exp(formula)
```

```
# valued: Exp(formula)
```

**Arguments**

`formula` a one-sided `ergm()`-style formula with the terms to be evaluated

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

F-ergmTerm	<i>Filtering on arbitrary one-term model</i>
------------	--

---

**Description**

Evaluates the given formula on a network constructed by taking  $y$  and removing any edges for which  $f_{i,j}(y_{i,j}) = 0$ .

**Usage**

```
# binary: F(formula, filter)
```

**Arguments**

`formula` a one-sided `ergm()`-style formula with the terms to be evaluated  
`filter` must contain one binary `ergm` term, with the following properties:

- dyadic independence;
- dyadwise contribution of 0 for a 0-valued dyad.

Formally, this means that it is expressible as

$$g(y) = \sum_{i,j} f_{i,j}(y_{i,j}),$$

where for all  $i, j$ , and  $y$ ,  $f_{i,j}(y_{i,j})$  for which  $f_{i,j}(0) = 0$ . For convenience, the term in specified can be a part of a simple logical or comparison operation: (e.g., `~!nodematch("A")` or `~abs("X")>3`), which filters on  $f_{i,j}(y_{i,j}) \circ 0$  instead.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary

---

faux.desert.high

*Faux desert High School as a network object*

---

**Description**

This data set represents a simulation of a directed in-school friendship network. The network is named faux.desert.high.

**Usage**

```
data(faux.desert.high)
```

**Format**

faux.desert.high is a [network](#) object with 107 vertices (students, in this case) and 439 directed edges (friendship nominations). To obtain additional summary information about it, type `summary(faux.desert.high)`.

The vertex attributes are Grade, Sex, and Race. The Grade attribute has values 7 through 12, indicating each student's grade in school. The Race attribute is based on the answers to two questions, one on Hispanic identity and one on race, and takes six possible values: White (non-Hisp.), Black (non-Hisp.), Hispanic, Asian (non-Hisp.), Native American, and Other (non-Hisp.)

**Licenses and Citation**

If the source of the data set does not specified otherwise, this data set is protected by the Creative Commons License <https://creativecommons.org/licenses/by-nc-nd/2.5/>.

When publishing results obtained using this data set, the original authors (Resnick et al. 1997) should be cited. In addition this package should be cited as:

Mark S. Handcock, David R. Hunter, Carter T. Butts, Steven M. Goodreau, and Martina Morris. 2003 *statnet: Software tools for the Statistical Modeling of Network Data* <https://statnet.org>.

**Source**

The data set is simulation based upon an ergm model fit to data from one school community from the AddHealth Study, Wave I (Resnick et al. 1997). It was constructed as follows:

The school in question (a single school with 7th through 12th grades) was selected from the Add Health "structure files." Documentation on these files can be found here: <https://addhealth.cpc.unc.edu/documentation/codebooks/>.

The stucture file contains directed out-ties representing each instance of a student who named another student as a friend. Students could nominate up to 5 male and 5 female friends. Note that

registered students who did not take the AddHealth survey or who were not listed by name on the schools' student roster are not included in the stucture files. In addition, we removed any students with missing values for race, grade or sex.

The following `ergm()` specification was fit to the original data (with code updated for modern syntax):

```
desert.fit <- ergm(original.net ~ edges + mutual +
absdiff("grade") + nodefactor("race", base=5) + nodefactor("grade", base=3)
+ nodefactor("sex") + nodematch("race", diff = TRUE) + nodematch("grade",
diff = TRUE) + nodematch("sex", diff = FALSE) + idegree(0:1) + odegree(0:1)
+ gwesp(0.1, fixed=T), constraints = ~bd(maxout=10), control =
control.ergm(MCMLE.steplength = .25, MCMC.burnin = 100000, MCMC.interval =
10000, MCMC.samplesize = 2500, MCMLE.maxit = 100), verbose=T)
```

Then the `faux.desert.high` dataset was created by simulating a single network from the above model fit:

```
faux.desert.high <- simulate(desert.fit, nsim=1,
control=snctrl(MCMC.burnin=1e+8),
constraints = ~edges)
```

## References

Resnick MD, Bearman PS, Blum RW, Bauman KE, Harris KM, Jones J, Tabor J, Beuhring T, Sieving RE, Shew M, Ireland M, Bearinger LH, Udry JR (1997). "Protecting Adolescents from Harm: Findings from the National Longitudinal Study on Adolescent Health." *Journal of the American Medical Association*, **278**(10), 823–832. doi:10.1001/jama.1997.03550100049038.

## See Also

`network`, `plot.network()`, `ergm()`, `faux.desert.high`, `faux.mesa.high`, `faux.magnolia.high`

---

`faux.dixon.high`

*Faux dixon High School as a network object*

---

## Description

This data set represents a simulation of a directed in-school friendship network. The network is named `faux.dixon.high`.

## Usage

```
data(faux.dixon.high)
```

## Format

faux.dixon.high is a `network` object with 248 vertices (students, in this case) and 1197 directed edges (friendship nominations). To obtain additional summary information about it, type `summary(faux.dixon.high)`.

The vertex attributes are Grade, Sex, and Race. The Grade attribute has values 7 through 12, indicating each student's grade in school. The Race attribute is based on the answers to two questions, one on Hispanic identity and one on race, and takes six possible values: White (non-Hisp.), Black (non-Hisp.), Hispanic, Asian (non-Hisp.), Native American, and Other (non-Hisp.)

## Licenses and Citation

If the source of the data set does not specified otherwise, this data set is protected by the Creative Commons License <https://creativecommons.org/licenses/by-nc-nd/2.5/>.

When publishing results obtained using this data set, the original authors (Resnick et al. 1997) should be cited. In addition this package should be cited as:

Mark S. Handcock, David R. Hunter, Carter T. Butts, Steven M. Goodreau, and Martina Morris. 2003 *statnet: Software tools for the Statistical Modeling of Network Data* <https://statnet.org>.

## Source

The data set is simulation based upon an `ergm` model fit to data from one school community from the AddHealth Study, Wave I (Resnick et al. 1997). It was constructed as follows:

The school in question (a single school with 7th through 12th grades) was selected from the Add Health "structure files." Documentation on these files can be found here: <https://addhealth.cpc.unc.edu/documentation/codebooks/>.

The stucture file contains directed out-ties representing each instance of a student who named another student as a friend. Students could nominate up to 5 male and 5 female friends. Note that registered students who did not take the AddHealth survey or who were not listed by name on the schools' student roster are not included in the stucture files. In addition, we removed any students with missing values for race, grade or sex.

The following `ergm()` specification was fit to the original data (with code updated for modern syntax):

```
dixon.fit <- ergm(original.net ~ edges + mutual +
absdiff("grade") + nodefactor("race", base=5) + nodefactor("grade", base=3)
+ nodefactor("sex") + nodematch("race", diff = TRUE) + nodematch("grade",
diff = TRUE) + nodematch("sex", diff = FALSE) + idegree(0:1) + odegree(0:1)
+ gwesp(0.1, fixed=T), constraints = ~bd(maxout=10), control =
control.ergm(MCMLE.steplength = .25, MCMC.burnin = 100000, MCMC.interval =
10000, MCMC.samplesize = 2500, MCMLE.maxit = 100), verbose=T)
```

Then the faux.dixon.high dataset was created by simulating a single network from the above model fit:

```
faux.dixon.high <- simulate(dixon.fit, nsim=1, burnin=1e+8,
constraint = "edges")
```

## References

Resnick MD, Bearman PS, Blum RW, Bauman KE, Harris KM, Jones J, Tabor J, Beuhring T, Sieving RE, Shew M, Ireland M, Bearinger LH, Udry JR (1997). “Protecting Adolescents from Harm: Findings from the National Longitudinal Study on Adolescent Health.” *Journal of the American Medical Association*, **278**(10), 823–832. doi:10.1001/jama.1997.03550100049038.

## See Also

[network](#), [plot.network\(\)](#), [ergm\(\)](#), [faux.desert.high](#), [faux.mesa.high](#), [faux.magnolia.high](#)

---

faux.magnolia.high      *Goodreau’s Faux Magnolia High School as a network object*

---

## Description

This data set represents a simulation of an in-school friendship network. The network is named faux.magnolia.high because the school communities on which it is based are large and located in the southern US.

## Usage

```
data(faux.magnolia.high)
```

## Format

faux.magnolia.high is a [network](#) object with 1461 vertices (students, in this case) and 974 undirected edges (mutual friendships). To obtain additional summary information about it, type `summary(faux.magnolia.high)`.

The vertex attributes are Grade, Sex, and Race. The Grade attribute has values 7 through 12, indicating each student’s grade in school. The Race attribute is based on the answers to two questions, one on Hispanic identity and one on race, and takes six possible values: White (non-Hisp.), Black (non-Hisp.), Hispanic, Asian (non-Hisp.), Native American, and Other (non-Hisp.)

## Licenses and Citation

If the source of the data set does not specified otherwise, this data set is protected by the Creative Commons License <https://creativecommons.org/licenses/by-nc-nd/2.5/>.

When publishing results obtained using this data set, the original authors (Resnick et al. 1997) should be cited. In addition this package should be cited as:

Mark S. Handcock, David R. Hunter, Carter T. Butts, Steven M. Goodreau, and Martina Morris. 2003 *statnet: Software tools for the Statistical Modeling of Network Data* <https://statnet.org>.

## Source

The data set is based upon a model fit to data from two school communities from the AddHealth Study, Wave I (Resnick et al. 1997). It was constructed as follows:

The two schools in question (a junior and senior high school in the same community) were combined into a single network dataset. Students who did not take the AddHealth survey or who were not listed on the schools' student rosters were eliminated, then an undirected link was established between any two individuals who both named each other as a friend. All missing race, grade, and sex values were replaced by a random draw with weights determined by the size of the attribute classes in the school.

The following `ergm()` specification was fit to the original data:

```
magnolia.fit <- ergm (magnolia ~ edges +
  nodematch("Grade",diff=T) + nodematch("Race",diff=T) +
  nodematch("Sex",diff=F) + absdiff("Grade") + gwesp(0.25, fixed=T),
  control=control.ergm(MCMC.burnin=10000, MCMC.interval=1000, MCMLE.maxit=25,
    MCMC.samplesize=2500, MCMLE.steplength=0.25))
```

Then the `faux.magnolia.high` dataset was created by simulating a single network from the above model fit:

```
faux.magnolia.high <- simulate (magnolia.fit, nsim=1,
  control = snctrl(MCMC.burnin=10000000), constraints = ~edges)
```

## References

Resnick MD, Bearman PS, Blum RW, Bauman KE, Harris KM, Jones J, Tabor J, Beuhring T, Sieving RE, Shew M, Ireland M, Bearinger LH, Udry JR (1997). "Protecting Adolescents from Harm: Findings from the National Longitudinal Study on Adolescent Health." *Journal of the American Medical Association*, **278**(10), 823–832. doi:10.1001/jama.1997.03550100049038.

## See Also

`network`, `plot.network()`, `ergm()`, `faux.mesa.high`

---

faux.mesa.high

*Goodreau's Faux Mesa High School as a network object*

---

## Description

This data set (formerly called "fauxhigh") represents a simulation of an in-school friendship network. The network is named `faux.mesa.high` because the school community on which it is based is in the rural western US, with a student body that is largely Hispanic and Native American.

## Usage

```
data(faux.mesa.high)
```

## Format

faux.mesa.high is a `network` object with 205 vertices (students, in this case) and 203 undirected edges (mutual friendships). To obtain additional summary information about it, type `summary(faux.mesa.high)`.

The vertex attributes are Grade, Sex, and Race. The Grade attribute has values 7 through 12, indicating each student's grade in school. The Race attribute is based on the answers to two questions, one on Hispanic identity and one on race, and takes six possible values: White (non-Hisp.), Black (non-Hisp.), Hispanic, Asian (non-Hisp.), Native American, and Other (non-Hisp.)

## Licenses and Citation

If the source of the data set does not specified otherwise, this data set is protected by the Creative Commons License <https://creativecommons.org/licenses/by-nc-nd/2.5/>.

When publishing results obtained using this data set, the original authors (Resnick et al. 1997) should be cited. In addition this package should be cited as:

Mark S. Handcock, David R. Hunter, Carter T. Butts, Steven M. Goodreau, and Martina Morris. 2003 *statnet: Software tools for the Statistical Modeling of Network Data* <https://statnet.org>.

## Source

The data set is based upon a model fit to data from one school community from the AddHealth Study, Wave I (Resnick et al. 1997). It was constructed as follows:

A vector representing the sex of each student in the school was randomly re-ordered. The same was done with the students' response to questions on race and grade. These three attribute vectors were permuted independently. Missing values for each were randomly assigned with weights determined by the size of the attribute classes in the school.

The following `ergm()` specification was used to fit a model to the original data:

```
~ edges + nodefactor("Grade") + nodefactor("Race") +
nodefactor("Sex") + nodematch("Grade",diff=TRUE) +
nodematch("Race",diff=TRUE) + nodematch("Sex",diff=FALSE) +
gwdegree(1.0,fixed=TRUE) + gwesp(1.0,fixed=TRUE) + gwds(1.0,fixed=TRUE)
```

The resulting model fit was then applied to a network with actors possessing the permuted attributes and with the same number of edges as in the original data.

The processes for handling missing data and defining the race attribute are described in Hunter et al. (2008).

## References

Hunter DR, Goodreau SM, Handcock MS (2008). "Goodness of Fit for Social Network Models." *Journal of the American Statistical Association*, **103**(481), 248–258. ISSN 0162-1459. doi:10.1198/016214507000000446.

Resnick MD, Bearman PS, Blum RW, Bauman KE, Harris KM, Jones J, Tabor J, Beuhring T, Sieving RE, Shew M, Ireland M, Bearinger LH, Udry JR (1997). "Protecting Adolescents from Harm: Findings from the National Longitudinal Study on Adolescent Health." *Journal of the American Medical Association*, **278**(10), 823–832. doi:10.1001/jama.1997.03550100049038.

**See Also**

[network](#), [plot.network\(\)](#), [ergm\(\)](#), [faux.magnolia.high](#)

---

 fix.curved

---

 Convert a curved ERGM into a corresponding "fixed" ERGM.
 

---

**Description**

The generic `fix.curved` converts an [ergm](#) object or formula of a model with curved terms to the variant in which the curved parameters are fixed. Note that each term has to be treated as a special case.

**Usage**

```
fix.curved(object, ...)

## S3 method for class 'ergm'
fix.curved(object, ...)

## S3 method for class 'formula'
fix.curved(object, theta, ...)
```

**Arguments**

object	An <a href="#">ergm</a> object or an ERGM formula. The curved terms of the given formula (or the formula used in the fit) must have all of their arguments passed by name.
...	Unused at this time.
theta	Curved model parameter configuration.

**Details**

Some ERGM terms such as [gwesp](#) and [gwdegree](#) have two forms: a curved form, for which their decay or similar parameters are to be estimated, and whose canonical statistics is a vector of the term's components ([esp\(1\)](#), [esp\(2\)](#), ... and [degree\(1\)](#), [degree\(2\)](#), ..., respectively) and a "fixed" form where the decay or similar parameters are fixed, and whose canonical statistic is just the term itself. It is often desirable to fit a model estimating the curved parameters but simulate the "fixed" statistic.

This function thus takes in a fit or a formula and performs this mapping, returning a "fixed" model and parameter specification. It only works for curved ERGM terms included with the [ergm](#) package. It does not work with curved terms not included in `ergm`.

**Value**

A list with the following components:

formula	The "fixed" formula.
theta	The "fixed" parameter vector.

**See Also**

[ergm\(\)](#), [simulate.ergm\(\)](#)

**Examples**

```
data(sampson)
gest<-ergm(samplike~edges+gwesp(),
           control=control.ergm(MCMLE.maxit=2))
summary(gest)
# A statistic for esp(1),...,esp(16)
simulate(gest,output="stats")

tmp<-fix.curved(gest)
tmp
# A gwesp() statistic only
simulate(tmp$formula, coef=tmp$theta, output="stats")
```

---

fixallbut-ergmConstraint

*Preserve the dyad status in all but the given edges*

---

**Description**

Preserve the dyad status in all but free.dyads.

**Usage**

```
# fixallbut(free.dyads)
```

**Arguments**

free.dyads      a two-column edge list, a [network](#), or an [rlebdm](#). Networks will be converted to the corresponding edgelist.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

`fixedas-ergmConstraint`*Fix specific dyads*

---

**Description**

Fix the dyads in `fixed.dyads` at their current value, preserve the edges in present, and preclude the edges in absent.

**Usage**

```
# fixedas(fixed.dyads, present, absent)
```

**Arguments**

`fixed.dyads`, `present`, `absent`  
a two-column edge list or a [network](#)

**Details**

`present` and `absent` differ from `fixed.dyads` in that they check that the specified edges are in fact present and/or absent and stop with an error if not.

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

`florentine`*Florentine Family Marriage and Business Ties Data as a "network" object*

---

**Description**

This is a data set of marriage and business ties among Renaissance Florentine families. The data is originally from Padgett (1994) via UCINET and stored as a [network](#) object.

**Usage**

```
data(florentine)
```

### Details

Breiger and Pattison (1986), in their discussion of local role analysis, use a subset of data on the social relations among Renaissance Florentine families (person aggregates) collected by John Padgett from historical documents. The two relations are business ties (flobusiness - specifically, recorded financial ties such as loans, credits and joint partnerships) and marriage alliances (flomarriage).

As Breiger & Pattison point out, the original data are symmetrically coded. This is acceptable perhaps for marital ties, but is unfortunate for the financial ties (which are almost certainly directed). To remedy this, the financial ties can be recoded as directed relations using some external measure of power - for instance, a measure of wealth. Both graphs provide vertex information on (1) wealth each family's net wealth in 1427 (in thousands of lira); (2) priorates the number of priorates (seats on the civic council) held between 1282- 1344; and (3) totalties the total number of business or marriage ties in the total dataset of 116 families (see Breiger and Pattison 1986, p 239).

Substantively, the data include families who were locked in a struggle for political control of the city of Florence around 1430. Two factions were dominant in this struggle: one revolved around the infamous Medicis (9), the other around the powerful Strozis (15).

### Source

(Padgett 1994).

### References

Breiger RL, Pattison PE (1986). "Cumulated Social Roles: The Duality of Persons and their Algebras." *Social Networks*, 8(3), 215–256. doi:10.1016/03788733(86)900067.

Padgett JF (1994). "Marriage and Elite Structure in Renaissance Florence, 1282-1500." Paper delivered to the Social Science History Association.

Wasserman S, Faust K (1994). *Social Network Analysis: Methods and Applications*. Cambridge University Press, Cambridge, England. doi:10.1017/CBO9780511815478.

### See Also

flo, network, plot.network, ergm

---

For-ergmTerm

A *for* operator for terms

---

### Description

This operator evaluates the formula given to it, substituting the specified loop counter variable with each element in a sequence.

### Usage

```
# binary: For(...)
```

```
# valued: For(...)
```

## Arguments

- ... in any order,
- one *unnamed* one-sided `ergm()`-style formula with the terms to be evaluated, containing one or more placeholders *VAR* and
  - one or more *named* expressions of the form `VAR = SEQ` specifying the placeholder and its range. See Details below.

## Details

Placeholders are specified in the style of `foreach::foreach()`, as `VAR = SEQ`. `VAR` can be any valid R variable name, and `SEQ` can be a vector, a list, a function of one argument, or a one-sided formula. The vector or list will be used directly, whereas a function will be called with the network as its argument to produce the list, and the formula will be used analogously to `purrr::as_mapper()`, its RHS evaluated in an environment in which the network itself will be accessible as `.` or `.nw`.

If more than one named expression is given, they will be expanded as one would expect in a nested `for` loop: earlier expressions will form the outer loops and later expressions the inner loops.

## See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

## Examples

```
#
# The following are equivalent ways to compute differential
# homophily.
#

data(sampson)
(groups <- sort(unique(samplike%v%"group"))) # Sorted list of groups.

# The "normal" way:
summary(samplike ~ nodematch("group", diff=TRUE))

# One element at a time, specifying a list:
summary(samplike ~ For(~nodematch("group", levels=., diff=TRUE),
  . = groups))

# One element at a time, specifying a function that returns a list:
summary(samplike ~ For(~nodematch("group", levels=., diff=TRUE),
  . = function(nw) sort(unique(nw%v%"group"))))

# One element at a time, specifying a formula whose RHS expression
# returns a list:
summary(samplike ~ For(~nodematch("group", levels=., diff=TRUE),
  . = ~sort(unique(.%v%"group"))))
```

```

#
# Multiple iterators are possible, in any order. Here, absdiff() is
# being computed for each combination of attribute and power.
#

data(florentine)

# The "normal" way:
summary(flomarriage ~ absdiff("wealth", pow=1) + absdiff("priorates", pow=1) +
        absdiff("wealth", pow=2) + absdiff("priorates", pow=2) +
        absdiff("wealth", pow=3) + absdiff("priorates", pow=3))

# With a loop; note that the attribute (a) is being iterated within
# power (.):
summary(flomarriage ~ For(. = 1:3, a = c("wealth", "priorates"), ~absdiff(a, pow=.)))

```

---

g4

*Goodreau's four node network as a "network" object*


---

## Description

This is an example thought of by Steve Goodreau. It is a directed network of four nodes and five ties stored as a [network](#) object.

## Usage

```
data(g4)
```

## Details

It is interesting because the maximum likelihood estimator of the model with out degree 3 in it exists, but the maximum pseudolikelihood estimator does not.

## Source

Steve Goodreau

## See Also

[florentine](#), [network](#), [plot.network](#), [ergm](#)

## Examples

```

data(g4)
summary(ergm(g4 ~ odegree(3), estimate="MPLE"))
summary(ergm(g4 ~ odegree(3), control=control.ergm(init=0)))

```

---

geweke.diag.mv	<i>Multivariate version of coda's <code>coda::geweke.diag()</code>.</i>
----------------	---

---

### Description

Rather than comparing each mean independently, compares them jointly. Note that it returns an `htest` object, not a `geweke.diag` object.

### Usage

```
geweke.diag.mv(x, frac1 = 0.1, frac2 = 0.5, split.mcmc.list = FALSE, ...)
```

### Arguments

<code>x</code>	an <code>mcmc</code> , <code>mcmc.list</code> , or just a matrix with observations in rows and variables in columns.
<code>frac1</code> , <code>frac2</code>	the fraction at the start and, respectively, at the end of the sample to compare.
<code>split.mcmc.list</code>	when given an <code>mcmc.list</code> , whether to test each chain individually.
<code>...</code>	additional arguments, passed on to <code>approx.hotelling.diff.test()</code> , which passes them to <code>spectrum0.mvar()</code> , etc.; in particular, <code>order.max=</code> can be used to limit the order of the AR model used to estimate the effective sample size.

### Value

An object of class `htest`, inheriting from that returned by `approx.hotelling.diff.test()`, but with p-value considered to be 0 on insufficient sample size.

### Note

If `approx.hotelling.diff.test()` returns an error, then assume that burn-in is insufficient.

### See Also

`coda::geweke.diag()`, `approx.hotelling.diff.test()`

---

gof *Conduct Goodness-of-Fit Diagnostics on a Exponential Family Random Graph Model*

---

### Description

`gof()` calculates  $p$ -values for a variety of network features to diagnose the goodness-of-fit of exponential family random graph models. For binary networks, these default to geodesic distance, degree, and reachability summaries. See `ergm()` for more information on these models.

### Usage

```
gof(object, ...)

## S3 method for class 'ergm'
gof(
  object,
  ...,
  coef = coefficients(object),
  GOF = NULL,
  response = object$network %ergmlhs% "response",
  reference = object$reference,
  constraints = object$constraints,
  control = control.gof.ergm(),
  verbose = FALSE
)

## S3 method for class 'formula'
gof(
  object,
  ...,
  coef = NULL,
  GOF = NULL,
  response = NULL,
  reference = NULL,
  constraints = NULL,
  basis = eval_lhs.formula(object),
  control = NULL,
  unconditional = TRUE,
  verbose = FALSE
)

## S3 method for class 'gof'
print(x, ...)

## S3 method for class 'gof'
plot(
```

```

x,
...,
cex.axis = 0.7,
plotlogodds = FALSE,
main = "Goodness-of-fit diagnostics",
normalize.reachability = FALSE,
verbose = FALSE
)

```

## Arguments

object	Either a formula or an <a href="#">ergm</a> object. See documentation for <a href="#">ergm()</a> .
...	Additional arguments, to be passed to lower-level functions.
coef	When given either a formula or an object of class <code>ergm</code> , <code>coef</code> are the parameters from which the sample is drawn. By default set to a vector of 0. If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
GOF	<p>formula; a one-sided formula, of the form <code>~ &lt;model terms&gt;</code> specifying the statistics to use to diagnosis the goodness-of-fit of the model. They do not need to be in the model formula specified in <code>formula</code>, and typically are not. These can be any <code>ergm()</code> terms, but the following are given special meaning:</p> <p><b>the degree distribution</b> <code>degree</code> for undirected graphs, <code>idegree</code> and/or <code>odegree</code> for directed graphs, and <code>b1degree</code> and <code>b2degree</code> for bipartite undirected graphs</p> <p><b>geodesic distances</b> <code>distance</code></p> <p><b>shared partner distributions</b> <code>espartners</code> and <code>dspartners</code></p> <p><b>triad census</b> <code>triadcensus</code></p> <p><b>the cumulative distribution function of edge values</b> <code>cdf(min, max, step, margin, nmax)</code>, which will be autodetected from the observed network (using <code>margin</code> and <code>nmax</code> if possible)</p> <p><b>terms of the original model</b> <code>model</code></p> <p>The default formula for undirected networks is <code>~ degree + espartners + distance + model</code>, for directed networks <code>~ idegree + odegree + espartners + distance + model</code>, and for bipartite <code>~b1degree + b2degree + dspartners + distance</code>. For valued networks, only <code>~cdf</code> is calculated, regardless of directedness. By default a <code>model</code> term is added to the formula. It is a very useful overall validity check and a reminder of the statistical variation in the estimates of the mean value parameters. To omit the <code>model</code> term, add <code>- model</code> to the formula.</p> <p>Ordinary <code>ergm()</code> terms can also be given on the formula; if present, they will be returned as "user" statistics.</p>
response, reference, constraints	See analogous arguments for <a href="#">simulate.ergm()</a> .
control	A list of control parameters for algorithm tuning, typically constructed with <a href="#">control.gof.formula()</a> or <a href="#">control.gof.ergm()</a> , which have different defaults. Their documentation gives the the list of recognized control parameters

	and their meaning. The more generic utility <code>snctrl()</code> (StatNet ConTRoL) also provides argument completion for the available control functions and limited argument name checking.
<code>verbose</code>	A logical or an integer to control the amount of progress and diagnostic information to be printed. <code>FALSE/0</code> produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
<code>basis</code>	a value (usually a <code>network</code> ) to override the LHS of the formula.
<code>unconditional</code>	logical; if <code>TRUE</code> , the simulation is unconditional on the observed dyads. if not <code>TRUE</code> , the simulation is conditional on the observed dyads. This is primarily used internally when the network has missing data and a conditional GoF is produced.
<code>x</code>	an object of class <code>gof</code> for printing or plotting.
<code>cex.axis</code>	Character expansion of the axis labels relative to that for the plot.
<code>plotlogodds</code>	Plot the odds of a dyad having given characteristics (e.g., reachability, minimum geodesic distance, shared partners). This is an alternative to the probability of a dyad having the same property.
<code>main</code>	Title for the goodness-of-fit plots.
<code>normalize.reachability</code>	Should the reachability proportion be normalized to make it more comparable with the other geodesic distance proportions.

## Details

A sample of graphs is randomly drawn from the specified model. The first argument is typically the output of a call to `ergm()` and the model used for that call is the one fit.

For `GOF = ~model`, the model's observed sufficient statistics are plotted as quantiles of the simulated sample. In a good fit, the observed statistics should be near the sample median (0.5).

By default, the sample consists of 100 simulated networks, but this sample size (and many other settings) can be changed using the control argument described above.

## Value

`gof()`, `gof.ergm()`, and `gof.formula()` return an object of class `gof.ergm`, which inherits from class `gof`. This is a list of the tables of statistics and *p*-values. This is typically plotted using `plot.gof()`.

## Methods (by class)

- `gof(ergm)`: Perform simulation to evaluate goodness-of-fit for a specific `ergm()` fit.
- `gof(formula)`: Perform simulation to evaluate goodness-of-fit for a model configuration specified by a `formula`, coefficient, constraints, and other settings.

**Methods (by generic)**

- `print(gof)`: `print.gof()` summaries the diagnostics such as the degree distribution, geodesic distances, shared partner distributions, and reachability for the goodness-of-fit of exponential family random graph models. (`summary.gof` is a deprecated alias that may be repurposed in the future.)
- `plot(gof)`: `plot.gof()` plots diagnostics such as the degree distribution, geodesic distances, shared partner distributions, and reachability for the goodness-of-fit of exponential family random graph models.

**See Also**

`ergm()`, `network()`, `simulate.ergm()`, `summary.ergm()`

**Examples**

```
data(florentine)
gest <- ergm(flomarriage ~ edges + kstar(2))
gest
summary(gest)

# test the gof.ergm function
gofflo <- gof(gest)
gofflo

# Plot all three on the same page
# with nice margins
par(mfrow=c(1,3))
par(oma=c(0.5,2,1,0.5))
plot(gofflo)

# And now the log-odds
plot(gofflo, plotlogodds=TRUE)

# Use the formula version of gof
gofflo2 <- gof(flomarriage ~ edges + kstar(2), coef=c(-1.6339, 0.0049))
plot(gofflo2)
```

---

greaterthan-ergmTerm *Number of dyads with values strictly greater than a threshold*

---

**Description**

Adds the number of statistics equal to the length of threshold equaling to the number of dyads whose values exceed the corresponding element of threshold .

**Usage**

```
# valued: greaterthan(threshold=0)
```

**Arguments**

threshold      a vector of numerical values

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

gwb1degree-ergmTerm	<i>Geometrically weighted degree distribution for the first mode in a bipartite network</i>
---------------------	---

---

**Description**

This term adds one network statistic to the model equal to the weighted degree distribution with decay controlled by the decay parameter, which should be non-negative, for nodes in the first mode of a bipartite network. The first mode of a bipartite network object is sometimes known as the "actor" mode.

This term can only be used with undirected bipartite networks.

**Usage**

```
# binary: gwb1degree(decay, fixed=FALSE, attr=NULL, cutoff=30, levels=NULL)
```

**Arguments**

decay	nonnegative decay parameter for the first mode degree frequencies; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Hancock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
cutoff	This optional argument sets the number of underlying degree terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
levels	TODO (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, curved, undirected, binary

---

gwb1dsp-ergmTerm	<i>Geometrically weighted dyadwise shared partner distribution for dyads in the first bipartition</i>
------------------	---

---

**Description**

This term adds one network statistic to the model equal to the geometrically weighted dyadwise shared partner distribution for dyads in the first bipartition with decay parameter decay parameter, which should be non-negative. This term can only be used with bipartite networks.

**Usage**

```
# binary: gwb1dsp(decay=0, fixed=FALSE, cutoff=30)
```

**Arguments**

decay	nonnegative decay parameter for the shared partner counts; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
cutoff	This optional argument sets the number of underlying b1dsp terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)

**Note**

This term takes an additional term option (see [options?ergm](#)), cache.sp, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, curved, undirected, binary

---

gwb2degree-ergmTerm     *Geometrically weighted degree distribution for the second mode in a bipartite network*

---

### Description

This term adds one network statistic to the model equal to the weighted degree distribution with decay controlled by the decay parameter, which should be non-negative, for nodes in the second mode of a bipartite network. The second mode of a bipartite network object is sometimes known as the "event" mode.

This term can only be used with undirected bipartite networks.

### Usage

```
# binary: gwb2degree(decay, fixed=FALSE, attr=NULL, cutoff=30, levels=NULL)
```

### Arguments

decay	nonnegative decay parameter for the second mode degree frequencies; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
cutoff	This optional argument sets the number of underlying degree terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
levels	TODO (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, curved, undirected, binary

---

gwb2dsp-ergmTerm	<i>Geometrically weighted dyadwise shared partner distribution for dyads in the second bipartition</i>
------------------	--

---

### Description

This term adds one network statistic to the model equal to the geometrically weighted dyadwise shared partner distribution for dyads in the second bipartition with decay parameter decay parameter, which should be non-negative. This term can only be used with bipartite networks.

### Usage

```
# binary: gwb2dsp(decay=0, fixed=FALSE, cutoff=30)
```

### Arguments

decay	nonnegative decay parameter for the shared partner counts; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Hancock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
cutoff	This optional argument sets the number of underlying b2dsp terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)

### Note

This term takes an additional term option (see [options?ergm](#)), cache.sp, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, curved, undirected, binary

---

gwdegree-ergmTerm      *Geometrically weighted degree distribution*

---

### Description

This term adds one network statistic to the model equal to the weighted degree distribution with decay controlled by the decay parameter, which should be non-negative.

### Usage

```
# binary: gwdegree(decay, fixed=FALSE, attr=NULL, cutoff=30, levels=NULL)
```

### Arguments

decay	nonnegative decay parameter for the degree frequencies; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Hancock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
cutoff	This optional argument sets the number of underlying degree terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
levels	TODO (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** curved, frequently-used, undirected, binary

---

gwdsp-ergmTerm      *Geometrically weighted dyadwise shared partner distribution*

---

### Description

This term adds one network statistic to the model equal to the geometrically weighted dyadwise shared partner distribution with decay parameter decay parameter.

**Usage**

```
# binary: dgwdsp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

```
# binary: gwdsp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

**Arguments**

decay	nonnegative decay parameter for the shared partner or selected directed analogue count; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
cutoff	This optional argument sets the number of underlying DSP terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
type	A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

**Shared partner types**

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the type argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the relevent package):

- Outgoing Two-path ("OTP"): vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- Incoming Two-path ("ITP"): vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- Reciprocated Two-path ("RTP"): vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .
- Outgoing Shared Partner ("OSP"): vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- Incoming Shared Partner ("ISP"): vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

**Note**

This term takes an additional term option (see [options?ergm](#)), cache.sp, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

The GWDSP statistic is equal to the sum of GWNSP plus GWESP.

The decay parameter was called `alpha` prior to `ergm` 3.7.

## References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

## See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

gwesp-ergmTerm

*Geometrically weighted edgewise shared partner distribution*

---

## Description

This term adds a statistic equal to the geometrically weighted edgewise (not dyadwise) shared partner distribution with decay parameter `decay`.

## Usage

```
# binary: dgwesp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

```
# binary: gwesp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

## Arguments

<code>decay</code>	nonnegative decay parameter for the shared partner or selected directed analogue count; required if <code>fixed=TRUE</code> and ignored with a warning otherwise.
<code>fixed</code>	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is <code>FALSE</code> , which means the scale parameter is not fixed and thus the model is a curved exponential family.
<code>cutoff</code>	This optional argument sets the number of underlying ESP terms to use in computing the statistics when <code>fixed=FALSE</code> , in order to reduce the computational burden. Its default value can also be controlled by the <code>gw.cutoff</code> term option control parameter. (See <code>?control.ergm</code> .)
<code>type</code>	A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

## Shared partner types

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the `type` argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the `relevent` package):

- **Outgoing Two-path ("OTP")**: vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- **Incoming Two-path ("ITP")**: vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- **Reciprocated Two-path ("RTP")**: vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .
- **Outgoing Shared Partner ("OSP")**: vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- **Incoming Shared Partner ("ISP")**: vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

## Note

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

The decay parameter was called `alpha` prior to `ergm` 3.7.

## References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

## See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

gwidegree-ergmTerm      *Geometrically weighted in-degree distribution*

---

### Description

This term adds one network statistic to the model equal to the weighted in-degree distribution with decay parameter decay parameter, which should be non-negative. This term can only be used with directed networks.

### Usage

```
# binary: gwidegree(decay, fixed=FALSE, attr=NULL, cutoff=30, levels=NULL)
```

### Arguments

decay	nonnegative decay parameter for the indegree frequencies; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
cutoff	This optional argument sets the number of underlying degree terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
levels	TODO (See Specifying Vertex attributes and Levels (?nodal_attributes) for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** curved, directed, binary

gwnsp-ergmTerm

*Geometrically weighted non-edgewise shared partner distribution***Description**

This term is just like gwesp and gwdsp except it adds a statistic equal to the geometrically weighted nonedgewise (that is, over dyads that do not have an edge) shared partner distribution with decay parameter decay parameter.

**Usage**

```
# binary: dgwnsp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

```
# binary: gwnsp(decay, fixed=FALSE, cutoff=30, type="OTP")
```

**Arguments**

decay	nonnegative decay parameter for the shared partner or selected directed analogue count; required if fixed=TRUE and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is FALSE, which means the scale parameter is not fixed and thus the model is a curved exponential family.
cutoff	This optional argument sets the number of underlying NSP terms to use in computing the statistics when fixed=FALSE, in order to reduce the computational burden. Its default value can also be controlled by the gw.cutoff term option control parameter. (See ?control.ergm.)
type	A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

**Shared partner types**

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the type argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the relevant package):

- Outgoing Two-path ("OTP"): vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- Incoming Two-path ("ITP"): vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- Reciprocated Two-path ("RTP"): vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .

- **Outgoing Shared Partner ("OSP"):** vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- **Incoming Shared Partner ("ISP"):** vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

### Note

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

The decay parameter was called `alpha` prior to `ergm 3.7`.

### References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

gwodegree-ergmTerm      *Geometrically weighted out-degree distribution*

---

### Description

This term adds one network statistic to the model equal to the weighted out-degree distribution with decay parameter `decay`, which should be positive. This term can only be used with directed networks.

### Usage

```
# binary: gwodegree(decay, fixed=FALSE, attr=NULL, cutoff=30, levels=NULL)
```

**Arguments**

decay	nonnegative decay parameter for the outdegree frequencies; required if <code>fixed=TRUE</code> and ignored with a warning otherwise.
fixed	optional argument indicating whether the decay parameter is fixed at the given value, or is to be fit as a curved exponential-family model (see Hunter and Handcock, 2006). The default is <code>FALSE</code> , which means the scale parameter is not fixed and thus the model is a curved exponential family.
attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
cutoff	This optional argument sets the number of underlying degree terms to use in computing the statistics when <code>fixed=FALSE</code> , in order to reduce the computational burden. Its default value can also be controlled by the <code>gw.cutoff</code> term option control parameter. (See <a href="#">?control.ergm.</a> )
levels	TODO (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** curved, directed, binary

---

hamming-ergmConstraint

*Preserve the hamming distance to the given network (BROKEN: Do NOT Use)*

---

**Description**

This constraint is currently broken. Do not use.

**Usage**

```
# hamming
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, undirected

---

hamming-ergmTerm	<i>Hamming distance</i>
------------------	-------------------------

---

### Description

This term adds one statistic to the model equal to the weighted or unweighted Hamming distance of the network from the network specified by  $x$ . Unweighted Hamming distance is defined as the total number of pairs  $(i, j)$  (ordered or unordered, depending on whether the network is directed or undirected) on which the two networks differ. If the optional argument `cov` is specified, then the weighted Hamming distance is computed instead, where each pair  $(i, j)$  contributes a pre-specified weight toward the distance when the two networks differ on that pair.

### Usage

```
# binary: hamming(x, cov, attrname=NULL)
```

### Arguments

<code>x</code>	defaults to be the observed network, i.e., the network on the left side of the $\sim$ in the formula that defines the ERGM.
<code>cov</code>	either a matrix of edgewise weights or a network
<code>attrname</code>	option argument that provides the name of the edge attribute to use for weight values when a network is specified in <code>cov</code>

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, binary

---

I-ergmConstraint	<i>Substitute a formula into the constraints formula</i>
------------------	--

---

### Description

This is a convenience operator that can be used to paste terms constructed elsewhere into a formula.

### Usage

```
# I(formula)
```

### Arguments

<code>formula</code>	a constraints formula
----------------------	-----------------------

**Note**

formula can also be a [term\\_list](#).

**See Also**

[base::I\(\)](#) (a.k.a. AsIs)

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** operator

---

I-ergmTerm

*Substitute a formula into the model formula*

---

**Description**

This is a convenience operator that can be used to paste terms constructed elsewhere into a formula.

**Usage**

```
# binary: I(formula)
```

```
# valued: I(formula)
```

**Arguments**

formula            a one-sided [ergm\(\)](#)-style formula with the terms to be evaluated

**Note**

formula can also be a [term\\_list](#) or [character](#). In the latter case, if there are multiple strings, they will be concatenated with +, and if they do not start with "~", one will be prepended. Its environment will be inherited from the top-level formula.

**See Also**

[base::I\(\)](#) (a.k.a. AsIs)

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

**Examples**

```
data(florentine)

(terms <- paste0("degree(", 0:5, "))")
(s <- summary(flomarriage ~ I(terms)))
```

---

idegrange-ergmTerm      *In-degree range*

---

### Description

This term adds one network statistic to the model for each element of `from` (or `to`); the  $i$ th such statistic equals the number of nodes in the network of in-degree greater than or equal to `from[i]` but strictly less than `to[i]`, i.e. with in-edge count in semiopen interval `[from, to)`.

This term can only be used with directed networks; for undirected networks (bipartite and not) see `degrange`. For degrees of specific modes of bipartite networks, see `b1degrange` and `b2degrange`. For in-degrees, see `idegrange`.

### Usage

```
# binary: idegrange(from, to=+Inf, by=NULL, homophily=FALSE, levels=NULL)
```

### Arguments

`from`, `to`            vectors of distinct integers. If one of the vectors have length 1, it is recycled to the length of the other. Otherwise, it must have the same length.

`by`, `levels`, `homophily`      the optional argument `by` specifies a vertex attribute (see `Specifying Vertex attributes` and `Levels (?nodal_attributes)` for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

idegree-ergmTerm      *In-degree*

---

### Description

This term adds one network statistic to the model for each element in `d`; the  $i$ th such statistic equals the number of nodes in the network of in-degree `d[i]`, i.e. the number of nodes with exactly `d[i]` in-edges. This term can only be used with directed networks; for undirected networks see `degree`.

**Usage**

```
# binary: idegree(d, by=NULL, homophily=FALSE, levels=NULL)
```

**Arguments**

**d** a vector of distinct integers

**by, levels, homophily** the optional argument **by** specifies a vertex attribute (see [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details). If this is specified and **homophily** is TRUE, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the **by** attribute. If **by** is specified and **homophily** is FALSE (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. **levels** selects which levels of **by** to include.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, frequently-used, binary

idegree1.5-ergmTerm *In-degree to the 3/2 power*

**Description**

This term adds one network statistic to the model equaling the sum over the actors of each actor's indegree taken to the  $3/2$  power (or, equivalently, multiplied by its square root). This term is analogous to the term of Snijders et al. (2010), equation (12). This term can only be used with directed networks.

**Usage**

```
# binary: idegree1.5
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

idegreedist-ergmConstraint

*Preserve the indegree distribution*

---

**Description**

Preserve the indegree distribution of the given network.

**Usage**

```
# idegreedist
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed

---

idegrees-ergmConstraint

*Preserve indegree for directed networks*

---

**Description**

For directed networks, preserve the indegree of each vertex of the given network, while allowing outdegree to vary

**Usage**

```
# idegrees
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed

---

ininterval-ergmTerm *Number of dyads whose values are in an interval*

---

### Description

Adds one statistic equaling to the number of dyads whose values are between lower and upper .

### Usage

```
# valued: ininterval(lower=-Inf, upper=+Inf, open=c(TRUE,TRUE))
```

### Arguments

lower	defaults to -Inf
upper	defaults to +Inf
open	a logical vector of length 2 that controls whether the interval is open (exclusive) on the lower and on the upper end, respectively. open can also be specified as one of "[ ]" , "( )" , "[ )" , and "( )" .

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

intransitive-ergmTerm *Intransitive triads*

---

### Description

This term adds one statistic to the model, equal to the number of triads in the network that are intransitive. The intransitive triads are those of type 111D , 201 , 111U , 021C , or 030C in the categorization of Davis and Leinhardt (1972). For details on the 16 possible triad types, see `triad.classify` in the **sna** package. Note the distinction from the `ctriple` term.

### Usage

```
# binary: intransitive
```

### Note

This term can only be used with directed networks.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, binary

is.curved

*Testing for curved exponential family***Description**

These functions test whether an ERGM fit, formula, or some other object represents a curved exponential family.

The method for NULL always returns FALSE by convention.

**Usage**

```
is.curved(object, ...)

## S3 method for class '`NULL`'
is.curved(object, ...)

## S3 method for class 'formula'
is.curved(object, response = NULL, basis = NULL, ...)

## S3 method for class 'ergm'
is.curved(object, ...)
```

**Arguments**

object	An <a href="#">ergm</a> object or an ERGM formula.
...	Arguments passed on to lower-level functions.
response	Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows: NULL Model simple presence or absence, via a binary ERGM. <b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <a href="#">logical</a> (TRUE/FALSE) for binary or <a href="#">numeric</a> for valued. <b>a formula</b> must be of the form NAME~EXPR TYPE (with   being literal). EXPR is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional NAME specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of EXPR. Normally, the type of ERGM is determined by whether the result of evaluating EXPR is logical or numeric, but the optional TYPE can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).
basis	See <a href="#">ergm()</a> .

**Details**

Curvature is checked by testing if all model parameters are canonical.

**Value**

TRUE if the object represents a curved exponential family; FALSE otherwise.

---

```
is.dyad.independent    Testing for dyad-independence
```

---

**Description**

These functions test whether an ERGM fit, a formula, or some other object represents a dyad-independent model.

The method for NULL always returns TRUE by convention.

**Usage**

```
is.dyad.independent(object, ...)

## S3 method for class '`NULL`'
is.dyad.independent(object, ...)

## S3 method for class 'formula'
is.dyad.independent(object, response = NULL, basis = NULL, ...)

## S3 method for class 'ergm_conlist'
is.dyad.independent(object, object.obs = NULL, ...)

## S3 method for class 'ergm'
is.dyad.independent(object, how = c("overall", "terms", "space"), ...)
```

**Arguments**

object	The object to be tested for dyadic independence.
...	Unused at this time.
response	Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows: NULL Model simple presence or absence, via a binary ERGM. <b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <b>logical</b> (TRUE/FALSE) for binary or <b>numeric</b> for valued. <b>a formula</b> must be of the form NAME~EXPR TYPE (with   being literal). EXPR is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional NAME specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of EXPR. Normally, the type of ERGM is determined by whether the result of evaluating EXPR is logical or numeric, but the optional TYPE can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).

basis	See <code>ergm()</code> .
object.obs	For the <code>ergm_conlist</code> method, the observed data constraint.
how	one of "overall" (the default), "terms", or "space", to specify which aspect of the ERGM is to be tested for dyadic independence.

### Details

Dyad independence is determined by checking if all of the constituent parts of the object (formula, ergm terms, constraints, etc.) are flagged as dyad-independent.

### Value

TRUE if the model implied by the object is dyad-independent; FALSE otherwise.

---

is.valued	<i>Function to check whether an ERGM fit or some aspect of it is valued</i>
-----------	---

---

### Description

Function to check whether an ERGM fit or some aspect of it is valued

### Usage

```
is.valued(object, ...)

## S3 method for class 'ergm_state'
is.valued(object, ...)

## S3 method for class 'edgelist'
is.valued(object, ...)

## S3 method for class 'ergm'
is.valued(object, ...)

## S3 method for class 'network'
is.valued(object, ...)
```

### Arguments

object	the object to be tested.
...	additional arguments for methods, currently unused.

**Methods (by class)**

- `is.valued(ergm_state)`: a method for `ergm_state` objects.
- `is.valued(edgelist)`: a method for `edgelist` objects.
- `is.valued(ergm)`: a method for `ergm` objects.
- `is.valued(network)`: a method for `network` objects that tests whether the network has been instrumented with a valued `%ergmlhs%` "response" specification, typically by `ergm_preprocess_response()`. Note that it is *not* a test for whether a network has edge attributes. This method is primarily for internal use.

---

 isolatededges-ergmTerm
*Isolated edges***Description**

This term adds one statistic to the model equal to the number of isolated edges in the network, i.e., the number of edges each of whose endpoints has degree 1. This term can only be used with undirected networks.

**Usage**

```
# binary: isolatededges
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, undirected, binary

---

 isolates-ergmTerm
*Isolates***Description**

This term adds one statistic to the model equal to the number of isolates in the network. For an undirected network, an isolate is defined to be any node with degree zero. For a directed network, an isolate is any node with both in-degree and out-degree equal to zero.

**Usage**

```
# binary: isolates
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, frequently-used, undirected, binary

---

istar-ergmTerm	<i>In-stars</i>
----------------	-----------------

---

### Description

This term adds one network statistic to the model for each element in  $k$ . The  $i$ th such statistic counts the number of distinct  $k[i]$ -instars in the network, where a  $k$ -instar is defined to be a node  $N$  and a set of  $k$  different nodes  $\{O_1, \dots, O_k\}$  such that the ties  $(O_j \rightarrow N)$  exist for  $j = 1, \dots, k$ . This term can only be used for directed networks; for undirected networks see `kstar`. Note that `istar(1)` is equal to both `ostar(1)` and `edges`.

### Usage

```
# binary: istar(k, attr=NULL, levels=NULL)
```

### Arguments

<code>k</code>	a vector of distinct integers
<code>attr, levels</code>	a vertex attribute specification; if <code>attr</code> is specified, then the count is over the instances where all nodes involved have the same value of the attribute. <code>levels</code> specified which values of <code>attr</code> are included in the count. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

kapferer	<i>Kapferer's tailor shop data</i>
----------	------------------------------------

---

### Description

This well-known social network dataset, collected by Bruce Kapferer in Zambia from June 1965 to August 1965, involves interactions among workers in a tailor shop as observed by Kapferer himself.

### Usage

```
data(kapferer)
```

### Format

Two network objects, `kapferer` and `kapferer2`. The `kapferer` dataset contains only the 39 individuals who were present at both data-collection time periods. However, these data only reflect data collected during the first period. The individuals' names are included as a nodal covariate called `names`.

## Details

An interaction is defined by Kapferer as "continuous uninterrupted social activity involving the participation of at least two persons"; only transactions that were relatively frequent are recorded. All of the interactions in this particular dataset are "sociational", as opposed to "instrumental". Kapferer explains the difference (p. 164) as follows:

"I have classed as transactions which were sociational in content those where the activity was markedly convivial such as general conversation, the sharing of gossip and the enjoyment of a drink together. Examples of instrumental transactions are the lending or giving of money, assistance at times of personal crisis and help at work."

Kapferer also observed and recorded instrumental transactions, many of which are unilateral (directed) rather than reciprocal (undirected), though those transactions are not recorded here. However, there was a second period of data collection, from September 1965 to January 1966, but these data are also not recorded here. All data are given in Kapferer (1972) on pp. 176-179.

During the first time period, there were 43 individuals working in this particular tailor shop; however, the better-known dataset includes only those 39 individuals who were present during both time collection periods. (Missing are the workers named Lenard, Peter, Lazarus, and Laurent.) Thus, we give two separate network datasets here: `kapferer` is the well-known 39-individual dataset, whereas `kapferer2` is the full 43-individual dataset.

## Source

Original source: (Kapferer 1972).

---

kstar-ergmTerm	<i>k-stars</i>
----------------	----------------

---

## Description

This term adds one network statistic to the model for each element in  $k$ . The  $i$ th such statistic counts the number of distinct  $k[i]$ -stars in the network, where a  $k$ -star is defined to be a node  $N$  and a set of  $k$  different nodes  $\{O_1, \dots, O_k\}$  such that the ties  $\{N, O_i\}$  exist for  $i = 1, \dots, k$ . This term can only be used for undirected networks; for directed networks, see `istar`, `ostar`, `twopath` and `m2star`. Note that `kstar(1)` is equal to `edges`.

## Usage

```
# binary: kstar(k, attr=NULL, levels=NULL)
```

## Arguments

<code>k</code>	a vector of distinct integers
<code>attr, levels</code>	a vertex attribute specification; if <code>attr</code> is specified, then the count is over the instances where all nodes involved have the same value of the attribute. <code>levels</code> specified which values of <code>attr</code> are included in the count. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, undirected, binary

---

Label-ergmTerm      *Modify terms' coefficient names*

---

**Description**

This operator evaluates `formula` without modification, but modifies its coefficient and/or parameter names based on `label` and `pos`.

**Usage**

```
# binary: Label(formula, label, pos)
```

```
# valued: Label(formula, label, pos)
```

**Arguments**

<code>formula</code>	a one-sided <a href="#">ergm()</a> -style formula with the terms to be evaluated
<code>label</code>	a character vector specifying the label for the terms, a <a href="#">list</a> of two character vectors (see <a href="#">Details</a> ), or a function through which term names are mapped (or a <a href="#">as_mapper</a> -style formula).
<code>pos</code>	controls how <code>label</code> modifies the term names: one of "prepend" , "replace" , "append" , or "(" , with the latter wrapping the term names in parentheses like a function call with name specified by <code>label</code> .

**Details**

If `pos == "replace"`:

- Elements for which `is.na(label) == TRUE` are preserved.
- If the model is curved, `label=` can be either function/mapper or a [list](#) with two elements, the first element giving the curved (model) parameter names and second giving the canonical parameter names. `NULL` leaves the respective name unchanged.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

 localtriangle-ergmTerm

*Triangles within neighborhoods*


---

### Description

This term adds one statistic to the model equal to the number of triangles in the network between nodes "close to" each other. For an undirected network, a local triangle is defined to be any set of three edges between nodal pairs  $\{(i, j), (j, k), (k, i)\}$  that are in the same neighborhood. For a directed network, a triangle is defined as any set of three edges  $(i \rightarrow j), (j \rightarrow k)$  and either  $(k \rightarrow i)$  or  $(k \leftarrow i)$  where again all nodes are within the same neighborhood.

### Usage

```
# binary: localtriangle(x)
```

### Arguments

x                    an undirected network or an symmetric adjacency matrix that specifies whether the two nodes are in the same neighborhood. Note that `triangle`, with or without an argument, is a special case of `localtriangle`.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical dyadic attribute, directed, triad-related, undirected, binary

---

 Log-ergmTerm

*Take a natural logarithm of a network's statistic*


---

### Description

Evaluate the terms specified in `formula` and takes a natural (base  $e$ ) logarithm of them. Since an ERGM statistic must be finite, `log0` specifies the value to be substituted for  $\log(\emptyset)$ . The default value seems reasonable for most purposes.

### Usage

```
# binary: Log(formula, log0=-1/sqrt(.Machine$double.eps))
```

```
# valued: Log(formula, log0=-1/sqrt(.Machine$double.eps))
```

### Arguments

formula            a one-sided `ergm()`-style formula with the terms to be evaluated  
 log0                the value to be substituted for  $\log(\emptyset)$

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

logLik.ergm	A <a href="#">logLik()</a> method for <a href="#">ergm</a> fits.
-------------	--

---

**Description**

A function to return the log-likelihood associated with an [ergm](#) fit, evaluating it if necessary. If the log-likelihood was not computed for object, produces an error unless `eval.loglik=TRUE`.

**Usage**

```
## S3 method for class 'ergm'
logLik(
  object,
  add = FALSE,
  force.reeval = FALSE,
  eval.loglik = add || force.reeval,
  control = control.logLik.ergm(),
  ...,
  verbose = FALSE
)

## S3 method for class 'ergm'
deviance(object, ...)

## S3 method for class 'ergm'
AIC(object, ..., k = 2)

## S3 method for class 'ergm'
BIC(object, ...)
```

**Arguments**

<code>object</code>	An <a href="#">ergm</a> fit, returned by <a href="#">ergm()</a> .
<code>add</code>	Logical: If TRUE, instead of returning the log-likelihood, return object with log-likelihood value (and the null likelihood value) set.
<code>force.reeval</code>	Logical: If TRUE, reestimate the log-likelihood even if object already has an estimate.
<code>eval.loglik</code>	Logical: If TRUE, evaluate the log-likelihood if not set on object.

control	A list of control parameters for algorithm tuning, typically constructed with <code>control.logLik.ergm()</code> . Its documentation gives the list of recognized control parameters and their meaning. The more generic utility <code>snctrl()</code> (Stat-Net ConTRoL) also provides argument completion for the available control functions and limited argument name checking.
...	Other arguments to the likelihood functions.
verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. <code>FALSE/0</code> produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
k	see help for <code>AIC()</code> .

### Value

The form of the output of `logLik.ergm` depends on `add`: `add=FALSE` (the default), a `logLik` object. If `add=TRUE` (the default), an `ergm` object with the log-likelihood set.

As of version 3.1, all likelihoods for which `logLikNull` is not implemented are computed relative to the reference measure. (I.e., a null model, with no terms, is defined to have likelihood of 0, and all other models are defined relative to that.)

### Functions

- `deviance(ergm)`: A `deviance()` method.
- `AIC(ergm)`: An `AIC()` method.
- `BIC(ergm)`: A `BIC()` method.

### References

There are no references for Rd macro `\insertAllCites` on this help page.

### See Also

[logLik\(\)](#), [logLikNull\(\)](#), [ergm.bridge.llr\(\)](#), [ergm.bridge.dindstart.llk\(\)](#)

### Examples

```
# See help(ergm) for a description of this model. The likelihood will
# not be evaluated.
data(florentine)
## Not run:
# The default maximum number of iterations is currently 20. We'll only
# use 2 here for speed's sake.
gest <- ergm(floamarriage ~ kstar(1:2) + absdiff("wealth") + triangle, eval.loglik=FALSE)

gest <- ergm(floamarriage ~ kstar(1:2) + absdiff("wealth") + triangle, eval.loglik=FALSE,
            control=control.ergm(MCMLE.maxit=2))
# Log-likelihood is not evaluated, so no deviance, AIC, or BIC:
summary(gest)
# Evaluate the log-likelihood and attach it to the object.
```

```

# The default number of bridges is currently 20. We'll only use 3 here
# for speed's sake.
gest.logLik <- logLik(gest, add=TRUE)

gest.logLik <- logLik(gest, add=TRUE, control=control.logLik.ergm(bridge.nsteps=3))
# Deviances, AIC, and BIC are now shown:
summary(gest.logLik)
# Null model likelihood can also be evaluated, but not for all constraints:
logLikNull(gest) # == network.dyadcount(flomarriage)*log(1/2)

## End(Not run)

```

---

logLikNull

*Calculate the null model likelihood*


---

### Description

Calculate the null model likelihood

### Usage

```

logLikNull(object, ...)

## S3 method for class 'ergm'
logLikNull(object, control = control.logLik.ergm(), ...)

```

### Arguments

object	a fitted model.
...	further arguments to lower-level functions. logLikNull computes, when possible the log-probability of the data under the null model (reference distribution).
control	A list of control parameters for algorithm tuning, typically constructed with <a href="#">control.logLik.ergm()</a> . Its documentation gives the the list of recognized control parameters and their meaning. The more generic utility <a href="#">snctrl()</a> (Stat-Net ConTRoL) also provides argument completion for the available control functions and limited argument name checking.

### Value

logLikNull returns an object of type [logLik](#) if it is able to compute the null model probability, and NA otherwise.

### Methods (by class)

- `logLikNull(ergm)`: A method for [ergm](#) fits; currently only implemented for binary ERGMs with dyad-independent sample-space constraints.

---

m2star-ergmTerm	<i>Mixed 2-stars, a.k.a 2-paths</i>
-----------------	-------------------------------------

---

### Description

This term adds one statistic to the model, equal to the number of mixed 2-stars in the network, where a mixed 2-star is a pair of distinct edges  $(i \rightarrow j), (j \rightarrow k)$ . A mixed 2-star is sometimes called a 2-path because it is a directed path of length 2 from  $i$  to  $k$  via  $j$ . However, in the case of a 2-path the focus is usually on the endpoints  $i$  and  $k$ , whereas for a mixed 2-star the focus is usually on the midpoint  $j$ . This term can only be used with directed networks; for undirected networks see `kstar(2)`. See also `twopath`.

### Usage

```
# binary: m2star
```

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

mcmc.diagnostics	<i>Conduct MCMC diagnostics on a model fit</i>
------------------	--

---

### Description

This function prints diagnostic information and creates simple diagnostic plots for MCMC sampled statistics produced from a fit.

### Usage

```
mcmc.diagnostics(object, ...)

## S3 method for class 'ergm'
mcmc.diagnostics(
  object,
  center = TRUE,
  esteq = TRUE,
  vars.per.page = 3,
  which = c("plots", "texts", "summary", "autocorrelation", "crosscorrelation", "burnin"),
  compact = FALSE,
  ...
)
```

**Arguments**

object	A model fit object to be diagnosed.
...	Additional arguments, to be passed to plotting functions.
center	Logical: If TRUE, center the samples on the observed statistics.
esteq	Logical: If TRUE, for statistics corresponding to curved ERGM terms, summarize the curved statistics by their negated estimating function values (evaluated at the MLE of any curved parameters) (i.e., $\eta'_I(\hat{\theta}) \cdot (g_I(Y) - g_I(y))$ for $I$ being indices of the canonical parameters in question), rather than the canonical (sufficient) vectors of the curved statistics relative to the observed $(g_I(Y) - g_I(y))$ .
vars.per.page	Number of rows (one variable per row) per plotting page. Ignored if <b>latticeExtra</b> package is not installed.
which	A character vector specifying which diagnostics to plot and/or print. Defaults to all of the below if meaningful: "plots" Traceplots and density plots of sample values for all statistic or estimating function elements. "texts" Shorthand for the following text diagnostics. "summary" Summary of network statistic or estimating function elements as produced by <code>coda::summary.mcmc.list()</code> . "autocorrelation" Autocorrelation of each of the network statistic or estimating function elements. "crosscorrelation" Cross-correlations between each pair of the network statistic or estimating function elements. "burnin" Burn-in diagnostics, in particular, the Geweke test. Partial matching is supported. (E.g., <code>which=c("auto", "cross")</code> will print autocorrelation and cross-correlations.)
compact	Numeric: For diagnostics that print variables in columns (e.g. correlations, hypothesis test p-values), try to abbreviate variable names to this many characters and round the numbers to compact - 2 digits after the decimal point; 0 or FALSE for no abbreviation.

**Details**

A pair of plots are produced for each statistic: a trace of the sampled output statistic values on the left and density estimate for each variable in the MCMC chain on the right. Diagnostics printed to the console include correlations and convergence diagnostics.

For `ergm()` specifically, recent changes in the estimation algorithm mean that these plots can no longer be used to ensure that the mean statistics from the model match the observed network statistics. For that functionality, please use the GOF command: `gof(object, GOF=~model)`.

In fact, an `ergm()` output object contains the sample of statistics from the last MCMC run as element `$sample`. If missing data MLE is fit, the corresponding element is named `$sample.obs`. These are objects of `mcmc` and can be used directly in the `coda` package to assess MCMC convergence.

More information can be found by looking at the documentation of `ergm()`.

**Methods (by class)**

- `mcmc.diagnostics(ergm)`:

**References**

Raftery AE, Lewis SM (1995). “The Number of Iterations, Convergence Diagnostics and Generic Metropolis Algorithms.” In Gilks WR, Spiegelhalter DJ, Richardson S (eds.), *Practical Markov Chain Monte Carlo*. Chapman and Hall, London, U.K.

**See Also**

`ergm()`, **network** package, **coda** package, `summary.ergm()`

**Examples**

```
## Not run:
#
data(florentine)
#
# test the mcmc.diagnostics function
#
gest <- ergm(flomarriage ~ edges + kstar(2))
summary(gest)

#
# Plot the probabilities first
#
mcmc.diagnostics(gest)
#
# Use coda directly
#
library(coda)
#
plot(gest$sample, ask=FALSE)
#
# A full range of diagnostics is available
# using codamenu()
#

## End(Not run)
```

---

meandeg-ergmTerm

*Mean vertex degree*


---

**Description**

This term adds one network statistic to the model equal to the average degree of a node. Note that this term is a constant multiple of both edges and density .

**Usage**

```
# binary: meandeg
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, binary

mm-ergmTerm

*Mixing matrix cells and margins***Description**

`attrs` is the rows of the mixing matrix and whose RHS gives that for its columns (which may be different). A one-sided formula (e.g.,  $\sim A$ ) is symmetrized (e.g.,  $A \sim A$ ). A two-sided formula with a dot on one side calculates the margins of the mixing matrix, analogously to `nodefactor`, with  $A \sim \cdot$  calculating the row/sender/b1 margins and  $\cdot \sim A$  calculating the column/receiver/b2 margins. If row and column attributes are the same and the network is undirected, only the cells at or above the diagonal (where  $\text{row} \leq \text{column}$ ) will be calculated.

**Usage**

```
# binary: mm(attrs, levels=NULL, levels2=-1)
```

```
# valued: mm(attrs, levels=NULL, levels2=-1, form="sum")
```

**Arguments**

<code>attrs</code>	a two-sided formula whose LHS gives the attribute or attribute function (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) for the rows of the mixing matrix and whose RHS gives for its columns. A one-sided formula (e.g., $\sim A$ ) is symmetrized (e.g., $A \sim A$ )
<code>levels</code>	subset of rows and columns to be used. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>levels2</code>	which specific cells of the matrix to include; <a href="#">?nodal_attributes</a> for details
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i,j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, frequently-used, undirected, binary, valued

---

molecule	<i>Synthetic network with 20 nodes and 28 edges</i>
----------	---

---

### Description

This is a synthetic network of 20 nodes that is used as an example within the `ergm()` documentation. It has an interesting elongated shape

- reminiscent of a chemical molecule. It is stored as a `network` object.

### Usage

```
data(molecule)
```

### See Also

florentine, sampson, network, plot.network, ergm

---

mutual-ergmTerm	<i>Mutuality</i>
-----------------	------------------

---

### Description

In binary ERGMs, equal to the number of pairs of actors  $i$  and  $j$  for which  $(i \rightarrow j)$  and  $(j \rightarrow i)$  both exist.

For valued ERGMs, equal to  $\sum_{i < j} m(y_{i,j}, y_{j,i})$ , where  $m$  is determined by form argument: "min" for  $\min(y_{i,j}, y_{j,i})$ , "nabsdiff" for  $-|y_{i,j} - y_{j,i}|$ , "product" for  $y_{i,j}y_{j,i}$ , and "geometric" for  $\sqrt{y_{i,j}}\sqrt{y_{j,i}}$ . See Krivitsky (2012) for a discussion of these statistics. `form="threshold"` simply computes the binary mutuality after thresholding at `threshold`.

This term can only be used with directed networks.

### Usage

```
# binary: mutual(same=NULL, by=NULL, diff=FALSE, keep=NULL, levels=NULL)
```

```
# valued: mutual(form="min", threshold=0)
```

### Arguments

same	if the optional argument is passed (see Specifying Vertex attributes and Levels (?nodal_attributes) for details), only mutual pairs that match on the attribute are counted; separate counts for each unique matching value can be obtained by using <code>diff=TRUE</code> with <code>same</code> . Only one of <code>same</code> or <code>by</code> may be used. If both parameters are used, <code>by</code> is ignored. This parameter is affected by <code>diff</code> .
------	---

by	if the optional argument is passed (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details), then each node is counted separately for each mutual pair in which it occurs and the counts are tabulated by unique values of the attribute. This means that the sum of the mutual statistics when by is used will equal twice the standard mutual statistic. Only one of same or by may be used. If both parameters are used, by is ignored. This parameter is not affected by diff.
keep	deprecated
levels	which statistics should be kept whenever the mutual term would ordinarily result in multiple statistics. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
form, threshold	variant to be used in the valued case.

**Note**

The argument keep is retained for backwards compatibility and may be removed in a future version. When both keep and levels are passed, levels overrides keep. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, frequently-used, binary, valued

---

nearsimmelian-ergmTerm

*Near simmelian triads*

---

**Description**

This term adds one statistic to the model equal to the number of near Simmelian triads, as defined by Krackhardt and Handcock (2007). This is a sub-graph of size three which is exactly one tie short of being complete.

**Usage**

```
# binary: nearsimmelian
```

**Note**

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, binary

---

network.list	<i>A convenience container for a list of <a href="#">network</a> objects, output by <a href="#">simulate.ergm()</a> among others.</i>
--------------	---

---

### Description

A convenience container for a list of [network](#) objects, output by [simulate.ergm\(\)](#) among others.

### Usage

```
network.list(object, ...)

## S3 method for class 'network.list'
print(x, stats.print = FALSE, ...)

## S3 method for class 'network.list'
summary(
  object,
  stats.print = TRUE,
  net.print = FALSE,
  net.summary = FALSE,
  ...
)
```

### Arguments

object, x	a list of networks or a <code>network.list</code> object.
...	for <code>network.list</code> , additional attributes to be set on the network list; for others, arguments passed down to lower-level functions.
stats.print	Logical: If TRUE, print network statistics.
net.print	Logical: If TRUE, print network overviews.
net.summary	Logical: If TRUE, print network summaries.

### Methods (by generic)

- `print(network.list)`: A `print()` method for network lists.
- `summary(network.list)`: A `summary()` method for network lists.

### Note

Functions from the [simulate.ergm\(\)](#) family can also return lists of lists of networks. In this case, they have an additional class `"network.list.list"`. At this time, it only affects printing.

### See Also

[simulate.ergm\(\)](#)

**Examples**

```
# Draw from a Bernoulli model with 16 nodes
# and tie probability 0.1
#
g.use <- network(16, density=0.1, directed=FALSE)
#
# Starting from this network let's draw 3 realizations
# of a model with edges and 2-star terms
#
g.sim <- simulate(~edges+kstar(2), nsim=3, coef=c(-1.8, 0.03),
                 basis=g.use, control=control.simulate(
                   MCMC.burnin=100000,
                   MCMC.interval=1000))
print(g.sim)
summary(g.sim)
```

---

nodal\_attributes

*Specifying nodal attributes and their levels*


---

**Description**

This document describes the ways to specify nodal attributes or functions of nodal attributes and which levels for categorical factors to include. For the helper functions to facilitate this, see [nodal\\_attributes-API](#).

**Usage**

```
LARGEST(l, a)
```

```
SMALLEST(l, a)
```

```
COLLAPSE_SMALLEST(object, n, into)
```

**Arguments**

```
object, l, a, n, into
```

COLLAPSE\_SMALLEST, LARGEST, and SMALLEST are technically functions but they are generally not called in a standard fashion but rather as a part of an vertex attribute specification or a level specification as described below. The above usage examples are needed to pass R's package checking without warnings; please disregard them, and refer to the sections and examples below instead.

**Specifying nodal attributes**

Term nodal attribute arguments, typically called `attr`, `attrs`, `by`, or `on` are interpreted as follows:

**a character string** Extract the vertex attribute with this name.

- a character vector of length > 1** Extract the vertex attributes and paste them together, separated by dots if the term expects categorical attributes and (typically) combine into a covariate matrix if it expects quantitative attributes.
- a function** The function is called on the LHS network and additional arguments to `ergm_get_vattr()`, expected to return a vector or matrix of appropriate dimension. (Shorter vectors and matrix columns will be recycled as needed.)
- a formula** The expression on the RHS of the formula is evaluated in an environment of the vertex attributes of the network, expected to return a vector or matrix of appropriate dimension. (Shorter vectors and matrix columns will be recycled as needed.) Within this expression, the network itself accessible as either `.` or `.nw`. For example, `nodecov(~abs(Grade-mean(Grade))/network.size(.))` would return the absolute difference of each actor's "Grade" attribute from its network-wide mean, divided by the network size.
- an AsIs object created by I()** Use as is, checking only for correct length and type.

Any of these arguments may also be wrapped in or piped through `COLLAPSE_SMALLEST(attr, n, into)` or, `attr %>% COLLAPSE_SMALLEST(n, into)`, a convenience function that will transform the attribute by collapsing the smallest `n` categories into one, naming it `into`. Note that `into` must be of the same type (numeric, character, etc.) as the vertex attribute in question. If there are ties for `n`th smallest category, they will be broken in lexicographic order, and a warning will be issued.

The name the nodal attribute receives in the statistic can be overridden by setting an `attr()`-style attribute "name".

### Specifying categorical attribute levels and their ordering

For categorical attributes, to select which levels are of interest and their ordering, use the argument `levels`. Selection of nodes (from the appropriate vector of nodal indices) is likewise handled as the selection of levels, using the argument `nodes`. For mixing matrix effects such as `nodemix()` and `mm()`, first, the nodal attribute selection is performed using `levels`, then the cells of the resulting mixing matrix can be selected using `levels2`. These arguments are interpreted as follows:

- an expression wrapped in I()** Use the given list of levels as is.
- a numeric or logical vector** Used for indexing of a list of all possible levels (typically, unique values of the attribute) in default order (typically lexicographic), i.e., `sort(unique(attr))[levels]`. In particular, `levels=TRUE` will retain all levels. Negative values exclude. Another special value is `LARGEST`, which will refer to the most frequent category, so, say, to set such a category as the baseline, pass `levels=-LARGEST`. In addition, `LARGEST(n)` will refer to the `n` largest categories. `SMALLEST` works analogously. If there are ties in frequencies, they will be broken in lexicographic order, and a warning will be issued. To specify numeric or logical levels literally, wrap in `I()`.
- NULL** (Not recommended.) Retain all possible levels, equivalent to passing `TRUE`. Note that this is *not* the same as passing a numeric or logical vector of length 0, which will be interpreted as excluding all levels.
- a character vector** Use as is.
- a function** The function is called on the list of unique values of the attribute, the values of the attribute themselves, and the network itself, depending on its arity. Its return value is interpreted as above.

**a formula** The expression on the RHS of the formula is evaluated in an environment in which the network itself is accessible as `.nw`, the list of unique values of the attribute as `.` or as `.levels`, and the attribute vector itself as `.attr`. Its return value is interpreted as above.

**a matrix** For mixing effects (i.e., `level2=` arguments), a matrix can be used to select elements of the mixing matrix, either by specifying a logical (TRUE and FALSE) matrix of the same dimension as the mixing matrix to select the corresponding cells or a two-column numeric matrix indicating giving the coordinates of cells to be used.

Note that `levels`, `nodes`, and others often have a default that is sensible for the term in question.

### base and keep arguments

Earlier versions of many of the terms had arguments `base` and `keep` for selecting categorical attribute levels. They have been superseded since **ergm** 3.9.4 and will be removed soon.

In general, `keep = X` can be replaced by `levels = X`, as both typically have the same semantics.

The effect of `base` is opposite that of `levels`, `nodes`, and `levels2`: `levels` specify which levels to include, whereas `base` specifies which levels to exclude. Thus, if `X` is not 0 or NULL, `base = X` can be replaced with `levels = -X`. If `X` is 0 or NULL, `base = X` means to include all levels, so it should be replaced with `levels = TRUE`.

### Examples

```
library(magrittr) # for %>%

data(faux.mesa.high)

# Activity by grade with a baseline grade excluded:
summary(faux.mesa.high~nodefactor(~Grade))
# Name overrides:
summary(faux.mesa.high~nodefactor("Form"~Grade)) # Only for terms that don't use the LHS.
summary(faux.mesa.high~nodefactor(~structure(Grade,name="Form")))
# Retain all levels:
summary(faux.mesa.high~nodefactor(~Grade, levels=TRUE)) # or levels=NULL
# Use the largest grade as baseline (also Grade 7):
summary(faux.mesa.high~nodefactor(~Grade, levels=-LARGEST))
# Activity by grade with no baseline smallest two grades (11 and
# 12) collapsed into a new category, labelled 0:
table(faux.mesa.high %v% "Grade")
summary(faux.mesa.high~nodefactor((~Grade) %>% COLLAPSE_SMALLEST(2, 0),
                                levels=TRUE))

# Handling of tied frequencies
faux.mesa.high %v% "Plans" <-
  sample(rep(c("College", "Trade School", "Apprenticeship", "Undecided"), c(80,80,20,25)))
summary(faux.mesa.high ~ nodefactor("Plans", levels = -LARGEST))

# Mixing between lower and upper grades:
summary(faux.mesa.high~mm(~Grade>=10))
# Mixing between grades 7 and 8 only:
summary(faux.mesa.high~mm("Grade", levels=I(c(7,8))))
# or
```

```

summary(faux.mesa.high~mm("Grade", levels=1:2))
# or using levels2 (see ? mm) to filter the combinations of levels,
summary(faux.mesa.high~mm("Grade",
  levels2=~sapply(.levels,
    function(l)
      l[[1]]%in%c(7,8) && l[[2]]%in%c(7,8))))

# Here are some less complex ways to specify levels2. This is the
# full list of combinations of sexes in an undirected network:
summary(faux.mesa.high~mm("Sex", levels2=TRUE))
# Select only the second combination:
summary(faux.mesa.high~mm("Sex", levels2=2))
# Equivalently,
summary(faux.mesa.high~mm("Sex", levels2=-c(1,3)))
# or
summary(faux.mesa.high~mm("Sex", levels2=c(FALSE,TRUE,FALSE)))
# Select all *but* the second one:
summary(faux.mesa.high~mm("Sex", levels2=-2))
# Select via a mixing matrix: (Network is undirected and
# attributes are the same on both sides, so we can use either M or
# its transpose.)
(M <- matrix(c(FALSE,TRUE,FALSE,FALSE),2,2))
summary(faux.mesa.high~mm("Sex", levels2=M)+mm("Sex", levels2=t(M)))
# Select via an index of a cell:
idx <- cbind(1,2)
summary(faux.mesa.high~mm("Sex", levels2=idx))
# Or, select by specific attribute value combinations, though note
# the names 'row' and 'col' and the order for undirected networks:
summary(faux.mesa.high~mm("Sex",
  levels2 = I(list(list(row="M",col="M"),
    list(row="M",col="F"),
    list(row="F",col="M")))))

# Note the warning: in an undirected network with identical row and
# column attributes, the mixing matrix is symmetric and only the
# upper triangle (where row < column) is valid, so the [M,F] cell
# will get a statistic of 0 with a warning.

# mm() term allows two-sided attribute formulas with different attributes:
summary(faux.mesa.high~mm(Grade~Race, levels2=TRUE))
# It is possible to have collapsing functions in the formula; note
# the parentheses around "~Race": this is because a formula
# operator (~) has lower precedence than pipe (|>):
summary(faux.mesa.high~mm(Grade~(~Race) %>% COLLAPSE_SMALLEST(3,"BWO"), levels2=TRUE))

# Some terms, such as nodecov(), accept matrices of nodal
# covariates. An certain R quirk means that columns whose
# expressions are not typical variable names have their names
# dropped and need to be adjusted. Consider, for example, the
# linear and quadratic effects of grade:
Grade <- faux.mesa.high %v% "Grade"
colnames(cbind(Grade, Grade^2)) # Second column name missing.
colnames(cbind(Grade, Grade2=Grade^2)) # Can be set manually,
colnames(cbind(Grade, `Grade^2`=Grade^2)) # even to non-variable-names.

```

```

colnames(cbind(Grade, Grade^2, deparse.level=2)) # Alternatively, deparse.level=2 forces naming.
rm(Grade)

# Therefore, the nodal attribute names are set as follows:
summary(faux.mesa.high~nodecov(~cbind(Grade, Grade^2))) # column names dropped with a warning
summary(faux.mesa.high~nodecov(~cbind(Grade, Grade2=Grade^2))) # column names set manually
summary(faux.mesa.high~nodecov(~cbind(Grade, Grade^2, deparse.level=2))) # using deparse.level=2

# Activity by grade with a random covariate. Note that setting an attribute "name" gives it a name:
randomcov <- structure(I(rbinom(network.size(faux.mesa.high),1,0.5)), name="random")
summary(faux.mesa.high~nodefactor(I(randomcov)))

```

---

nodecov-ergmTerm	<i>Main effect of a covariate</i>
------------------	-----------------------------------

---

## Description

This term adds a single network statistic for each quantitative attribute or matrix column to the model equaling the sum of `attr(i)` and `attr(j)` for all edges  $(i, j)$  in the network. For categorical attributes, see `nodefactor`. Note that for directed networks, `nodecov` equals `nodeicov` plus `nodeocov`.

## Usage

```

# binary: nodecov(attr)

# binary: nodemain

# valued: nodecov(attr, form="sum")

# valued: nodemain(attr, form="sum")

```

## Arguments

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

## Note

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, frequently-used, quantitative nodal attribute, undirected, binary, valued

---

nodecovar-ergmTerm      *Covariance of undirected dyad values incident on each actor*

---

**Description**

This term adds one statistic equal to  $\sum_{i,j < k} y_{i,j} y_{i,k} / (n - 2)$  . This can be viewed as a valued analog of the `star(2)` statistic.

**Usage**

```
# valued: nodecovar(center, transform)
```

**Arguments**

center	If center=TRUE , the $y_{i,j}$ s are centered by their mean over the whole network before the calculation. Note that this makes the model non-local, but it may alleviate multimodality.
transform	If transform="sqrt" , $y_{i,j}$ s are repaced by their square roots before the calculation. This makes sense for counts in particular. If center=TRUE as well, they are centered by the mean of the square roots.

**Note**

Note that this term replaces `nodesqrtcovar` , which has been deprecated in favor of `nodecovar(transform="sqrt")` .

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** undirected, valued

---

nodecovrange-ergmTerm *Range of covariate values for neighbors of a node*

---

### Description

This term adds a single network statistic equalling the sum over the nodes of the range over of its neighbors' values.

### Usage

```
# binary: nodecovrange(attr)
```

### Arguments

attr            a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal\_attributes) for details.)

### Details

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

### References

Hoffman M, Block P, Snijders TAB (2023). "Modeling Partitions of Individuals." *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:10.1177/00811750221145166.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, quantitative nodal attribute, undirected, binary

---

nodefactor-ergmTerm *Factor attribute effect*

---

### Description

This term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the attr attribute (or each combination of the attributes given). Each of these statistics gives the number of times a node with that attribute or those attributes appears in an edge in the network.

### Usage

```
# binary: nodefactor(attr, base=1, levels=-1)
```

```
# valued: nodefactor(attr, base=1, levels=-1, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
base	deprecated
levels	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i,j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

To include all attribute values is usually not a good idea, because the sum of all such statistics equals the number of edges and hence a linear dependency would arise in any model also including edges. The default, `levels=-1`, is therefore to omit the first (in lexicographic order) attribute level. To include all levels, pass either `levels=TRUE` (i.e., keep all levels) or `levels=NULL` (i.e., do not filter levels).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, frequently-used, undirected, binary, valued

---

nodefactordistinct-ergmTerm

*Number of distinct neighbor types*

---

**Description**

This term adds a single network statistic to the model, counting, for each node, the number of distinct values of the attribute found among its neighbors.

**Usage**

```
# binary: nodefactordistinct(attr, levels=TRUE)
```

**Arguments**

attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
levels	this optional argument controls which levels of the attribute attributes and Levels (?nodal_attributes) for details.)

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). “Modeling Partitions of Individuals.” *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:10.1177/00811750221145166.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, undirected, binary

---

nodeicov-ergmTerm	<i>Main effect of a covariate for in-edges</i>
-------------------	--

---

**Description**

This term adds a single network statistic for each quantitative attribute or matrix column to the model equaling the total value of `attr(j)` for all edges  $(i, j)$  in the network. This term may only be used with directed networks. For categorical attributes, see `nodeifactor`.

**Usage**

```
# binary: nodeicov(attr)
# valued: nodeicov(attr, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, frequently-used, quantitative nodal attribute, binary, valued

---

nodeicovar-ergmTerm     *Covariance of in-dyad values incident on each actor*

---

**Description**

This term adds one statistic equal to  $\sum_{i,j,k} y_{j,i} y_{k,i} / (n-2)$ . This can be viewed as a valued analog of the `istar(2)` statistic.

**Usage**

```
# valued: nodeicovar(center, transform)
```

**Arguments**

center	If center=TRUE, the $y_{j,i}$ s are centered by their mean over the whole network before the calculation. Note that this makes the model non-local, but it may alleviate multimodality.
transform	If transform="sqrt", $y_{j,i}$ s are repaced by their square roots before the calculation. This makes sense for counts in particular. If center=TRUE as well, they are centered by the mean of the square roots.

**Note**

Note that this term replaces `nodeisqrtcovar`, which has been deprecated in favor of `nodeicovar(transform="sqrt")`.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, valued

---

 nodeicovrange-ergmTerm

*Range of covariate values for in-neighbors of a node*


---

### Description

This term adds a single network statistic equalling the sum over the nodes of the range over of its neighbors' values.

### Usage

```
# binary: nodeicovrange(attr)
```

### Arguments

`attr` a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal\_attributes) for details.)

### Details

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

### References

Hoffman M, Block P, Snijders TAB (2023). "Modeling Partitions of Individuals." *Sociological Methodology*, 53(1), 1–41. ISSN 1467-9531. doi:10.1177/00811750221145166.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, quantitative nodal attribute, binary

---

 nodeifactor-ergmTerm *Factor attribute effect for in-edges*


---

### Description

This term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute (or each combination of the attributes given). Each of these statistics gives the number of times a node with that attribute or those attributes appears as the terminal node of a directed tie.

For an analogous term for quantitative vertex attributes, see `nodeicov`.

**Usage**

```
# binary: nodeifactor(attr, base=1, levels=-1)

# valued: nodeifactor(attr, base=1, levels=-1, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
base	deprecated
levels	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i,j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

To include all attribute values is usually not a good idea, because the sum of all such statistics equals the number of edges and hence a linear dependency would arise in any model also including edges. The default, `levels=-1`, is therefore to omit the first (in lexicographic order) attribute level. To include all levels, pass either `levels=TRUE` (i.e., keep all levels) or `levels=NULL` (i.e., do not filter levels).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, frequently-used, binary, valued

nodeifactordistinct-ergmTerm

*Number of distinct in-neighbor types*

**Description**

This term adds a single network statistic to the model, counting, for each node, the number of distinct values of the attribute found among its neighbors.

**Usage**

```
# binary: nodeifactordistinct(attr, levels=TRUE)
```

**Arguments**

attr	a vertex attribute specification (see Specifying Vertex attributes and Levels (?nodal_attributes) for details.)
levels	this optional argument controls which levels of the attribute attributes and Levels (?nodal_attributes) for details.)

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). “Modeling Partitions of Individuals.” *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:10.1177/00811750221145166.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

nodematch-ergmTerm      *Uniform homophily and differential homophily*

---

**Description**

When `diff=FALSE`, this term adds one network statistic to the model, which counts the number of edges  $(i, j)$  for which `attr(i)==attr(j)`. This is also called “uniform homophily”, because each group is assumed to have the same propensity for within-group ties. When multiple attribute names are given, the statistic counts only ties for which all of the attributes match. When `diff=TRUE`,  $p$  network statistics are added to the model, where  $p$  is the number of unique values of the `attr` attribute. The  $k$  th such statistic counts the number of edges  $(i, j)$  for which `attr(i) == attr(j) == value(k)`, where `value(k)` is the  $k$  th smallest unique value of the `attr` attribute. This is also called “differential homophily”, because each group is allowed to have a unique propensity for within-group ties. Note that a statistical test of uniform vs. differential homophily should be conducted using the ANOVA function.

By default, matches on all levels  $k$  are counted. This works for both `diff=TRUE` and `diff=FALSE`.

**Usage**

```
# binary: nodematch(attr, diff=FALSE, keep=NULL, levels=NULL)
# valued: nodematch(attr, diff=FALSE, keep=NULL, levels=NULL, form="sum")
# valued: match(attr, diff=FALSE, keep=NULL, levels=NULL, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
diff	specify if the term has uniform or differential homophily
keep	deprecated
levels	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

The argument keep is retained for backwards compatibility and may be removed in a future version. When both keep and levels are passed, levels overrides keep. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, frequently-used, undirected, binary, valued

---

NodematchFilter-ergmTerm

*Filtering on nodematch*

---

**Description**

Evaluates the terms specified in formula on a network constructed by taking  $y$  and removing any edges for which `attrname(i) != attrname(j)`.

**Usage**

```
# binary: NodematchFilter(formula, attrname)
```

**Arguments**

formula	formula to be evaluated
attrname	a character vector giving one or more names of attributes in the network's vertex attribute list.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary

---

nodemix-ergmTerm      *Nodal attribute mixing*

---

**Description**

By default, this term adds one network statistic to the model for each possible pairing of attribute values. The statistic equals the number of edges in the network in which the nodes have that pairing of values. (When multiple attributes are specified, a statistic is added for each combination of attribute values for those attributes.) In other words, this term produces one statistic for every entry in the mixing matrix for the attribute(s). By default, the ordering of the attribute values is lexicographic: alphabetical (for nominal categories) or numerical (for ordered categories).

**Usage**

```
# binary: nodemix(attr, base=NULL, b1levels=NULL, b2levels=NULL, levels=NULL, levels2=-1)
```

```
# valued: nodemix(attr, base=NULL, b1levels=NULL, b2levels=NULL, levels=NULL,
#               levels2=-1, form="sum")
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
base	deprecated
b1levels, b2levels, levels	control what statistics are included in the model and the order in which they appear. <code>levels</code> applies to unipartite networks; <code>b1levels</code> and <code>b2levels</code> apply to bipartite networks (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details)
levels2	similar to the other levels arguments above and applies to all networks. Optionally allows a factor or character matrix to be specified to group certain levels. Level combinations corresponding to NA are excluded. Combinations specified by the same character or level will be grouped together and summarised by the same statistic. If an empty string is specified, the level combinations will be ungrouped. Only the upper triangle needs to be specified for undirected networks. For example, <code>levels2=matrix(c('A', '', NA, 'A'), 2, 2, byrow=TRUE)</code> on an undirected matrix will group homophilous ties while leaving ties between 1 and 2 ungrouped.
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels` are passed, `levels` overrides `base`. See [nodal\\_attributes](#).

The argument `base` is retained for backwards compatibility and may be removed in a future version. When both `base` and `levels2` are passed, `levels2` overrides `base`. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, frequently-used, undirected, binary, valued

---

nodecov-ergmTerm      *Main effect of a covariate for out-edges*

---

**Description**

This term adds a single network statistic for each quantitative attribute or matrix column to the model equaling the total value of `attr(i)` for all edges  $(i, j)$  in the network. This term may only be used with directed networks. For categorical attributes, see `nodeofactor`.

**Usage**

```
# binary: nodecov(attr)

# valued: nodecov(attr, form="sum")
```

**Arguments**

<code>attr</code>	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
<code>form</code>	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

**ergm** versions 3.9.4 and earlier used different arguments for this term. See [ergm-options](#) for how to invoke the old behaviour.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, quantitative nodal attribute, binary, valued

---

nodeocovar-ergmTerm      *Covariance of out-dyad values incident on each actor*

---

### Description

This term adds one statistic equal to  $\sum_{i,j,k} y_{i,j} y_{i,k} / (n-2)$ . This can be viewed as a valued analog of the ostar(2) statistic.

### Usage

```
# valued: nodeocovar(center, transform)
```

### Arguments

center	whether the $y_{i,j}$ s are centered by their mean over the whole network before the calculation. Note that this makes the model non-local, but it may alleviate multimodality.
transform	if transform="sqrt", $y_{i,j}$ s are repaced by their square roots before the calculation. This makes sense for counts in particular. If center=TRUE as well, they are centered by the mean of the square roots.

### Note

Note that this term replaces nodeosqrtcovar, which has been deprecated in favor of nodeocovar(transform="sqrt").

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, valued

---

nodeocovrange-ergmTerm      *Range of covariate values for out-neighbors of a node*

---

### Description

This term adds a single network statistic equalling the sum over the nodes of the range over of its neighbors' values.

### Usage

```
# binary: nodeocovrange(attr)
```

**Arguments**

`attr` a vertex attribute specification (see [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details.)

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). “Modeling Partitions of Individuals.” *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:[10.1177/00811750221145166](https://doi.org/10.1177/00811750221145166).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, quantitative nodal attribute, binary

nodeofactor-ergmTerm *Factor attribute effect for out-edges*

**Description**

This term adds multiple network statistics to the model, one for each of (a subset of) the unique values of the `attr` attribute (or each combination of the attributes given). Each of these statistics gives the number of times a node with that attribute or those attributes appears as the node of origin of a directed tie.

**Usage**

```
# binary: nodeofactor(attr, base=1, levels=-1)
```

```
# valued: nodeofactor(attr, base=1, levels=-1, form="sum")
```

**Arguments**

`attr` a vertex attribute specification (see [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details.)

`base` deprecated

`levels` this optional argument controls which levels of the attribute should be included and which should be excluded. (See [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details.)

`form` how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form  $\sum_{i,j} x_{i,j} y_{i,j}$ , where  $y_{i,j}$  is the value of dyad  $(i, j)$  and  $x_{i,j}$  is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See [ergmTerm](#) for more information.

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and levels are passed, levels overrides base. See [nodal\\_attributes](#).

To include all attribute values is usually not a good idea, because the sum of all such statistics equals the number of edges and hence a linear dependency would arise in any model also including edges. The default, levels=-1, is therefore to omit the first (in lexicographic order) attribute level. To include all levels, pass either levels=TRUE (i.e., keep all levels) or levels=NULL (i.e., do not filter levels).

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, dyad-independent, binary, valued

---

nodeofactordistinct-ergmTerm

*Number of distinct out-neighbor types*

---

**Description**

This term adds a single network statistic to the model, counting, for each node, the number of distinct values of the attribute found among its neighbors.

**Usage**

```
# binary: nodeofactordistinct(attr, levels=TRUE)
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
levels	this optional argument controls which levels of the attribute attributes and Levels ( <a href="#">?nodal_attributes</a> ) for details.)

**Details**

This is a network analogue of the statistic introduced by Hoffman et al. (2023).

**References**

Hoffman M, Block P, Snijders TAB (2023). “Modeling Partitions of Individuals.” *Sociological Methodology*, **53**(1), 1–41. ISSN 1467-9531. doi:[10.1177/00811750221145166](https://doi.org/10.1177/00811750221145166).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

nparam	<i>Length of the parameter vector associated with an object or with its terms.</i>
--------	--

---

**Description**

This is a generic that returns the number of parameters associated with a model or a model fit.

**Usage**

```
nparam(object, ...)  
  
## Default S3 method:  
nparam(object, ...)  
  
## S3 method for class 'ergm'  
nparam(object, offset = NA, ...)
```

**Arguments**

object	An object for which number of parameters is defined.
...	Additional arguments to methods.
offset	If NA (the default), all model terms are counted; if TRUE, only offset terms are counted; and if FALSE, offset terms are skipped.

**Methods (by class)**

- `nparam(default)`: By default, the length of the `coef()` vector is returned.
- `nparam(ergm)`: A method to return the number of parameters of an [ergm](#) fit.

---

nsp-ergmTerm

*Directed non-edgewise shared partners*


---

### Description

This term adds one network statistic to the model for each element in  $d$  where the  $i$  th such statistic equals the number of non-edges in the network with exactly  $d[i]$  shared partners.

### Usage

```
# binary: dnsp(d, type="OTP")
```

```
# binary: nsp(d, type="OTP")
```

### Arguments

d	a vector of distinct integers
type	A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

### Shared partner types

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the `type` argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the `relevent` package):

- **Outgoing Two-path ("OTP"):** vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- **Incoming Two-path ("ITP"):** vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- **Reciprocated Two-path ("RTP"):** vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .
- **Outgoing Shared Partner ("OSP"):** vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- **Incoming Shared Partner ("ISP"):** vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

**Note**

This term takes an additional term option (see [options?ergm](#)), `cache.sp`, controlling whether the implementation will cache the number of shared partners for each dyad in the network; this is usually enabled by default.

This term can only be used with directed networks.

**References**

Butts CT (2008). “A Relational Event Framework for Social Action.” *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). “Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks.” *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

observed-ergmConstraint

*Preserve the observed dyads of the given network*

---

**Description**

Preserve the observed dyads of the given network.

**Usage**

# observed

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed, dyad-independent, undirected

---

odegrange-ergmTerm      *Out-degree range*

---

### Description

This term adds one network statistic to the model for each element of `from` (or `to`); the  $i$ th such statistic equals the number of nodes in the network of out-degree greater than or equal to `from[i]` but strictly less than `to[i]`, i.e. with out-edge count in semiopen interval `[from, to)`.

This term can only be used with directed networks; for undirected networks (bipartite and not) see `degrange`. For degrees of specific modes of bipartite networks, see `b1degrange` and `b2degrange`. For in-degrees, see `idegrange`.

### Usage

```
# binary: odegrange(from, to=+Inf, by=NULL, homophily=FALSE, levels=NULL)
```

### Arguments

`from, to`            vectors of distinct integers. If one of the vectors have length 1, it is recycled to the length of the other. Otherwise, it must have the same length.

`by, levels, homophily`    the optional argument `by` specifies a vertex attribute (see `Specifying Vertex attributes and Levels (?nodal_attributes)` for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

`attr`                a vertex attribute specification (see `Specifying Vertex attributes and Levels (?nodal_attributes)` for details.)

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

odegree-ergmTerm      *Out-degree*


---

### Description

This term adds one network statistic to the model for each element in  $d$ ; the  $i$ th such statistic equals the number of nodes in the network of out-degree  $d[i]$ , i.e. the number of nodes with exactly  $d[i]$  out-edges. This term can only be used with directed networks; for undirected networks see `degree`.

### Usage

```
# binary: odegree(d, by=NULL, homophily=FALSE, levels=NULL)
```

### Arguments

`d`                    a vector of distinct integers  
`by, levels, homophily`      the optional argument `by` specifies a vertex attribute (see `Specifying Vertex attributes and Levels (?nodal_attributes)` for details). If this is specified and `homophily` is `TRUE`, then degrees are calculated using the subnetwork consisting of only edges whose endpoints have the same value of the `by` attribute. If `by` is specified and `homophily` is `FALSE` (the default), then separate degree range statistics are calculated for nodes having each separate value of the attribute. `levels` selects which levels of `by` to include.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, frequently-used, binary

---

odegree1.5-ergmTerm      *Out-degree to the 3/2 power*


---

### Description

This term adds one network statistic to the model equaling the sum over the actors of each actor's outdegree taken to the  $3/2$  power (or, equivalently, multiplied by its square root). This term is analogous to the term of Snijders et al. (2010), equation (12). This term can only be used with directed networks.

### Usage

```
# binary: odegree1.5
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, binary

---

odegreedist-ergmConstraint

*Preserve the outdegree distribution*

---

**Description**

Preserve the outdegree distribution of the given network.

**Usage**

```
# odegreedist
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed

---

odegrees-ergmConstraint

*Preserve outdegree for directed networks*

---

**Description**

For directed networks, preserve the outdegree of each vertex of the given network, while allowing indegree to vary

**Usage**

```
# odegrees
```

**See Also**

[ergmConstraint](#) for index of constraints and hints currently visible to the package.

**Keywords:** directed

---

Offset-ergmTerm	<i>Terms with fixed coefficients</i>
-----------------	--------------------------------------

---

**Description**

This operator is analogous to the `offset()` wrapper, but the coefficients are specified within the term and the curved ERGM mechanism is used internally.

**Usage**

```
# binary: Offset(formula, coef, which)
```

**Arguments**

formula	a one-sided <code>ergm()</code> -style formula with the terms to be evaluated
coef	coefficients to the formula
which	used to specify which of the parameters in the formula are fixed. It can be a logical vector (recycled as needed), a numeric vector of indices of parameters to be fixed, or a character vector of parameter names.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary

---

opentriad-ergmTerm	<i>Open triads</i>
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---

**Description**

This term adds one statistic to the model equal to the number of 2-stars minus three times the number of triangles in the network. It is currently only implemented for undirected networks.

**Usage**

```
# binary: opentriad
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** triad-related, undirected, binary

---

ostar-ergmTerm	<i>k-Outstars</i>
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---

**Description**

This term adds one network statistic to the model for each element in  $k$ . The  $i$ th such statistic counts the number of distinct  $k[i]$ -outstars in the network, where a  $k$ -outstar is defined to be a node  $N$  and a set of  $k$  different nodes  $\{O_1, \dots, O_k\}$  such that the ties  $(N \rightarrow O_j)$  exist for  $j = 1, \dots, k$ . This term can only be used with directed networks; for undirected networks see `kstar`.

**Usage**

```
# binary: ostar(k, attr=NULL, levels=NULL)
```

**Arguments**

<code>k</code>	a vector of distinct integers
<code>attr, levels</code>	a vertex attribute specification; if <code>attr</code> is specified, then the count is over the instances where all nodes involved have the same value of the attribute. <code>levels</code> specified which values of <code>attr</code> are included in the count. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**Note**

`ostar(1)` is equal to both `istar(1)` and `edges`.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, binary

---

param_names	<i>Names of the parameters associated with an object.</i>
-------------	---

---

**Description**

This is a generic that returns a vector giving the names of the parameters associated with a model or a model fit.

**Usage**

```
param_names(object, ...)
```

## Default S3 method:

```
param_names(object, ...)
```

```
param_names(object, ...) <- value
```

**Arguments**

object	An object for which parameter names are defined.
...	Additional arguments to methods.
value	Specification for the new parameter names.

**Methods (by class)**

- param\_names(default): By default, the names of the `coef()` vector is returned.

**Functions**

- param\_names(object, ...) <- value: a method for modifying parameter names of an object.

---

predict.formula	<i>ERGM-based tie probabilities</i>
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---

**Description**

Calculate model-predicted **conditional** and **unconditional** tie probabilities for dyads in the given network. Conditional probabilities of a dyad given the state of all the remaining dyads in the graph are computed exactly. Unconditional probabilities are computed through simulating networks using the given model. Currently there are two methods implemented:

- Method for formula objects requires (1) an ERGM model formula with an existing network object on the left hand side and model terms on the right hand side, and (2) a vector of corresponding parameter values.
- Method for ergm objects, as returned by `ergm()`, takes both the formula and parameter values from the fitted model object.

Both methods can limit calculations to specific set of dyads of interest.

**Usage**

```
## S3 method for class 'formula'
predict(
  object,
  eta,
  conditional = TRUE,
  type = c("response", "link"),
  nsim = 100,
  output = c("data.frame", "matrix"),
  ...,
  basis = ergm.getnetwork(object),
  theta = NULL
)

## S3 method for class 'ergm'
predict(object, ...)
```

**Arguments**

object	a formula or a fitted ERGM model object
eta	numeric vector of ERGM model <i>canonical</i> parameter values
conditional	logical whether to compute conditional or unconditional predicted probabilities
type	character element, one of "response" (default) or "link" - whether the returned predictions are on the probability scale or on the scale of linear predictor. This is similar to type argument of <code>predict.glm()</code> .
nsim	integer, number of simulated networks used for computing unconditional probabilities. Defaults to 100.
output	character, type of object returned. Defaults to "data.frame". See section Value below.
...	other arguments passed to/from other methods. For the <code>predict.formula</code> method, if <code>conditional=TRUE</code> arguments are passed to <code>ergmMPLC()</code> . If <code>conditional=FALSE</code> arguments are passed to <code>simulate_formula()</code> .
basis	a value (usually a <a href="#">network</a> ) to override the LHS of the formula.
theta	deprecated name for the parameter vector, renamed to eta since the canonical parameters are expected.

**Value**

Type of object returned depends on the argument output. If `output="data.frame"` the function will return a data frame with columns:

- tail, head – indices of nodes identifying a dyad
- p – predicted conditional tie probability

If `output="matrix"` the function will return an "adjacency matrix" with the predicted probabilities. Diagonal values are 0s.

**Examples**

```
# A three-node empty directed network
net <- network.initialize(3, directed=TRUE)

# In homogeneous Bernoulli model with odds of a tie of 1/5 all ties are
# equally likely
predict(net ~ edges, log(1/5))

# Let's add a tie so that `net` has 1 tie out of possible 6 (so odds of 1/5)
net[1,2] <- 1

# Fit the model
fit <- ergm(net ~ edges)

# The p's should be identical
predict(fit)
```

---

Prod-ergmTerm	<i>A product (or an arbitrary power combination) of one or more formulas</i>
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---

### Description

This operator evaluates a list of formulas whose corresponding RHS statistics will be multiplied elementwise. They are required to be nonnegative.

### Usage

# binary: Prod(formulas, label)

# valued: Prod(formulas, label)

### Arguments

**formulas** a list (constructed using `list()` or `c()`) of `ergm()`-style formulas whose RHS gives the statistics to be evaluated, or a single formula.

If a formula in the list has an LHS, it is interpreted as follows:

- a numeric scalar: Network statistics of this formula will be exponentiated by this.
- a numeric vector: Corresponding network statistics of this formula will be exponentiated by this.
- a numeric matrix: Vector of network statistics will be exponentiated by this using the same pattern as matrix multiplication.
- a character string: One of several predefined multiplicative combinations. Currently supported presets are as follows:
  - "prod": Network statistics of this formula will be multiplied together; equivalent to  $\text{matrix}(1,1,p)$ , where  $p$  is the length of the network statistic vector.
  - "geomean": Network statistics of this formula will be geometrically averaged; equivalent to  $\text{matrix}(1/p,1,p)$ , where  $p$  is the length of the network statistic vector.

**label** used to specify the names of the elements of the resulting term product vector. If label is a character vector of length 1, it will be recycled with indices appended. If a function is specified, formulas parameter names are extracted and their list of character vectors is passed label.

### Details

Note that each formula must either produce the same number of statistics or be mapped through a matrix to produce the same number of statistics.

A single formula is also permitted. This can be useful if one wishes to, say, scale or multiply together the statistics returned by a formula.

Offsets are ignored unless there is only one formula and the transformation only scales the statistics (i.e., the effective transformation matrix is diagonal).

Curved models are supported, subject to some limitations. In particular, the first model's etamap will be used, overwriting the others. If `label` is not of length 1, it should have an `attr`-style attribute "curved" specifying the names for the curved parameters.

### Note

The current implementation piggybacks on the `Log`, `Exp`, and `Sum` operators, essentially `Exp(~Sum(~Log(formula), label))`. This may result in loss of precision, particularly for extremely large or small statistics. The implementation may change in the future.

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

Project-ergmTerm      *Evaluation on a projection of a bipartite network*

---

### Description

This operator on a bipartite network evaluates the formula on the undirected, valued network constructed by projecting it onto its specified mode. `Proj1(formula)` and `Proj2(formula)` are aliases for `Project(formula, 1)` and `Project(formula, 2)`, respectively.

### Usage

```
# binary: Project(formula, mode)
```

```
# binary: Proj1(formula)
```

```
# binary: Proj2(formula)
```

### Arguments

<code>formula</code>	a one-sided <a href="#">ergm()</a> -style formula with the terms to be evaluated
<code>mode</code>	the mode onto which to project: 1 or 2

### See Also

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** bipartite, operator, binary

---

rank_test.ergm	<i>A lack-of-fit test for ERGMs</i>
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---

### Description

A simple test reporting the sample quantile of the observed network's probability in the distribution under the MLE. This is a conservative p-value for the null hypothesis of the observed network being a draw from the distribution of interest.

### Usage

```
rank_test.ergm(x, plot = FALSE)
```

### Arguments

x	an <code>ergm()</code> object.
plot	if TRUE, plot the empirical distribution.

### Value

The sample quantile of the observed network's probability among the predicted.

---

receiver-ergmTerm	<i>Receiver effect</i>
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---

### Description

This term adds one network statistic for each node equal to the number of in-ties for that node. This measures the popularity of the node. The term for the first node is omitted by default because of linear dependence that arises if this term is used together with edges, but its coefficient can be computed as the negative of the sum of the coefficients of all the other actors. That is, the average coefficient is zero, following the Holland-Leinhardt parametrization of the  $p_1$  model (Holland and Leinhardt, 1981). This term can only be used with directed networks. For undirected networks, see `sociality`.

### Usage

```
# binary: receiver(base=1, nodes=-1)
# valued: receiver(base=1, nodes=-1, form="sum")
```

**Arguments**

base	deprecated
nodes	specify which nodes' statistics should be included or excluded (see Specifying Vertex attributes and Levels (?nodal_attributes) for details)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j}y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and nodes are passed, nodes overrides base. See [nodal\\_attributes](#).

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, binary, valued

---

S-ergmTerm

*Evaluation on an induced subgraph*

---

**Description**

This operator takes a two-sided formula `attrs` whose LHS gives the attribute or attribute function for which tails and heads will be used to construct the induced subgraph. They must evaluate either to a logical vector equal in length to the number of tails (for LHS) and heads (for RHS) indicating which nodes are to be used to induce the subgraph or a numeric vector giving their indices.

**Usage**

```
# binary: S(formula, attrs)
```

```
# valued: S(formula, attrs)
```

**Arguments**

formula	a one-sided <a href="#">ergm()</a> -style formula with the terms to be evaluated
attrs	a two-sided formula to be used. A one-sided formula (e.g., $\sim A$ ) is symmetrized (e.g., $A \sim A$ ).

**Details**

As with indexing vectors, the logical vector will be recycled to the size of the network or the size of the appropriate bipartition, and negative indices will deselect vertices.

When the two sets are identical, the induced subgraph retains the directedness of the original graph. Otherwise, an undirected bipartite graph is induced.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

sampson	<i>Longitudinal and cumulative networks of positive and negative affect in a monastery</i>
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---

**Description**

A collection of [network](#) objects containing the "liking" nominations of the monks studied by Sampson (1968) over the three time points: `data(samplk)` contains the time-sliced networks of liking and disliking (`samplk1`, `samplk2`, `samplk3`, `sampdlk1`, `sampdlk2`, and `sampdlk3`) and `data(sampson)` (`samplike`) a network cumulative network of liking nominations.

**Usage**

```
data(sampson)
data(samplk)
```

**Details**

Sampson (1968) recorded the social interactions among a group of monks while he was a resident as an experimenter at the cloister. During his stay, a political "crisis in the cloister" resulted in the expulsion of four monks—namely, the three "outcasts," Brothers Elias, Simplicius, Basil, and the leader of the "young Turks," Brother Gregory. Not long after Brother Gregory departed, all but one of the "young Turks" left voluntarily: Brothers John Bosco, Albert, Boniface, Hugh, and Mark. Then, all three of the "waverers" also left: First, Brothers Amand and Victor, then later Brother Romuald. Eventually, Brother Peter and Brother Winfrid also left, leaving only four of the original group.

Of particular interest are the data on positive affect relations ("liking," using the terminology later adopted by White et al. (1976)), in which each monk was asked to list three monks with whom he had positive affect ("liked the most", "liked 2nd most", and "liked 3rd most") and three monks with whom he had negative affect ("liked the least", "liked 2nd least", liked 3rd least"). (Some did not comply fully and provided additional names, forcing ties.)

The data were gathered at three times to capture changes in group sentiment over time. They represent three time points in the period during which a new cohort had entered the monastery near the end of the study but before the major conflict began. These three time points are labeled T2, T3, and T4 in Tables D5 through D16 in the appendices of Sampson's 1969 dissertation.

This data set is standard in the social network analysis literature, having been modeled by Holland and Leinhardt (1981), Reitz (1982), Holland et al. (1983), Fienberg and Wasserman (1981), Hoff et al. (2002) (using `samplk3`), and Krivitsky et al. (2009) (`samplike`). This is only a small piece of the data collected by Sampson.

**Common attributes:**

All of the networks contain the following identical vertex attributes:

`cloisterville` An indicator of attendance at the minor seminary of "Cloisterville" before coming to the monastery.

`vertex.names` The given names of the novices. NB: These names have been corrected as of `ergm` version 3.6.1; see details below.

`group4` The original grouping by Sampson ("[Young] Turks", "Loyal [Opposition]", "Outcasts", and "Waverers").

`group3` As `group4`, but with "Waverers" merged into their nearest group; retained for historical reasons.

Note that the `group` vertex attribute differs between `sampson` and `samp1k` for historical reasons.

#### **Time-sliced networks (`samp1k`):**

The data from the three time points (T2, T3, T4) are provided as `samp1k1`, `samp1k2`, and `samp1k3` for liking most and `sampd1k1`, `sampd1k2`, and `sampd1k3` for liking least, respectively. A directed edge from monk A to monk B exists if A nominated B among his top three (or four, in case of ties) choices at that time point. Each network also has an edge attribute `score`, indicating the ranking given:

list	score
liked the most	+3
liked 2nd most	+2
liked 3rd most	+1
not nominated	0
liked 3rd least	-1
liked 2nd least	-2
liked the least	-3

Note that the `samp1k[1-3]` networks only contain positive scores and `sampd1k[1-3]` only negative.

For historical reasons, their vertex attribute `group` is the same as `group4` described above.

#### **Cumulative ties (`sampson`):**

The `samplike` network is the time-aggregated network. Thus, a tie from monk A to monk B exists if A nominated B as one of his three (or four, in case of ties) most liked at any of the three time points. An edge attribute, `nominations`, gives the number of times (out of 3) that monk A nominated monk B.

For historical reasons, its vertex attribute `group` is the same as `group3` described above.

## **History**

### **Dislike networks, edge scores, and group harmonization:**

`ergm` 4.11 added dislike networks `sampd1k[1-3]`; note that unlike the positive affection networks, it is not clear whether these were collected contemporaneously or retrospectively.

For all networks in `samp1k`, scores reflecting the position in the ranking were added.

The `group` vertex attribute meaning differed between the `sampson` (`samplike`) and the `samp1k` networks and will continue to do so for reproducibility; for removal of ambiguity, both datasets now have `group3` and `group4` vertex attributes, with `group3` inherited from `sampson` and `group4` from `samp1k`.

**Cloisterville and vertex names:**

This data set was updated for version 2.5 (March 2012) to add the `cloisterville` variable and refine the names. This information is from de Nooy et al. (2005). The original vertex names were: Romul\_10, Bonaven\_5, Ambrose\_9, Berth\_6, Peter\_4, Louis\_11, Victor\_8, Winf\_12, John\_1, Greg\_2, Hugh\_14, Boni\_15, Mark\_7, Albert\_16, Amand\_13, Basil\_3, Elias\_17, Simp\_18. The numbers indicate the ordering used in the original dissertation of Sampson (1968).

**Mislabeling in Versions Prior to 3.6.1:**

In `ergm` version 3.6.0 and earlier, The adjacency matrices of the `samplike`, `samplk1`, `samplk2`, and `samplk3` networks reflected the original Sampson (1968) ordering of the names even though the vertex labels used the name order of de Nooy et al. (2005). That is, in `ergm` version 3.6.0 and earlier, the vertices were mislabeled. The correct order is the same one given in Tables D5, D9, and D13 of Sampson (1968): John Bosco, Gregory, Basil, Peter, Bonaventure, Berthold, Mark, Victor, Ambrose, Romauld (Sampson uses both spellings "Romauld" and "Ramauld" in the dissertation), Louis, Winfrid, Amand, Hugh, Boniface, Albert, Elias, Simplicius. By contrast, the order given in `ergm` version 3.6.0 and earlier is: Ramuald, Bonaventure, Ambrose, Berthold, Peter, Louis, Victor, Winfrid, John Bosco, Gregory, Hugh, Boniface, Mark, Albert, Amand, Basil, Elias, Simplicius.

**Source**

(Sampson 1968).

<https://github.com/bavla/Nets/raw/refs/heads/master/data/Pajek/esna/Sampson.zip>

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### See Also

[florentine](#), [network](#), [plot.network](#), [ergm](#)

### Examples

```
data(samplk)

# Table D5 in \insertCite{Sa68n;textual}{ergm}
as.matrix(samplk1, attrname = "score") + as.matrix(sampdlk1, attrname = "score")

# Table D9
as.matrix(samplk2, attrname = "score") + as.matrix(sampdlk2, attrname = "score")

# Table D13
as.matrix(samplk3, attrname = "score") + as.matrix(sampdlk3, attrname = "score")

# Cumulative ties in `samplike`
data(sampson)
all(as.matrix(samplike) ==
    as.matrix(samplk1) | as.matrix(samplk2) | as.matrix(samplk3))
all(as.matrix(samplike, attrname = "nominations") ==
    as.matrix(samplk1) + as.matrix(samplk2) + as.matrix(samplk3))
```

---

san

*Generate networks with a given set of network statistics*

---

### Description

This function attempts to find a network or networks whose statistics match those passed in via the `target.stats` vector.

### Usage

```
san(object, ...)

## S3 method for class 'formula'
san(
  object,
  response = NULL,
  reference = ~Bernoulli,
```

```

constraints = ~.,
target.stats = NULL,
basis = NULL,
output = c("network", "edgelist", "ergm_state"),
only.last = TRUE,
control = control.san(),
verbose = FALSE,
offset.coef = NULL,
...
)

## S3 method for class 'ergm_model'
san(
  object,
  reference = ~Bernoulli,
  constraints = ~.,
  target.stats = NULL,
  basis = NULL,
  output = c("network", "edgelist", "ergm_state"),
  only.last = TRUE,
  control = control.san(),
  verbose = FALSE,
  offset.coef = NULL,
  ...
)

```

## Arguments

object	Either a <a href="#">formula</a> or some other supported representation of an ERGM, such as an <a href="#">ergm_model</a> object. <a href="#">formula</a> should be of the form $y \sim \langle \text{model terms} \rangle$ , where $y$ is a network object or a matrix that can be coerced to a <a href="#">network</a> object. For the details on the possible $\langle \text{model terms} \rangle$ , see <a href="#">ergmTerm</a> . To create a <a href="#">network</a> object in <code>R</code> , use the <code>network()</code> function, then add nodal attributes to it using the <code>%v%</code> operator if necessary.
...	Further arguments passed to other functions.
response	Either a character string, a formula, or NULL (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows:  NULL Model simple presence or absence, via a binary ERGM. <b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <a href="#">logical</a> (TRUE/FALSE) for binary or <a href="#">numeric</a> for valued. <b>a formula</b> must be of the form <code>NAME~EXPR TYPE</code> (with <code> </code> being literal). <code>EXPR</code> is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional <code>NAME</code> specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of <code>EXPR</code> . Normally, the type of ERGM is determined by whether the result of evaluating <code>EXPR</code> is logical or numeric, but the optional

	TYPE can be used to override by specifying a scalar of the type involved (e.g., TRUE for binary and 1 for valued).
reference	A one-sided formula specifying the reference measure ( $h(y)$ ) to be used. See help for <a href="#">ERGM reference measures</a> implemented in the <a href="#">ergm</a> package.
constraints	<p>A formula specifying one or more constraints on the support of the distribution of the networks being modeled. Multiple constraints may be given, separated by “+” and “-” operators. See <a href="#">ergmConstraint</a> for the detailed explanation of their semantics and also for an indexed list of the constraints visible to the <a href="#">ergm</a> package.</p> <p>The default is to have no constraints except those provided through the <a href="#">ergmlhs</a> API.</p> <p>Together with the model terms in the formula and the reference measure, the constraints define the distribution of networks being modeled.</p> <p>It is also possible to specify a proposal function directly either by passing a string with the function’s name (in which case, arguments to the proposal should be specified through the <code>MCMC.prop.args</code> argument to the relevant control function, or by giving it on the LHS of the hints formula to <code>MCMC.prop</code> argument to the control function. This will override the one chosen automatically.</p> <p>Note that not all possible combinations of constraints and reference measures are supported. However, for relatively simple constraints (i.e., those that simply permit or forbid specific dyads or sets of dyads from changing), arbitrary combinations should be possible.</p>
target.stats	A vector of the same length as the number of non-offset statistics implied by the formula. If the vector is named, its names will be matched to the corresponding statistic names, and if the named vector has a single coefficient without a name, it will be used for the unmatched statistics. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
basis	If not NULL, a network object used to start the Markov chain. If NULL, this is taken to be the network named in the formula.
output	Character, one of “network” (default), “edgelist”, or “ergm_state”: determines the output format. Partial matching is performed.
only.last	if TRUE, only return the last network generated; otherwise, return a <a href="#">network.list</a> with a network for each iteration.
control	A list of control parameters for algorithm tuning, typically constructed with <a href="#">control.san()</a> . Its documentation gives the the list of recognized control parameters and their meaning. The more generic utility <a href="#">snctrl()</a> (StatNet CONTRoL) also provides argument completion for the available control functions and limited argument name checking.
verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
offset.coef	A vector of offset coefficients; these must be passed in by the user. Note that these should be the same set of coefficients one would pass to <a href="#">ergm</a> via its <code>offset.coef</code> argument.

formula (By default, the formula is taken from the `ergm` object. If a different formula object is wanted, specify it here.)

### Details

The following description is an exegesis of section 4 of Krivitsky et al. (2023).

Let  $\mathbf{g}$  be a vector of target statistics for the network we wish to construct. That is, we are given an arbitrary network  $\mathbf{y}^0 \in \mathcal{Y}$ , and we seek a network  $\mathbf{y} \in \mathcal{Y}$  such that  $\mathbf{g}(\mathbf{y}) \approx \mathbf{g}$  – ideally equality is achieved, but in practice we may have to settle for a close approximation. The variant of simulated annealing is as follows.

The energy function is defined

$$E_W(\mathbf{y}) = (\mathbf{g}(\mathbf{y}) - \mathbf{g})^\top W(\mathbf{g}(\mathbf{y}) - \mathbf{g}),$$

with  $W$  a symmetric positive (barring multicollinearity in statistics) definite matrix of weights. This function achieves 0 only if the target is reached. A good choice of this matrix yields a more efficient search.

A standard simulated annealing loop is used, as described below, with some modifications. In particular, we allow the user to specify a vector of offsets  $\eta$  to bias the annealing, with  $\eta_k = 0$  denoting no offset. Offsets can be used with SAN to forbid certain statistics from ever increasing or decreasing. As with `ergm()`, offset terms are specified using the `offset()` decorator and their coefficients specified with the `offset.coef` argument. By default, finite offsets are ignored by, but this can be overridden by setting the `control.san()` argument `SAN.ignore.finite.offsets = FALSE`.

The number of simulated annealing runs is specified by the `SAN.maxit` control parameter and the initial value of the temperature  $T$  is set to `SAN.tau`. The value of  $T$  decreases linearly until  $T = 0$  at the last run, which implies that all proposals that increase  $E_W(\mathbf{y})$  are rejected. The weight matrix  $W$  is initially set to  $I_p/p$ , where  $I_p$  is the identity matrix of an appropriate dimension. For weight  $W$  and temperature  $T$ , the simulated annealing iteration proceeds as follows:

1. Test if  $E_W(\mathbf{y}) = 0$ . If so, then exit.
2. Generate a perturbed network  $\mathbf{y}^*$  from a proposal that respects the model constraints. (This is typically the same proposal as that used for MCMC.)
3. Store the quantity  $\mathbf{g}(\mathbf{y}^*) - \mathbf{g}(\mathbf{y})$  for later use.
4. Calculate acceptance probability

$$\alpha = \exp[-(E_W(\mathbf{y}^*) - E_W(\mathbf{y}))/T + \eta^\top(\mathbf{g}(\mathbf{y}^*) - \mathbf{g}(\mathbf{y}))]$$

(If  $|\eta_k| = \infty$  and  $g_k(\mathbf{y}^*) - g_k(\mathbf{y}) = 0$ , their product is defined to be 0.)

5. Replace  $\mathbf{y}$  with  $\mathbf{y}^*$  with probability  $\min(1, \alpha)$ .

After the specified number of iterations,  $T$  is updated as described above, and  $W$  is recalculated by first computing a matrix  $S$ , the sample covariance matrix of the proposed differences stored in Step 3 (i.e., whether or not they were rejected), then  $W = S^+ / \text{tr}(S^+)$ , where  $S^+$  is the Moore–Penrose pseudoinverse of  $S$  and  $\text{tr}(S^+)$  is the trace of  $S^+$ . The differences in Step 3 closely reflect the relative variances and correlations among the network statistics.

In Step 2, the many options for MCMC proposals can provide for effective means of speeding the SAN algorithm’s search for a viable network.

**Value**

A network or list of networks that hopefully have network statistics close to the `target.stats` vector. No guarantees are provided about their probability distribution. Additionally, `attr()`-style attributes `formula` and `stats` are included.

**Methods (by class)**

- `san(formula)`: Sufficient statistics are specified by a `formula`.
- `san(ergm_model)`: A lower-level function that expects a pre-initialized `ergm_model`.

**References**

Krivitsky PN, Hunter DR, Morris M, Klumb C (2023). “ergm 4: New Features for Analyzing Exponential-Family Random Graph Models.” *Journal of Statistical Software*, **105**(6), 1–44. [doi:10.18637/jss.v105.i06](https://doi.org/10.18637/jss.v105.i06).

**Examples**

```
# initialize x to a random undirected network with 50 nodes and a density of 0.1
x <- network(50, density = 0.05, directed = FALSE)

# try to find a network on 50 nodes with 300 edges, 150 triangles,
# and 1250 4-cycles, starting from the network x
y <- san(x ~ edges + triangles + cycle(4), target.stats = c(300, 150, 1250))

# check results
summary(y ~ edges + triangles + cycle(4))

# initialize x to a random directed network with 50 nodes
x <- network(50)

# add vertex attributes
x %v% 'give' <- runif(50, 0, 1)
x %v% 'take' <- runif(50, 0, 1)

# try to find a set of 100 directed edges making the outward sum of
# 'give' and the inward sum of 'take' both equal to 62.5, so in
# edges (i,j) the node i tends to have above average 'give' and j
# tends to have above average 'take'
y <- san(x ~ edges + nodecov('give') + nodecov('take'), target.stats = c(100, 62.5, 62.5))

# check results
summary(y ~ edges + nodecov('give') + nodecov('take'))

# initialize x to a random undirected network with 50 nodes
x <- network(50, directed = FALSE)

# add a vertex attribute
x %v% 'popularity' <- runif(50, 0, 1)
```

```

# try to find a set of 100 edges making the total sum of
# popularity(i) and popularity(j) over all edges (i,j) equal to
# 125, so nodes with higher popularity are more likely to be
# connected to other nodes
y <- san(x ~ edges + nodecov('popularity'), target.stats = c(100, 125))

# check results
summary(y ~ edges + nodecov('popularity'))

# creates a network with denser "core" spreading out to sparser
# "periphery"
plot(y)

```

---

search.ergmTerms

*Search ERGM terms, constraints, references, hints, and proposals*


---

## Description

Searches through the database of [ergmTerms](#), [ergmConstraints](#), [ergmReferences](#), [ergmHints](#), and [ergmProposals](#) and prints out a list of terms and term-alikes appropriate for the specified network's structural constraints, optionally restricting by additional keywords and search term matches.

## Usage

```
search.ergmTerms(search, net, keywords, name, packages)
```

```
search.ergmConstraints(search, keywords, name, packages)
```

```
search.ergmReferences(search, keywords, name, packages)
```

```
search.ergmHints(search, keywords, name, packages)
```

```
search.ergmProposals(search, name, reference, constraints, packages)
```

## Arguments

search	optional character search term to search for in the text of the term descriptions. Only matching terms will be returned. Matching is case insensitive.
net	a network object that the term would be applied to, used as template to determine directedness, bipartite, etc
keywords	optional character vector of keyword tags to use to restrict the results (i.e. 'curved', 'triad-related')
name	optional character name of a specific term to return
packages	optional character vector indicating the subset of packages in which to search
reference, constraints	optional names of references and constraints to narrow down the proposal

**Details**

Uses `grep()` internally to match the search terms against the term description, so search is currently matched as a single phrase. Keyword tags will only return a match if all of the specified tags are included in the term.

**Value**

prints out the name and short description of matching terms, and invisibly returns them as a list. If name is specified, prints out the full definition for the named term.

**Author(s)**

skyebend@uw.edu

**See Also**

See also [ergmTerm](#), [ergmConstraint](#), [ergmReference](#), [ergmHint](#), and [ergmProposal](#), for lists of terms and term-alikes visible to **ergm**.

**Examples**

```
# find all of the terms that mention triangles
search.ergmTerms('triangle')

# two ways to search for bipartite terms:

# search using a bipartite net as a template
myNet<-network.initialize(5,bipartite=3)
search.ergmTerms(net=myNet)

# or request the bipartite keyword
search.ergmTerms(keywords='bipartite')

# search on multiple keywords
search.ergmTerms(keywords=c('bipartite','dyad-independent'))

# print out the content for a specific term
search.ergmTerms(name='b2factor')

# request the bipartite keyword in the ergm package
search.ergmTerms(keywords='bipartite', packages='ergm')

# find all of the constraint that mention degrees
search.ergmConstraints('degree')

# search on multiple keywords
search.ergmConstraints(keywords=c('directed','dyad-independent'))

# print out the content for a specific constraint
search.ergmConstraints(name='b1degrees')
```

```

# request the bipartite keyword in the ergm package
search.ergmConstraints(keywords='directed', packages='ergm')

# find all discrete references
search.ergmReferences(keywords='discrete')

# find all of the hints
search.ergmHints()

# find all of the proposals that mention triangles
search.ergmProposals('triangle')

# print out the content for a specific proposals
search.ergmProposals(name='randomtoggle')

# find all proposals with a given required or optional constraint
search.ergmProposals(constraints='.dyads')

# find all proposals a given reference
search.ergmProposals(reference='Bernoulli')

# request proposals that mention triangle in the ergm package
search.ergmProposals('triangle', packages='ergm')

```

---

sender-ergmTerm	<i>Sender effect</i>
-----------------	----------------------

---

### Description

This term adds one network statistic for each node equal to the number of out-ties for that node. This measures the activity of the node. The term for the first node is omitted by default because of linear dependence that arises if this term is used together with edges, but its coefficient can be computed as the negative of the sum of the coefficients of all the other actors. That is, the average coefficient is zero, following the Holland-Leinhardt parametrization of the  $p_1$  model (Holland and Leinhardt, 1981).

For undirected networks, see `sociality`.

### Usage

```

# binary: sender(base=1, nodes=-1)

# valued: sender(base=1, nodes=-1, form="sum")

```

**Arguments**

base	deprecated
nodes	specify which nodes' statistics should be included or excluded (see Specifying Vertex attributes and Levels (?nodal_attributes) for details)
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and nodes are passed, nodes overrides base. See [nodal\\_attributes](#).

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, binary, valued

---

simmelian-ergmTerm      *Simmelian triads*

---

**Description**

This term adds one statistic to the model equal to the number of Simmelian triads, as defined by Krackhardt and Handcock (2007). This is a complete sub-graph of size three.

**Usage**

```
# binary: simmelian
```

**Note**

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, binary

---

`simmelianties-ergmTerm`*Ties in simmelian triads*

---

**Description**

This term adds one statistic to the model equal to the number of ties in the network that are associated with Simmelian triads, as defined by Krackhardt and Handcock (2007). Each Simmelian has six ties in it but, because Simmelians can overlap in terms of nodes (and associated ties), the total number of ties in these Simmelians is less than six times the number of Simmelians. Hence this is a measure of the clustering of Simmelians (given the number of Simmelians).

**Usage**

```
# binary: simmelianties
```

**Note**

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, binary

---

`simulate.ergm`*Draw from the distribution of an Exponential Family Random Graph Model*

---

**Description**

[simulate](#) is used to draw from exponential family random network models. See [ergm\(\)](#) for more information on these models.

The method for [ergm](#) objects inherits the model, the coefficients, the response attribute, the reference, the constraints, and most simulation parameters from the model fit, unless overridden by passing them explicitly. Unless overridden, the simulation is initialized with either a random draw from near the fitted model saved by [ergm\(\)](#) or, if unavailable, the network to which the ERGM was fit.

**Usage**

```

## S3 method for class 'formula_lhs_network'
simulate(object, nsim = 1, seed = NULL, ...)

simulate_formula(object, ..., basis = eval_lhs.formula(object))

## S3 method for class 'network'
simulate_formula(
  object,
  nsim = 1,
  seed = NULL,
  coef,
  response = NULL,
  reference = ~Bernoulli,
  constraints = ~.,
  observational = FALSE,
  monitor = NULL,
  statonly = FALSE,
  esteq = FALSE,
  output = c("network", "stats", "edgelist", "ergm_state"),
  simplify = TRUE,
  sequential = TRUE,
  control = control.simulate.formula(),
  verbose = FALSE,
  ...,
  basis = ergm.getnetwork(object),
  do.sim = NULL,
  return.args = NULL
)

## S3 method for class 'ergm_state'
simulate_formula(
  object,
  nsim = 1,
  seed = NULL,
  coef,
  response = NULL,
  reference = ~Bernoulli,
  constraints = ~.,
  observational = FALSE,
  monitor = NULL,
  statonly = FALSE,
  esteq = FALSE,
  output = c("network", "stats", "edgelist", "ergm_state"),
  simplify = TRUE,
  sequential = TRUE,
  control = control.simulate.formula(),
  verbose = FALSE,

```

```
    ...,
    basis = ergm.getnetwork(object),
    do.sim = NULL,
    return.args = NULL
)

## S3 method for class 'ergm_model'
simulate(
  object,
  nsim = 1,
  seed = NULL,
  coef,
  reference = if (is(constraints, "ergm_proposal")) NULL else trim_env(~Bernoulli),
  constraints = trim_env(~.),
  observational = FALSE,
  monitor = NULL,
  basis = NULL,
  esteq = FALSE,
  output = c("network", "stats", "edgelist", "ergm_state"),
  simplify = TRUE,
  sequential = TRUE,
  control = control.simulate.formula(),
  verbose = FALSE,
  ...,
  do.sim = NULL,
  return.args = NULL
)

## S3 method for class 'ergm_state_full'
simulate(
  object,
  nsim = 1,
  seed = NULL,
  coef,
  esteq = FALSE,
  output = c("network", "stats", "edgelist", "ergm_state"),
  simplify = TRUE,
  sequential = TRUE,
  control = control.simulate.formula(),
  verbose = FALSE,
  ...,
  return.args = NULL
)

## S3 method for class 'ergm'
simulate(
  object,
  nsim = 1,
```

```

seed = NULL,
coef = coefficients(object),
response = object$network %ergmlhs% "response",
reference = object$reference,
constraints = list(object$constraints, object$obs.constraints),
observational = FALSE,
monitor = NULL,
basis = if (observational || esteq) object$network else NVL(object$newnetwork,
  object$network),
statonly = FALSE,
esteq = FALSE,
output = c("network", "stats", "edgelist", "ergm_state"),
simplify = TRUE,
sequential = TRUE,
control = control.simulate.ergm(),
verbose = FALSE,
...,
return.args = NULL
)

```

## Arguments

object	Either a <a href="#">formula</a> or an <a href="#">ergm</a> object. The <a href="#">formula</a> should be of the form $y \sim \langle \text{model terms} \rangle$ , where $y$ is a network object or a matrix that can be coerced to a <a href="#">network</a> object. For the details on the possible $\langle \text{model terms} \rangle$ , see <a href="#">ergmTerm</a> . To create a <a href="#">network</a> object in <code>R</code> , use the <code>network()</code> function, then add nodal attributes to it using the <code>%v%</code> operator if necessary.
nsim	Number of networks to be randomly drawn from the given distribution on the set of all networks, returned by the Metropolis-Hastings algorithm.
seed	Seed value (integer) for the random number generator. See <a href="#">set.seed()</a> .
...	Further arguments passed to or used by methods.
basis	a value (usually a <a href="#">network</a> ) to override the LHS of the formula.
coef	Vector of parameter values for the model from which the sample is to be drawn. If object is of class <code>ergm</code> , the default value is the vector of estimated coefficients. Can be set to <code>NULL</code> to bypass, but only if <code>return.args</code> below is used. Note that <code>NaN</code> values are treated specially: see the section on skipping below. If the vector is named, its names will be matched to the corresponding coefficient names, and if the named vector has a single coefficient without a name, it will be used for the unmatched coefficients. In particular, <code>setNames(x, "")</code> will be treated as a vector of <code>xs</code> .
response	Either a character string, a formula, or <code>NULL</code> (the default), to specify the response attributes and whether the ERGM is binary or valued. Interpreted as follows: <code>NULL</code> Model simple presence or absence, via a binary ERGM. <b>character string</b> The name of the edge attribute whose value is to be modeled. Type of ERGM will be determined by whether the attribute is <a href="#">logical</a> ( <code>TRUE/FALSE</code> ) for binary or <a href="#">numeric</a> for valued.

**a formula** must be of the form `NAME~EXPR|TYPE` (with `|` being literal). `EXPR` is evaluated in the formula's environment with the network's edge attributes accessible as variables. The optional `NAME` specifies the name of the edge attribute into which the results should be stored, with the default being a concise version of `EXPR`. Normally, the type of ERGM is determined by whether the result of evaluating `EXPR` is logical or numeric, but the optional `TYPE` can be used to override by specifying a scalar of the type involved (e.g., `TRUE` for binary and `1` for valued).

reference	A one-sided formula specifying the reference measure ( $h(y)$ ) to be used. See help for <a href="#">ERGM reference measures</a> implemented in the <a href="#">ergm</a> package.
constraints	<p>A formula specifying one or more constraints on the support of the distribution of the networks being modeled. Multiple constraints may be given, separated by "+" and "-" operators. See <a href="#">ergmConstraint</a> for the detailed explanation of their semantics and also for an indexed list of the constraints visible to the <a href="#">ergm</a> package.</p> <p>The default is to have no constraints except those provided through the <a href="#">ergmlhs</a> API.</p> <p>Together with the model terms in the formula and the reference measure, the constraints define the distribution of networks being modeled.</p> <p>It is also possible to specify a proposal function directly either by passing a string with the function's name (in which case, arguments to the proposal should be specified through the <code>MCMC.prop.args</code> argument to the relevant control function, or by giving it on the LHS of the hints formula to <code>MCMC.prop</code> argument to the control function. This will override the one chosen automatically.</p> <p>Note that not all possible combinations of constraints and reference measures are supported. However, for relatively simple constraints (i.e., those that simply permit or forbid specific dyads or sets of dyads from changing), arbitrary combinations should be possible.</p>
observational	Inherit observational constraints rather than model constraints.
monitor	A one-sided formula specifying one or more terms whose value is to be monitored. These terms are appended to the model, along with a coefficient of 0, so their statistics are returned. An <a href="#">ergm_model</a> object can be passed as well.
statonly	Logical: If <code>TRUE</code> , return only the network statistics, not the network(s) themselves. Deprecated in favor of <code>output=</code> .
esteq	Logical: If <code>TRUE</code> , compute the sample estimating equations of an ERGM: if the model is non-curved, all non-offset statistics are returned either way, but if the model is curved, the score estimating function values (3.1) by Hunter and Handcock (2006) are returned instead, relative to the initial network, which for the <code>ergm</code> method defaults to the LHS network.
output	<p>Normally character, one of "network" (default), "stats", "edgelist", or "ergm_state": determines the output format. Partial matching is performed.</p> <p>Alternatively, a function with prototype <code>function(ergm_state, chain, iter, ...)</code> that is called for each returned network, and its return value, rather than the network itself, is stored. This can be used to, for example, store the simulated networks to disk without storing them in memory or compute network statistics not implemented using the ERGM API, without having to store the networks themselves.</p>

simplify	Logical: If TRUE the output is "simplified": sampled networks are returned in a single list, statistics from multiple parallel chains are stacked, etc.. This makes it consistent with behavior prior to ergm 3.10.
sequential	Logical: If FALSE, each of the nsim simulated Markov chains begins at the initial network. If TRUE, the end of one simulation is used as the start of the next. Irrelevant when nsim=1.
control	A list of control parameters for algorithm tuning, typically constructed with <code>control.simulate.ergm()</code> or <code>control.simulate.formula()</code> , which have different defaults. Their documentation gives the the list of recognized control parameters and their meaning. The more generic utility <code>snctrl()</code> (StatNet CONTRoL) also provides argument completion for the available control functions and limited argument name checking.
verbose	A logical or an integer to control the amount of progress and diagnostic information to be printed. FALSE/0 produces minimal output, with higher values producing more detail. Note that very high values (5+) may significantly slow down processing.
do.sim	Logical; a deprecated interface superseded by <code>return.args</code> , that saves the inputs to the next level of the function.
return.args	Character; if not NULL, the <code>simulate</code> method for that particular class will, instead of proceeding for simulation, instead return its arguments as a list that can be passed as a second argument to <code>do.call()</code> or a lower-level function such as <code>ergm_MCMC_sample()</code> . This can be useful if, for example, one wants to run several simulations with varying coefficients and does not want to reinitialize the model and the proposal every time. Valid inputs at this time are "formula", "ergm_model", and one of the "ergm_state" classes, for the three respective stopping points.

## Details

A sample of networks is randomly drawn from the specified model. The model is specified by the first argument of the function. If the first argument is a `formula` then this defines the model. If the first argument is the output of a call to `ergm()` then the model used for that call is the one fit – and unless `coef` is specified, the sample is from the MLE of the parameters. If neither of those are given as the first argument then a Bernoulli network is generated with the probability of ties defined by `prob` or `coef`.

Note that the first network is sampled after `burnin` steps, and any subsequent networks are sampled each `interval` steps after the first.

More information can be found by looking at the documentation of `ergm()`.

## Value

If `output=="stats"` an `mcmc` object containing the simulated network statistics. If `control$parallel>0`, an `mcmc.list` object. If `simplify=TRUE` (the default), these would then be "stacked" and converted to a standard `matrix`. A logical vector indicating whether or not the term had come from the `monitor= formula` is stored in `attr()`-style attribute "monitored".

Otherwise, a representation of the simulated network is returned, in the form specified by output. In addition to a network representation or a list thereof, they have the following `attr()`-style attributes:

`formula` The `formula` used to generate the sample.  
`stats` An `mcmc` or `mcmc.list` object as above.  
`control` Control parameters used to generate the sample.  
`constraints` Constraints used to generate the sample.  
`reference` The reference measure for the sample.  
`monitor` The monitoring formula.  
`response` The edge attribute used as a response.

The following are the permitted network formats:

"network" A `network` object.  
"edgelist" An `edgelist` representation of the network, or a list thereof, depending on `nsim`.  
"ergm\_state" `ergm_state`, a semi-internal representation of a network consisting of a `network` object emptied of edges, with an attached edgelist matrix.

If `nsim > 1`, these objects are returned in a list, with class `network.list`.

If `simplify==FALSE`, the networks are returned as a nested list, with outer list being the parallel chain (including 1 for no parallelism) and inner list being the samples within that chains (including 1, if one network per chain). It is assigned an additional class, `network.list.list`. If `TRUE`, they are concatenated, and if a total of one network had been simulated, the network itself will be returned.

## Functions

- `simulate(ergm_state_full)`: a low-level function to simulate from an `ergm_state` object.

## Skipping MCMC iterations (advanced)

In some scenarios, it is helpful to forbid certain network configurations from being sampled this can be specified using `constraints`, or by creating an `offset()` term which has value 0 if the network is allowed and positive (negative) if the network is not, with offset coefficient set to `-Inf` (`+Inf`). Sometimes, however, a permitted configuration can be reached by "passing through" a forbidden one. For example, if isolates are possible but not nodes with degree exactly 1. Then, an offset term with coefficient `NaN` (not `NA`!) will cause the MCMC to not terminate as long as the value of that offset term is different from 0.

Note that this means that MCMC is not guaranteed to terminate, and there are very few safeguards at this time.

## Note

The actual `network` method for `simulate_formula()` is actually called `.simulate_formula.network()` and is also exported as an object. This allows it to be overridden by extension packages, such as `tergm`, but also accessed directly when needed.

`simulate.ergm_model()` is a lower-level interface, providing a `simulate()` method for the `ergm_model` class. The `basis` argument is required; `monitor`, if passed, must be an `ergm_model` as well; and `constraints` can be an `ergm_proposal` object instead.

### See Also

`ergm()`, `network`, `ergm_MCMC_sample()` for a demonstration of `return.args=`.

### Examples

```
#
# Let's draw from a Bernoulli model with 16 nodes
# and density 0.5 (i.e., coef = c(0,0))
#
g.sim <- simulate(network(16) ~ edges + mutual, coef=c(0, 0))
#
# What are the statistics like?
#
summary(g.sim ~ edges + mutual)
#
# Now simulate a network with higher mutuality
#
g.sim <- simulate(network(16) ~ edges + mutual, coef=c(0,2))
#
# How do the statistics look?
#
summary(g.sim ~ edges + mutual)
#
# Let's draw from a Bernoulli model with 16 nodes
# and tie probability 0.1
#
g.use <- network(16,density=0.1,directed=FALSE)
#
# Starting from this network let's draw 3 realizations
# of a edges and 2-star network
#
# Here, we also use control.simulate() to specify some MCMC
# settings. We could also use more explicitly
# control.simulate.formula() or snctrl().
g.sim <- simulate(~edges+kstar(2), nsim=3, coef=c(-1.8,0.03),
                 basis=g.use, control=control.simulate(
                 MCMC.burnin=1000,
                 MCMC.interval=100))

g.sim
summary(g.sim)
#
# attach the Florentine Marriage data
#
data(florentine)
#
# fit an edges and 2-star model using the ergm function
#
```

```

gest <- ergm(flomarriage ~ edges + kstar(2))
summary(gest)
#
# Draw from the fitted model (statistics only), and observe the number
# of triangles as well.
#
g.sim <- simulate(gest, nsim=10,
                 monitor=~triangles, output="stats",
                 control=control.simulate.ergm(MCMC.burnin=1000, MCMC.interval=100))
g.sim

# Custom output: store the edgcount (computed in R), iteration index, and chain index.
output.f <- function(x, iter, chain, ...){
  list(nedges = network.edgcount(as.network(x)),
       chain = chain, iter = iter)
}
g.sim <- simulate(gest, nsim=3,
                 output=output.f, simplify=FALSE,
                 control=control.simulate.ergm(MCMC.burnin=1000, MCMC.interval=100))
unclass(g.sim)

```

---

simulate.formula	<i>A simulate Method for formula objects that dispatches based on the Left-Hand Side</i>
------------------	--

---

## Description

This method evaluates the left-hand side (LHS) of the given formula and dispatches it to an appropriate method based on the result by setting a nonce class name on the formula.

## Usage

```

## S3 method for class 'formula'
simulate(object, nsim = 1, seed = NULL, ..., basis, newdata, data)

## S3 method for class 'formula_lhs'
simulate(object, nsim = 1, seed = NULL, ...)

```

## Arguments

object	a one- or two-sided <a href="#">formula</a> .
nsim, seed	number of realisations to simulate and the random seed to use; see <a href="#">simulate()</a> .
...	additional arguments to methods.
basis	if given, overrides the LHS of the formula for the purposes of dispatching.
newdata, data	if passed, the object's LHS is evaluated in this environment; at most one of the two may be passed. The dispatching works as follows:

1. If `basis` is not passed, and the formula has an LHS the expression on the LHS of the formula in the object is evaluated in the environment `newdata` or `data` (if given), in any case enclosed by the environment of object. Otherwise, `basis` is used.
2. The result is set as an attribute `".Basis"` on object. If there is no `basis` or LHS, it is not set.
3. The class vector of object has `c("formula_lhs_CLASS", "formula_lhs")` prepended to it, where `CLASS` is the class of the LHS value or `basis`. If LHS or `basis` has multiple classes, they are all prepended; if there is no LHS or `basis`, `c("formula_lhs_", "formula_lhs")` is.
4. `simulate()` generic is evaluated on the new object, with all arguments passed on, excluding `basis`; if `newdata` or `data` are missing, they too are not passed on. The evaluation takes place in the parent's environment.

A "method" to receive a formula whose LHS evaluates to `CLASS` can therefore be implemented by a function `simulate.formula_lhs_\var{CLASS}()`. This function can expect a `formula` object, with additional attribute `.Basis` giving the evaluated LHS (so that it does not need to be evaluated again).

## Functions

- `simulate(formula_lhs)`: A function to catch the situation when there is no method implemented for the class to which the LHS evaluates.

## See Also

`simulate.ergm()` family of functions, which uses this interface.

---

smalldiff-ergmTerm      *Number of ties between actors with similar attribute values*

---

## Description

This term adds one statistic, having as its value the number of edges in the network for which the incident actors' attribute values differ less than `cutoff` ; that is, number of edges between `i` to `j` such that `abs(attr[i]-attr[j])<cutoff` .

## Usage

```
# binary: smalldiff(attr, cutoff)
```

## Arguments

<code>attr</code>	a vertex attribute specification (see <code>Specifying Vertex attributes and Levels (?nodal_attributes)</code> for details.)
<code>maximum</code>	difference in attribute values for ties to be considered

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, quantitative nodal attribute, undirected, binary

---

smallerthan-ergmTerm *Number of dyads with values strictly smaller than a threshold*

---

**Description**

Adds the number of statistics equal to the length of threshold equaling to the number of dyads whose values are exceeded by the corresponding element of threshold .

**Usage**

```
# valued: smallerthan(threshold=0)
```

**Arguments**

threshold      vector of numerical values

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, dyad-independent, undirected, valued

---

snctrl                      *Statnet Control*

---

**Description**

A utility to facilitate argument completion of control lists, reexported from statnet.common.

**Currently recognised control parameters**

This list is updated as packages are loaded and unloaded.

**Package ergm:**

`control.ergm` drop, init, init.method, main.method, force.main, main.hessian, checkpoint, resume, MPLE.samplesize, init.MPLE.samplesize, MPLE.type, MPLE.maxit, MPLE.nonvar, MPLE.nonident, MPLE.nonident.tol, MPLE.covariance.samplesize, MPLE.covariance.method, MPLE.covariance.sim.burnin, MPLE.covariance.sim.interval, MPLE.check, MPLE.constraints.ignore, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, MCMC.interval, MCMC.burnin, MCMC.samplesize, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxruns, MCMC.effectiveSize.burnin, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max, MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC, MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.return.stats, MCMC.runtime.traceplot, MCMC.maxedges, MCMC.addto.se, MCMC.packagenames, SAN.maxit, SAN.nsteps.times, SAN, MCMLE.termination, MCMLE.maxit, MCMLE.conv.min.pval, MCMLE.confidence, MCMLE.confidence.boost, MCMLE.confidence.boost.lag, MCMLE.NR.maxit, MCMLE.NR.reltol, obs.MCMC.mul, obs.MCMC.samplesize, obs.MCMC.samplesize, obs.MCMC.effectiveSize, obs.MCMC.interval.mul, obs.MCMC.interval, obs.MCMC.burnin.mul, obs.MCMC.burnin, obs.MCMC.prop, obs.MCMC.prop.weights, obs.MCMC.prop.args, obs.MCMC.impute.min\_informative, obs.MCMC.impute.default\_density, MCMLE.min.depfac, MCMLE.sampszie.boost.pow, MCMLE.MCMC.precision, MCMLE.MCMC.max.ESS.frac, MCMLE.metric, MCMLE.method, MCMLE.dampening, MCMLE.dampening.min.ess, MCMLE.dampening.level, MCMLE.steplength.margin, MCMLE.steplength, MCMLE.steplength.parallel, MCMLE.sequential, MCMLE.density.guard.min, MCMLE.density.guard, MCMLE.effectiveSize, obs.MCMLE.effectiveSize, MCMLE.interval, MCMLE.burnin, MCMLE.samplesize.per\_theta, MCMLE.samplesize.min, MCMLE.samplesize, obs.MCMLE.samplesize.per\_theta, obs.MCMLE.samplesize.min, obs.MCMLE.samplesize, obs.MCMLE.interval, obs.MCMLE.burnin, MCMLE.steplength.solver, MCMLE.last.boost, MCMLE.steplength.esteq, MCMLE.steplength.miss.sample, MCMLE.steplength.min, MCMLE.effectiveSize.interval\_drop, MCMLE.save\_intermediates, MCMLE.nonvar, MCMLE.nonident, MCMLE.nonident.tol, SA.phase1\_n, SA.initial\_gain, SA.nsubphases, SA.min.iterations, SA.max.iterations, SA.phase3\_n, SA.interval, SA.burnin, SA.samplesize, CD.samplesize.per\_theta, obs.CD.samplesize.per\_theta, CD.nsteps, CD.multiplicity, CD.nsteps.obs, CD.multiplicity.obs, CD.maxit, CD.conv.min.pval, CD.NR.maxit, CD.NR.reltol, CD.metric, CD.method, CD.dampening, CD.dampening.min.ess, CD.dampening.level, CD.steplength.margin, CD.steplength, CD.adaptive.epsilon, CD.steplength.esteq, CD.steplength.miss.sample, CD.steplength.min, CD.steplength.parallel, CD.steplength.solver, loglik, term.options, seed, parallel, parallel.type, parallel.version.check, parallel.inherit.MT, ...

`control.ergm.bridge` bridge.nsteps, bridge.target.se, bridge.bidirectional, drop, MCMC.burnin, MCMC.burnin.between, MCMC.interval, MCMC.samplesize, obs.MCMC.burnin, obs.MCMC.burnin.between, obs.MCMC.interval, obs.MCMC.samplesize, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, obs.MCMC.prop, obs.MCMC.prop.weights, obs.MCMC.prop.args, MCMC.maxedges, MCMC.packagenames, term.options, seed, parallel, parallel.type, parallel.version.check, parallel.inherit.MT, ...

`control.ergm3` drop, init, init.method, main.method, force.main, main.hessian, checkpoint, resume, MPLE.samplesize, init.MPLE.samplesize, MPLE.type, MPLE.maxit, MPLE.nonvar, MPLE.nonident, MPLE.nonident.tol, MPLE.covariance.samplesize, MPLE.covariance.method, MPLE.covariance.sim.burnin, MPLE.covariance.sim.interval, MPLE.check, MPLE.constraints.ignore, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, MCMC.interval, MCMC.burnin, MCMC.samplesize, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxruns, MCMC.effectiveSize.burnin, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max, MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC, MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.return.stats, MCMC.runtime.traceplot, MCMC.maxedges, MCMC.addto.se, MCMC.packagenames, SAN.maxit, SAN.nsteps.times, SAN, MCMLE.termination,

MCMLE.maxit, MCMLE.conv.min.pval, MCMLE.confidence, MCMLE.confidence.boost, MCMLE.confidence.boos  
 MCMLE.confidence.boost.lag, MCMLE.NR.maxit, MCMLE.NR.reltol, obs.MCMC.mul, obs.MCMC.samplesize.m  
 obs.MCMC.samplesize, obs.MCMC.effectiveSize, obs.MCMC.interval.mul, obs.MCMC.interval,  
 obs.MCMC.burnin.mul, obs.MCMC.burnin, obs.MCMC.prop, obs.MCMC.prop.weights, obs.MCMC.prop.args,  
 obs.MCMC.impute.min\_informative, obs.MCMC.impute.default\_density, MCMLE.min.depfac,  
 MCMLE.sampsiz.boost.pow, MCMLE.MCMC.precision, MCMLE.MCMC.max.ESS.frac, MCMLE.metric,  
 MCMLE.method, MCMLE.dampening, MCMLE.dampening.min.ess, MCMLE.dampening.level,  
 MCMLE.steplength.margin, MCMLE.steplength, MCMLE.steplength.parallel, MCMLE.sequential,  
 MCMLE.density.guard.min, MCMLE.density.guard, MCMLE.effectiveSize, obs.MCMLE.effectiveSize,  
 MCMLE.interval, MCMLE.burnin, MCMLE.samplesize.per\_theta, MCMLE.samplesize.min,  
 MCMLE.samplesize, obs.MCMLE.samplesize.per\_theta, obs.MCMLE.samplesize.min,  
 obs.MCMLE.samplesize, obs.MCMLE.interval, obs.MCMLE.burnin, MCMLE.steplength.solver,  
 MCMLE.last.boost, MCMLE.steplength.esteq, MCMLE.steplength.miss.sample, MCMLE.steplength.min,  
 MCMLE.effectiveSize.interval\_drop, MCMLE.save\_intermediates, MCMLE.nonvar, MCMLE.nonident,  
 MCMLE.nonident.tol, SA.phase1\_n, SA.initial\_gain, SA.nsubphases, SA.min.iterations,  
 SA.max.iterations, SA.phase3\_n, SA.interval, SA.burnin, SA.samplesize, CD.samplesize.per\_theta,  
 obs.CD.samplesize.per\_theta, CD.nsteps, CD.multiplicity, CD.nsteps.obs, CD.multiplicity.obs,  
 CD.maxit, CD.conv.min.pval, CD.NR.maxit, CD.NR.reltol, CD.metric, CD.method, CD.dampening,  
 CD.dampening.min.ess, CD.dampening.level, CD.steplength.margin, CD.steplength,  
 CD.adaptive.epsilon, CD.steplength.esteq, CD.steplength.miss.sample, CD.steplength.min,  
 CD.steplength.parallel, CD.steplength.solver, loglik, term.options, seed, parallel,  
 parallel.type, parallel.version.check, parallel.inherit.MT, ...

**control.gof.ergm** nsim, MCMC.burnin, MCMC.interval, MCMC.batch, MCMC.prop, MCMC.prop.weights,  
 MCMC.prop.args, MCMC.maxedges, MCMC.packagenames, MCMC.runtime.traceplot, network.output,  
 seed, parallel, parallel.type, parallel.version.check, parallel.inherit.MT

**control.gof.formula** nsim, MCMC.burnin, MCMC.interval, MCMC.batch, MCMC.prop, MCMC.prop.weights,  
 MCMC.prop.args, MCMC.maxedges, MCMC.packagenames, MCMC.runtime.traceplot, network.output,  
 seed, parallel, parallel.type, parallel.version.check, parallel.inherit.MT

**control.logLik.ergm** bridge.nsteps, bridge.target.se, bridge.bidirectional, drop,  
 MCMC.burnin, MCMC.interval, MCMC.samplesize, obs.MCMC.samplesize, obs.MCMC.interval,  
 obs.MCMC.burnin, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, obs.MCMC.prop,  
 obs.MCMC.prop.weights, obs.MCMC.prop.args, MCMC.maxedges, MCMC.packagenames,  
 term.options, seed, parallel, parallel.type, parallel.version.check, parallel.inherit.MT,  
 ...

**control.san** SAN.maxit, SAN.tau, SAN.invcov, SAN.invcov.diag, SAN.nsteps.alloc, SAN.nsteps,  
 SAN.samplesize, SAN.prop, SAN.prop.weights, SAN.prop.args, SAN.packagenames,  
 SAN.ignore.finite.offsets, term.options, seed, parallel, parallel.type, parallel.version.check,  
 parallel.inherit.MT

**control.simulate** MCMC.burnin, MCMC.interval, MCMC.prop, MCMC.prop.weights, MCMC.prop.args,  
 MCMC.batch, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxruns,  
 MCMC.effectiveSize.burnin.pval, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max,  
 MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC,  
 MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.maxedges,  
 MCMC.packagenames, MCMC.runtime.traceplot, network.output, term.options, parallel,  
 parallel.type, parallel.version.check, parallel.inherit.MT, ...

**control.simulate.ergm** MCMC.burnin, MCMC.interval, MCMC.scale, MCMC.prop, MCMC.prop.weights,  
 MCMC.prop.args, MCMC.batch, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxr  
 MCMC.effectiveSize.burnin.pval, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max,

MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC, MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.maxedges, MCMC.packagenames, MCMC.runtime.traceplot, network.output, term.options, parallel, parallel.type, parallel.version.check, parallel.inherit.MT, ...

`control.simulate.formula` MCMC.burnin, MCMC.interval, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, MCMC.batch, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxr, MCMC.effectiveSize.burnin.pval, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max, MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC, MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.maxedges, MCMC.packagenames, MCMC.runtime.traceplot, network.output, term.options, parallel, parallel.type, parallel.version.check, parallel.inherit.MT, ...

`control.simulate.formula.ergm` MCMC.burnin, MCMC.interval, MCMC.prop, MCMC.prop.weights, MCMC.prop.args, MCMC.batch, MCMC.effectiveSize, MCMC.effectiveSize.damp, MCMC.effectiveSize.maxr, MCMC.effectiveSize.burnin.pval, MCMC.effectiveSize.burnin.min, MCMC.effectiveSize.burnin.max, MCMC.effectiveSize.burnin.nmin, MCMC.effectiveSize.burnin.nmax, MCMC.effectiveSize.burnin.PC, MCMC.effectiveSize.burnin.scl, MCMC.effectiveSize.order.max, MCMC.maxedges, MCMC.packagenames, MCMC.runtime.traceplot, network.output, term.options, parallel, parallel.type, parallel.version.check, parallel.inherit.MT, ...

### See Also

`statnet.common::snctrl()`

---

sociality-ergmTerm      *Undirected degree*

---

### Description

This term adds one network statistic for each node equal to the number of ties of that node. For directed networks, see sender and receiver .

### Usage

```
# binary: sociality(attr=NULL, base=1, levels=NULL, nodes=-1)
```

```
# valued: sociality(attr=NULL, base=1, levels=NULL, nodes=-1, form="sum")
```

### Arguments

attr, levels	this optional argument is deprecated and will be replaced with a more elegant implementation in a future release. In the meantime, it specifies a categorical vertex attribute (see Specifying Vertex attributes and Levels (?nodal_attributes) for details). If provided, this term only counts ties between nodes with the same value of the attribute (an actor-specific version of the nodematch term), restricted to be one of the values specified by (also deprecated) levels if levels is not NULL .
base	deprecated

nodes	By default, nodes=-1 means that the statistic for the first node will be omitted, but this argument may be changed to control which statistics are included just as for the nodes argument of sender and receiver terms.
form	how to aggregate tie values in a valued ERGM: "sum" (the default) for a statistic of the form $\sum_{i,j} x_{i,j} y_{i,j}$ , where $y_{i,j}$ is the value of dyad $(i, j)$ and $x_{i,j}$ is the term's covariate associated with it; and "nonzero" with the edge considered to be present if its value is not 0. See <a href="#">ergmTerm</a> for more information.

**Note**

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and levels are passed, levels overrides base. See [nodal\\_attributes](#).

The argument base is retained for backwards compatibility and may be removed in a future version. When both base and nodes are passed, nodes overrides base. See [nodal\\_attributes](#).

This term can only be used with undirected networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, dyad-independent, undirected, binary, valued

---

sparse-ergmHint	<i>Sparse network</i>
-----------------	-----------------------

---

**Description**

The network is sparse. This typically results in a Tie-Non-Tie (TNT) proposal regime.

**Usage**

```
# sparse
```

**See Also**

[ergmHint](#) for index of constraints and hints currently visible to the package.

**Keywords:** dyad-independent

---

spectrum0.mvar      *Multivariate version of coda's [spectrum0.ar\(\)](#).*

---

### Description

Its return value, divided by `nrow(cbind(x))`, is the estimated variance-covariance matrix of the sampling distribution of the mean of `x` if `x` is a multivariate time series with  $AR(p)$  structure, with  $p$  determined by AIC.

### Usage

```
spectrum0.mvar(
  x,
  order.max = NULL,
  aic = is.null(order.max),
  tol = .Machine$double.eps^0.5,
  ...
)
```

### Arguments

<code>x</code>	a matrix with observations in rows and variables in columns.
<code>order.max</code>	maximum (or fixed) order for the AR model.
<code>aic</code>	use AIC to select the order (up to <code>order.max</code> ).
<code>tol</code>	tolerance used in detecting multicollinearity. See Note below.
<code>...</code>	additional arguments to <a href="#">ar()</a> .

### Value

A square matrix with dimension equalling to the number of columns of `x`, with an additional attribute "inf1" giving the factor by which the effective sample size is reduced due to autocorrelation, according to the Vats et al. (2019) estimate for ESS.

### Note

[ar\(\)](#) fails if `crossprod(x)` is singular. This is remedied as follows:

1. Standardize the variables.
2. Use the eigenvectors to map the variables onto their principal components.
3. Use the eigenvalues to standardize the principal components.
4. Drop those components whose standard deviation differs from 1 by more than `tol`. This should filter out redundant components or those too numerically unstable.
5. Call [ar\(\)](#) and calculate the variance.
6. Reverse the mapping in steps 1-4 to obtain the variance of the original data.

---

 StdNormal-ergmReference

*Standard Normal reference*


---

### Description

Specifies each dyad's baseline distribution to be the normal distribution with mean 0 and variance 1.

### Usage

```
# StdNormal
```

### See Also

[ergmReference](#) for index of reference distributions currently visible to the package.

**Keywords:** continuous

---

 strat-ergmHint

*Stratify Proposed Toggles by Mixing Type on a Vertex Attribute*


---

### Description

Proposed toggles are stratified according to mixing type on a vertex attribute.

### Usage

```
# strat(attr=NULL, pmat=NULL, empirical=FALSE)
```

### Details

The user may pass a vertex attribute `attr` as an argument (the default for `attr` gives every vertex the same attribute value), and may also pass a matrix of weights `pmat` (the default for `pmat` gives equal weight to each mixing type). See [Specifying Vertex Attributes and Levels for details](#) on specifying vertex attributes. The matrix `pmat`, if specified, must have the same dimensions as a mixing matrix for the network and vertex attribute under consideration, and the correspondence between rows and columns of `pmat` and values of `attr` is the same as for a mixing matrix.

The interpretation is that  $\text{pmat}[i, j] / \text{sum}(\text{pmat})$  is the probability of proposing a toggle for mixing type  $(i, j)$ . (For undirected, unipartite networks, `pmat` is first symmetrized, and then entries below the diagonal are set to zero. Only entries on or above the diagonal of the symmetrized `pmat` are considered when making proposals. This accounts for the convention that mixing is undirected in an undirected, unipartite network: a tail of type  $i$  and a head of type  $j$  has the same mixing type as a tail of type  $j$  and a head of type  $i$ .)

As an alternative way of specifying `pmat`, the user may pass `empirical = TRUE` to use the mixing matrix of the network beginning the MCMC chain as `pmat`. In order for this to work, that network should have a reasonable (in particular, nonempty) edge set.

While some mixing types may be assigned zero proposal probability (either with a direct specification of `pmat` or with `empirical = TRUE`), this will not be recognized as a constraint by all components of `ergm`, and should be used with caution.

### See Also

[ergmHint](#) for index of constraints and hints currently visible to the package.

**Keywords:** dyad-independent

---

Sum-ergmTerm	<i>A sum (or an arbitrary linear combination) of one or more formulas</i>
--------------	---

---

### Description

This operator sums up the RHS statistics of the input formulas elementwise.

### Usage

```
# binary: Sum(formulas, label)
```

```
# valued: Sum(formulas, label)
```

### Arguments

formulas	<p>a list (constructed using <code>list()</code> or <code>c()</code>) of <code>ergm()</code>-style formulas whose RHS gives the statistics to be evaluated, or a single formula.</p> <p>If a formula in the list has an LHS, it is interpreted as follows:</p> <ul style="list-style-type: none"> <li>• a numeric scalar: Network statistics of this formula will be multiplied by this.</li> <li>• a numeric vector: Corresponding network statistics of this formula will be multiplied by this.</li> <li>• a numeric matrix: Vector of network statistics will be pre-multiplied by this.</li> <li>• a character string: One of several predefined linear combinations. Currently supported presets are as follows: <ul style="list-style-type: none"> <li>– "sum" Network statistics of this formula will be summed up; equivalent to <code>matrix(1, 1, p)</code>, where <code>p</code> is the length of the network statistic vector.</li> <li>– "mean" Network statistics of this formula will be averaged; equivalent to <code>matrix(1/p, 1, p)</code>, where <code>p</code> is the length of the network statistic vector.</li> </ul> </li> </ul>
label	<p>used to specify the names of the elements of the resulting term sum vector. If <code>label</code> is a character vector of length 1, it will be recycled with indices appended. If a function is specified, <code>formulas</code> parameter names are extracted and their list of character vectors is passed <code>label</code>.</p>

**Details**

Note that each formula must either produce the same number of statistics or be mapped through a matrix to produce the same number of statistics.

A single formula is also permitted. This can be useful if one wishes to, say, scale or sum up the statistics returned by a formula.

Offsets are ignored unless there is only one formula and the transformation only scales the statistics (i.e., the effective transformation matrix is diagonal).

Curved models are supported, subject to some limitations. In particular, the first model's etamap will be used, overwriting the others. If label is not of length 1, it should have an attr -style attribute "curved" specifying the names for the curved parameters.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** operator, binary, valued

---

sum-ergmTerm	<i>Sum of dyad values (optionally taken to a power)</i>
--------------	---

---

**Description**

This term adds one statistic equal to the sum of dyad values taken to the power pow.

**Usage**

```
# valued: sum(pow=1)
```

**Arguments**

pow                    power of dyad values. Defaults to 1.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, undirected, valued

**Description**

`base::summary()` method for `ergm()` fits.

**Usage**

```
## S3 method for class 'ergm'
summary(
  object,
  ...,
  correlation = FALSE,
  covariance = FALSE,
  total.variation = TRUE
)

## S3 method for class 'summary.ergm'
print(
  x,
  digits = max(3, getOption("digits") - 3),
  correlation = x$correlation,
  covariance = x$covariance,
  signif.stars = getOption("show.signif.stars"),
  eps.Pvalue = 1e-04,
  print.formula = FALSE,
  print.fitinfo = TRUE,
  print.coefmat = TRUE,
  print.message = TRUE,
  print.deviiances = TRUE,
  print.drop = TRUE,
  print.offset = TRUE,
  print.call = TRUE,
  print.lindep = TRUE,
  ...
)
```

**Arguments**

<code>object</code>	an object of class <code>ergm</code> , usually, a result of a call to <code>ergm()</code> .
<code>...</code>	For <code>summary.ergm()</code> additional arguments are passed to <code>logLik.ergm()</code> . For <code>print.summary.ergm()</code> , to <code>stats::printCoefmat()</code> .
<code>correlation</code>	logical; if TRUE, the correlation matrix of the estimated parameters is returned and printed.

covariance	logical; if TRUE, the covariance matrix of the estimated parameters is returned and printed.
total.variation	logical; if TRUE, the standard errors reported in the Std. Error column are based on the sum of the likelihood variation and the MCMC variation. If FALSE only the likelihood variation is used. The $p$ -values are based on this source of variation.
x	object of class <code>summary.ergm</code> returned by <code>summary.ergm()</code> .
digits	significant digits for coefficients
signif.stars	whether to print dots and stars to signify statistical significance. See <code>print.summary.lm()</code> .
eps.Pvalue	$p$ -values below this level will be printed as "<eps.Pvalue".
print.formula, print.fitinfo, print.coefmat, print.message, print.deviances, print.drop, print.lindep, print.offset, print.call	which components of the fit summary to print.

## Details

`summary.ergm()` tries to be smart about formatting the coefficients, standard errors, etc.

The default printout of the summary object contains the call, number of iterations used, null and residual deviances, and the values of AIC and BIC (and their MCMC standard errors, if applicable).

The coefficient table contains the following columns:

- Estimate, Std. Error - parameter estimates and their standard errors
- MCMC % - if `total.variation=TRUE` (default) the percentage of standard error attributable to MCMC estimation process rounded to an integer. See also `vcov.ergm()` and its sources argument.
- z value,  $\Pr(>|z|)$  - z-test and  $p$ -values

## Value

The returned object is a list of class "ergm.summary" with the following elements:

formula	ERGM model formula
call	R call used to fit the model
correlation, covariance	whether to print correlation/covariance matrices of the estimated parameters
pseudolikelihood	was the model estimated with MPLE
independence	is the model dyad-independent
control	the <code>control.ergm()</code> object used
samplesize	MCMC sample size
message	optional message on the validity of the standard error estimates
null.lik.0	It is TRUE if the null model likelihood has not been calculated. See <code>logLikNull()</code>
devtext, devtable	Deviance type and table

aic, bic            values of AIC and BIC  
 coefficients       matrices with model parameters and associated statistics  
 asycov            asymptotic covariance matrix  
 asyse             asymptotic standard error matrix  
 offset, drop, estimate, iterations, mle.lik, null.lik  
                     see documentation of the object returned by [ergm\(\)](#)

### See Also

The model fitting function [ergm\(\)](#), [print.ergm\(\)](#), and [base::summary\(\)](#). Function [stats::coef\(\)](#) will extract the matrix of coefficients with standard errors, t-statistics and p-values.

### Examples

```

data(florentine)

x <- ergm(flomarriage ~ density)
summary(x)

```

---

summary.formula	<i>Calculation of network or graph statistics or other attributes specified on a formula</i>
-----------------	--

---

### Description

Most generally, this function computes those summaries of the object on the LHS of the formula that are specified by its RHS. In particular, if given a network as its LHS and [ergmTerm](#) on its RHS, it computes the sufficient statistics associated with those terms.

### Usage

```

## S3 method for class 'formula'
summary(object, ...)

```

### Arguments

object            A formula having as its LHS a [network](#) object or a matrix that can be coerced to a [network](#) object, a [network.list](#), or other types to be summarized using a formula. (See ‘[methods\(‘summary\\_formula’\)](#)’ for the possible LHS types.)  
 ...               further arguments passed to or used by methods.

### Details

In practice, [summary.formula\(\)](#) is a thin wrapper around the [summary\\_formula\(\)](#) generic, which dispatches methods based on the class of the LHS of the formula.

**Value**

A vector of statistics specified in RHS of the formula.

**See Also**

[ergm\(\)](#), [network\(\)](#), [ergmTerm](#)

**Examples**

```
#
# Lets look at the Florentine marriage data
#
data(florentine)
#
# test the summary_formula function
#
summary(flomarriage ~ edges + kstar(2))
m <- as.matrix(flomarriage)
summary(m ~ edges) # twice as large as it should be
summary(m ~ edges, directed=FALSE) # Now it's correct
```

---

Symmetrize-ergmTerm     *Evaluation on symmetrized (undirected) network*

---

**Description**

Evaluates the terms in formula on an undirected network constructed by symmetrizing the LHS network using one of four rules:

1. "weak"/"max" A tie  $(i, j)$  is present in the constructed network if the LHS network has either tie  $(i, j)$  or  $(j, i)$  (or both). For a valued network, the maximum is used.
2. "strong"/"min" A tie  $(i, j)$  is present in the constructed network if the LHS network has both tie  $(i, j)$  and tie  $(j, i)$ . For a valued network, the minimum is used.
3. "upper" A tie  $(i, j)$  is present in the constructed network if the LHS network has tie  $(\min(i, j), \max(i, j))$  : the upper triangle of the LHS network.
4. "lower" A tie  $(i, j)$  is present in the constructed network if the LHS network has tie  $(\max(i, j), \min(i, j))$  : the lower triangle of the LHS network.

**Usage**

```
# binary: Symmetrize(formula, rule="weak")
# valued: Symmetrize(formula, rule="weak")
```

**Arguments**

formula	a one-sided <code>ergm()</code> -style formula with the terms to be evaluated
rule	one of "weak", "strong", "upper", "lower", "max", or "min"

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, operator, binary, valued

thretrail-ergmTerm     *Three-trails*

**Description**

For an undirected network, this term adds one statistic equal to the number of 3-trails, where a 3-trail is defined as a trail of length three that traverses three distinct edges. Note that a 3-trail need not include four distinct nodes; in particular, a triangle counts as three 3-trails. For a directed network, this term adds four statistics (or some subset of these four), one for each of the four distinct types of directed three-paths. If the nodes of the path are written from left to right such that the middle edge points to the right (R), then the four types are RRR, RRL, LRR, and LRL. That is, an RRR 3-trail is of the form  $i \rightarrow j \rightarrow k \rightarrow l$ , and RRL 3-trail is of the form  $i \rightarrow j \rightarrow k \leftarrow l$ , etc. Like in the undirected case, there is no requirement that the nodes be distinct in a directed 3-trail. However, the three edges must all be distinct. Thus, a mutual tie  $i \leftrightarrow j$  does not count as a 3-trail of the form  $i \rightarrow j \rightarrow i \leftarrow j$ ; however, in the subnetwork  $i \leftrightarrow j \rightarrow k$ , there are two directed 3-trails, one LRR ( $k \leftarrow j \rightarrow i \leftarrow j$ ) and one RRR ( $j \rightarrow i \rightarrow j \leftarrow k$ ).

**Usage**

```
# binary: thretrail(keep=NULL, levels=NULL)
```

```
# binary: threpath(keep=NULL, levels=NULL)
```

**Arguments**

keep	deprecated
levels	specify a subset of the four statistics for directed networks. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**Note**

The argument `keep` is retained for backwards compatibility and may be removed in a future version. When both `keep` and `levels` are passed, `levels` overrides `keep`. See [nodal\\_attributes](#).

This term used to be (inaccurately) called `threpath`. That name has been deprecated and may be removed in a future version.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, undirected, binary

transitive-ergmTerm     *Transitive triads*

**Description**

This term adds one statistic to the model, equal to the number of triads in the network that are transitive. The transitive triads are those of type 120D, 030T, 120U, or 300 in the categorization of Davis and Leinhardt (1972). For details on the 16 possible triad types, see `?triad.classify` in the **sna** package. Note the distinction from the `ttriple` term. This term can only be used with directed networks.

**Usage**

```
# binary: transitive
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, binary

transitiveties-ergmTerm     *Transitive ties*

**Description**

This term adds one statistic, equal to the number of ties  $i \rightarrow j$  such that there exists a two-path from  $i$  to  $j$ . (Related to the `ttriple` term.)

**Usage**

```
# binary: transitiveties(attr=NULL, levels=NULL)
```

**Arguments**

<code>attr</code>	quantitative attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) If set, all three nodes involved ( $i$ , $j$ , and the node on the two-path) must match on this attribute in order for $i \rightarrow j$ to be counted.
<code>levels</code>	TODO (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, triad-related, undirected, binary

transitiveweights-ergmTerm

*Transitive weights*

**Description**

This statistic implements the transitive weights statistic defined by Krivitsky (2012), Equation 13. For each of these options, the first (and the default) is more stable but also more conservative, while the second is more sensitive but more likely to induce a multimodal distribution of networks.

**Usage**

```
# valued: transitiveweights(twopath="min", combine="max", affect="min")
```

**Arguments**

twopath	the minimum of the constituent dyads ( "min" ) or their geometric mean ( "geomean" )
combine	the maximum of the 2-path strengths ( "max" ) or their sum ( "sum" )
affect	the minimum of the focus dyad and the combined strength of the two paths ( "min" ) or their geometric mean ( "geomean" )

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, nonnegative, triad-related, undirected, valued

triadcensus-ergmTerm *Triad census*

**Description**

For a directed network, this term adds one network statistic for each of an arbitrary subset of the 16 possible types of triads categorized by Davis and Leinhardt (1972) as 003, 012, 102, 021D, 021U, 021C, 111D, 111U, 0 and 300 . Note that at least one category should be dropped; otherwise a linear dependency will exist among the 16 statistics, since they must sum to the total number of three-node sets. By default, the category 003 , which is the category of completely empty three-node sets, is dropped. This is considered category zero, and the others are numbered 1 through 15 in the order given above. Each statistic is the count of the corresponding triad type in the network. For details on the 16 types, see ?triad.classify in the **sna** package, on which this code is based. For an undirected network, the triad census is over the four types defined by the number of ties (i.e., 0, 1, 2, and 3).

**Usage**

```
# binary: triadcensus(levels)
```

**Arguments**

**levels** For directed networks, specify a set of terms to add other than the default value of 1:15. For undirected networks, specify which of the four types of ties to include. The default is 1:3 where 0 is dropped. (See [Specifying Vertex attributes and Levels \(?nodal\\_attributes\)](#) for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, triad-related, undirected, binary

---

triadic-ergmHint	<i>Network with strong clustering (triad-closure) effects</i>
------------------	---

---

**Description**

The network has a high clustering coefficient. This typically results in alternating between the Tie-Non-Tie (TNT) proposal and a triad-focused proposal along the lines of that of Wang and Atchadé (2013).

**Usage**

```
# triadic(triFocus = 0.25, type="OTP")

# .triadic(triFocus = 0.25, type = "OTP")
```

**Arguments**

**triFocus** A number between 0 and 1, indicating how often triad-focused proposals should be made relative to the standard proposals.

**type** A string indicating the type of shared partner or path to be considered for directed networks: "OTP" (default for directed), "ITP", "RTP", "OSP", and "ISP"; has no effect for undirected. See the section below on Shared partner types for details.

**Shared partner types**

While there is only one shared partner configuration in the undirected case, nine distinct configurations are possible for directed graphs, selected using the `type` argument. Currently, terms may be defined with respect to five of these configurations; they are defined here as follows (using terminology from Butts (2008) and the relevant package):

- Outgoing Two-path ("OTP"): vertex  $k$  is an OTP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k \rightarrow j$ . Also known as "transitive shared partner".
- Incoming Two-path ("ITP"): vertex  $k$  is an ITP shared partner of ordered pair  $(i, j)$  iff  $j \rightarrow k \rightarrow i$ . Also known as "cyclical shared partner"
- Reciprocated Two-path ("RTP"): vertex  $k$  is an RTP shared partner of ordered pair  $(i, j)$  iff  $i \leftrightarrow k \leftrightarrow j$ .
- Outgoing Shared Partner ("OSP"): vertex  $k$  is an OSP shared partner of ordered pair  $(i, j)$  iff  $i \rightarrow k, j \rightarrow k$ .
- Incoming Shared Partner ("ISP"): vertex  $k$  is an ISP shared partner of ordered pair  $(i, j)$  iff  $k \rightarrow i, k \rightarrow j$ .

By default, outgoing two-paths ("OTP") are calculated. Note that Robins et al. (2009) define closely related statistics to several of the above, using slightly different terminology.

`.triadic()` **versus** `triadic()`

If given a bipartite network, the dotted form will skip silently, whereas the plain form will raise an error, since triadic effects are not possible in bipartite networks. The dotted form is thus suitable as a default argument when the bipartitedness of the network is not known *a priori*.

## References

Butts CT (2008). "A Relational Event Framework for Social Action." *Sociological Methodology*, **38**(1), 155–200. doi:10.1111/j.14679531.2008.00203.x.

Robins G, Pattison P, Wang P (2009). "Closure, Connectivity, and Degree Distributions: Exponential Random Graph (p\*) Models for Directed Social Networks." *Social Networks*, **31**(2), 105–117. doi:10.1016/j.socnet.2008.10.006.

Wang J, Atchadé YF (2013). "Approximate Bayesian Computation for Exponential Random Graph Models for Large Social Networks." *Communications in Statistics - Simulation and Computation*, **43**(2), 359–377. ISSN 1532-4141. doi:10.1080/03610918.2012.703359.

## See Also

[ergmHint](#) for index of constraints and hints currently visible to the package.

**Keywords:** dyad-dependent

**Description**

By default, this term adds one statistic to the model equal to the number of triangles in the network. For an undirected network, a triangle is defined to be any set  $\{(i, j), (j, k), (k, i)\}$  of three edges. For a directed network, a triangle is defined as any set of three edges  $(i \rightarrow j)$  and  $(j \rightarrow k)$  and either  $(k \rightarrow i)$  or  $(k \leftarrow i)$ . The former case is called a "transitive triple" and the latter is called a "cyclic triple", so in the case of a directed network, triangle equals ttriple plus ctriple — thus at most two of these three terms can be in a model.

**Usage**

```
# binary: triangle(attr=NULL, diff=FALSE, levels=NULL)
```

```
# binary: triangles(attr=NULL, diff=FALSE, levels=NULL)
```

**Arguments**

attr, diff	quantitative attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) If attr is specified and diff is FALSE, then the count is restricted to those triples of nodes with equal values of the vertex attribute specified by attr. If attr is specified and diff is TRUE, then one statistic is added for each value of attr, equal to the number of triangles where all three nodes have that value of the attribute.
levels	this optional argument controls which levels of the attribute should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, frequently-used, triad-related, undirected, binary

tripercent-ergmTerm     *Triangle percentage*

**Description**

By default, this term adds one statistic to the model equal to 100 times the ratio of the number of triangles in the network to the sum of the number of triangles and the number of 2-stars not in triangles (the latter is considered a potential but incomplete triangle). In case the denominator equals zero, the statistic is defined to be zero. For the definition of triangle, see [triangle](#). This is often called the mean correlation coefficient. This term can only be used with undirected networks; for directed networks, it is difficult to define the numerator and denominator in a consistent and meaningful way.

**Usage**

```
# binary: tripercent(attr=NULL, diff=FALSE, levels=NULL)
```

**Arguments**

attr, diff	quantitative attribute (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.) If attr is specified and diff is FALSE , then the counts are restricted to those triples of nodes with equal values of the vertex attribute specified by attr . If attr is specified and diff is TRUE , then one statistic is added for each value of attr , equal to the number of triangles where all three nodes have that value of the attribute.
levels	add one statistic for each value specified if diff is TRUE should be included and which should be excluded. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, triad-related, undirected, binary

---

ttriple-ergmTerm	<i>Transitive triples</i>
------------------	---------------------------

---

**Description**

By default, this term adds one statistic to the model, equal to the number of transitive triples in the network, defined as a set of edges  $\{(i \rightarrow j), j \rightarrow k), (i \rightarrow k)\}$  . Note that triangle equals ttriple+ctriple for a directed network, so at most two of the three terms can be in a model.

**Usage**

```
# binary: ttriple(attr=NULL, diff=FALSE, levels=NULL)
```

```
# binary: ttriad
```

**Arguments**

attr	a vertex attribute specification (see <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)
diff	If attr is specified and diff is FALSE , then the count is over the number of transitive triples where all three nodes have the same value of the attribute. If attr is specified and diff is TRUE , then one statistic is added for each value of attr , equal to the number of triangles where all three nodes have that value of the attribute.
levels	add one statistic for each value specified if diff is TRUE. (See <a href="#">Specifying Vertex attributes and Levels (?nodal_attributes)</a> for details.)

**Note**

This term can only be used with directed networks.

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** categorical nodal attribute, directed, triad-related, binary

twopath-ergmTerm      *2-Paths*

**Description**

This term adds one statistic to the model, equal to the number of 2-paths in the network. For a directed network this is defined as a pair of edges  $(i \rightarrow j), (j \rightarrow k)$ , where  $i$  and  $j$  must be distinct. That is, it is a directed path of length 2 from  $i$  to  $k$  via  $j$ . For directed networks a 2-path is also a mixed 2-star but the interpretation is usually different; see `m2star`. For undirected networks a twopath is defined as a pair of edges  $\{i, j\}, \{j, k\}$ . That is, it is an undirected path of length 2 from  $i$  to  $k$  via  $j$ , also known as a 2-star.

**Usage**

```
# binary: twopath
```

**See Also**

[ergmTerm](#) for index of model terms currently visible to the package.

**Keywords:** directed, undirected, binary

Unif-ergmReference      *Continuous Uniform reference*

**Description**

Specifies each dyad's baseline distribution to be continuous uniform between  $a$  and  $b$ :  $h(y) = 1$ , with the support being  $[a, b]$ .

**Usage**

```
# Unif(a,b)
```

**Arguments**

$a, b$       minimum and maximum to the baseline discrete uniform distribution, both inclusive. Both values must be finite.

**See Also**

[ergmReference](#) for index of reference distributions currently visible to the package.

**Keywords:** continuous

---

update.network	<i>Update the edges in a network based on a matrix</i>
----------------	--

---

**Description**

Replaces the edges in a [network](#) object with the edges corresponding to the sociomatrix or edge list specified by new.

**Usage**

```
## S3 method for class 'network'
update(object, ...)

update_network(object, new, ...)

## S3 method for class 'matrix_edgelist'
update_network(object, new, attrname = if (ncol(new) > 2) names(new)[3], ...)

## S3 method for class 'data.frame'
update_network(object, new, attrname = if (ncol(new) > 2) names(new)[3], ...)

## S3 method for class 'matrix'
update_network(object, new, matrix.type = NULL, attrname = NULL, ...)

## S3 method for class 'ergm_state'
update_network(object, new, ...)
```

**Arguments**

object	a <a href="#">network</a> object.
...	Additional arguments; currently unused.
new	Either an adjacency matrix (a matrix of values indicating the presence and/or the value of a tie from i to j) or an edge list (a two-column matrix listing origin and destination node numbers for each edge, with an optional third column for the value of the edge).
attrname	For a network with edge weights gives the name of the edge attribute whose names to set.
matrix.type	One of "adjacency" or "edgelist" telling which type of matrix new is. Default is to use the <a href="#">which.matrix.type()</a> function.

**Value**

A new [network](#) object with the edges specified by `new` and `network` and vertex attributes copied from the input network object. Input network is not modified.

**Functions**

- `update_network()`: dispatcher for network update based on the type of updating information.
- `update_network(matrix_edgelist)`: a method for updating a network based on a matrix-form edgelist
- `update_network(data.frame)`: a method for updating a network based on an edgelist
- `update_network(matrix)`: a method for updating a network based on a matrix
- `update_network(ergm_state)`: a method for updating a network based on an [ergm\\_state](#) object.

**See Also**

[ergm\(\)](#), [network](#)

**Examples**

```
#
data(florentine)
#
# test the network.update function
#
# Create a Bernoulli network
rand.net <- network(network.size(flomarriage))
# store the sociomatrix
rand.mat <- rand.net[,]
# Update the network
update(flomarriage, rand.mat, matrix.type="adjacency")
# Try this with an edgelist
rand.mat <- as.matrix.network.edgelist(flomarriage)[1:5,]
update(flomarriage, rand.mat, matrix.type="edgelist")
```

---

wtd.median

*Weighted Median*


---

**Description**

Compute weighted median.

**Usage**

```
wtd.median(x, na.rm = FALSE, weight = FALSE)
```

**Arguments**

<code>x</code>	Vector of data, same length as <code>weight</code>
<code>na.rm</code>	Logical: Should NAs be stripped before computation proceeds?
<code>weight</code>	Vector of weights

**Details**

Uses a simple algorithm based on sorting.

**Value**

Returns an empirical .5 quantile from a weighted sample.

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